$$\frac{b(b+c)(b+2c)\ldots(b+n_1c-c)\,.\,r(r+c)\ldots(r+n_2c-c)}{(b+r)(b+r+c)(b+r+2c)\ldots(b+r+nc-c)}$$