

Top Quark Physics at D0

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Brown University

Particle Physics Seminar at



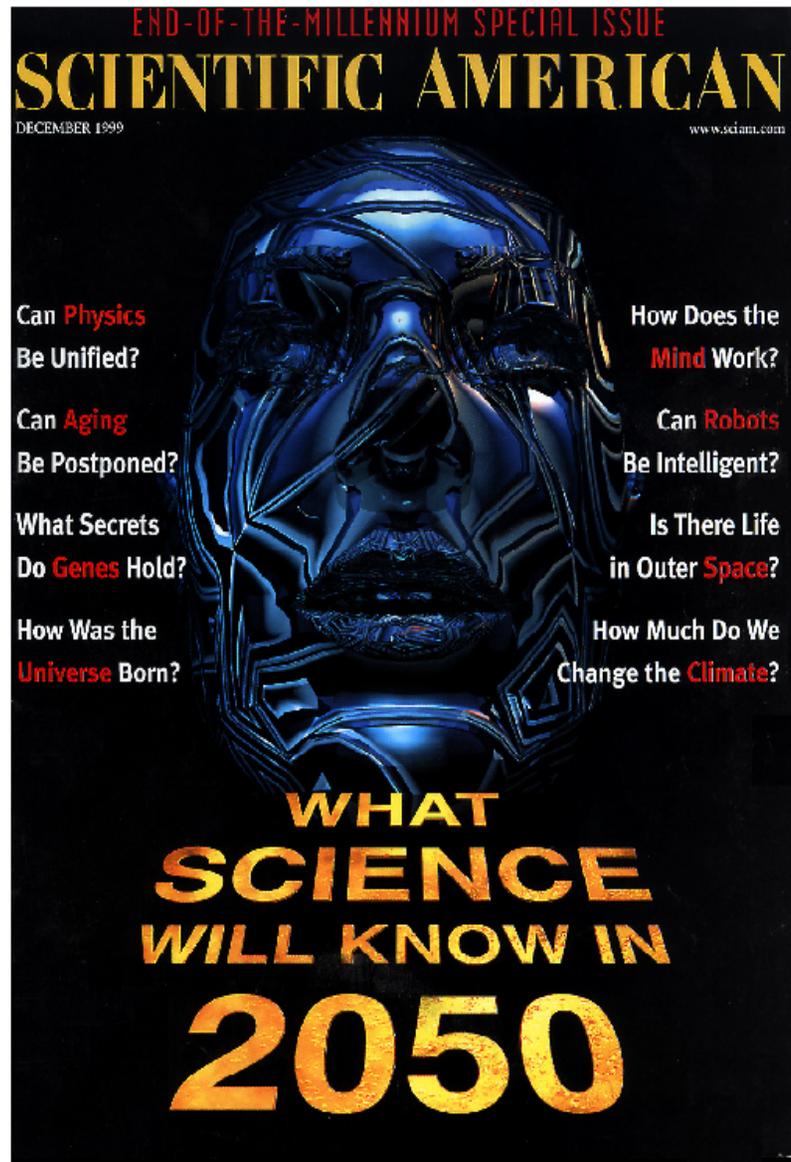
26 May 2011

Can **Physics**
Be Unified ?

Can **Aging**
Be Postponed ?

What Secrets
Do **Genes** Hold ?

How Was the
Universe Born ?



How Does the
Mind Work ?

Can **Robots**
Be Intelligent ?

Is There Life
In Outer **Space**?

How Much Do We
Change the **Climate**?

Big Questions

Can we combine QM and G. Relativity?

Dark energy?
Cosmological constant?

Unification of forces?

Arrow of time

Dark matter?

Correct interpretation
of QM?

Where is antimatter?

Why three generations of
matter?



Black hole information
paradox?

Extra dimensions?

Magnetic monopoles?

Inflation?

Mechanism of symmetry
breaking, Higgs, origin of mass,
mechanism for neutrino masses?

End of universe?

