$$\frac{\partial}{\partial p} \log[f(\mathbf{M} \mid p)] = \frac{(M - Np)}{(p - p^2)}$$