Are there many universes?

Locality in QM (Quantum
entanglement)?

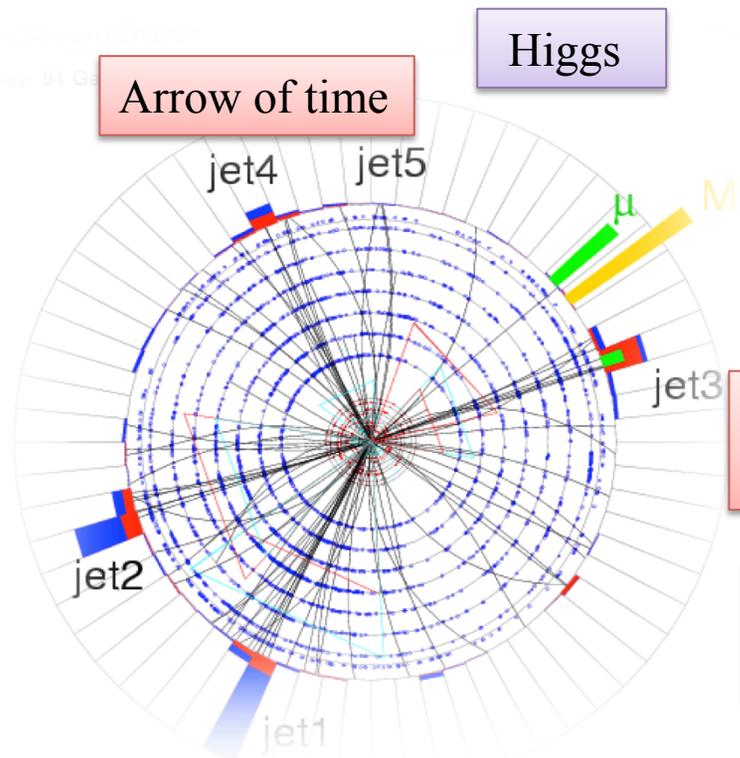
Clues from P-P(Pbar) Collisions?

Unification of forces?

Dark matter?

Where is antimatter?

Can we combine QM and G. Relativity?



Higgs

Correct interpretation of QM?

Why three generations of matter?

Mechanism of symmetry breaking, origin of mass

Extra dimensions?

QCD

B Physics

Electroweak

Top Quark

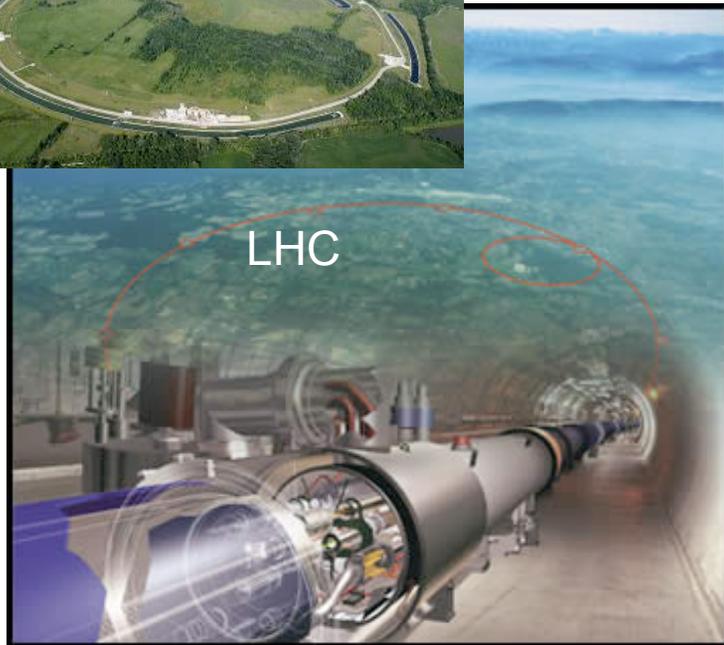
Higgs

New Phenomenon

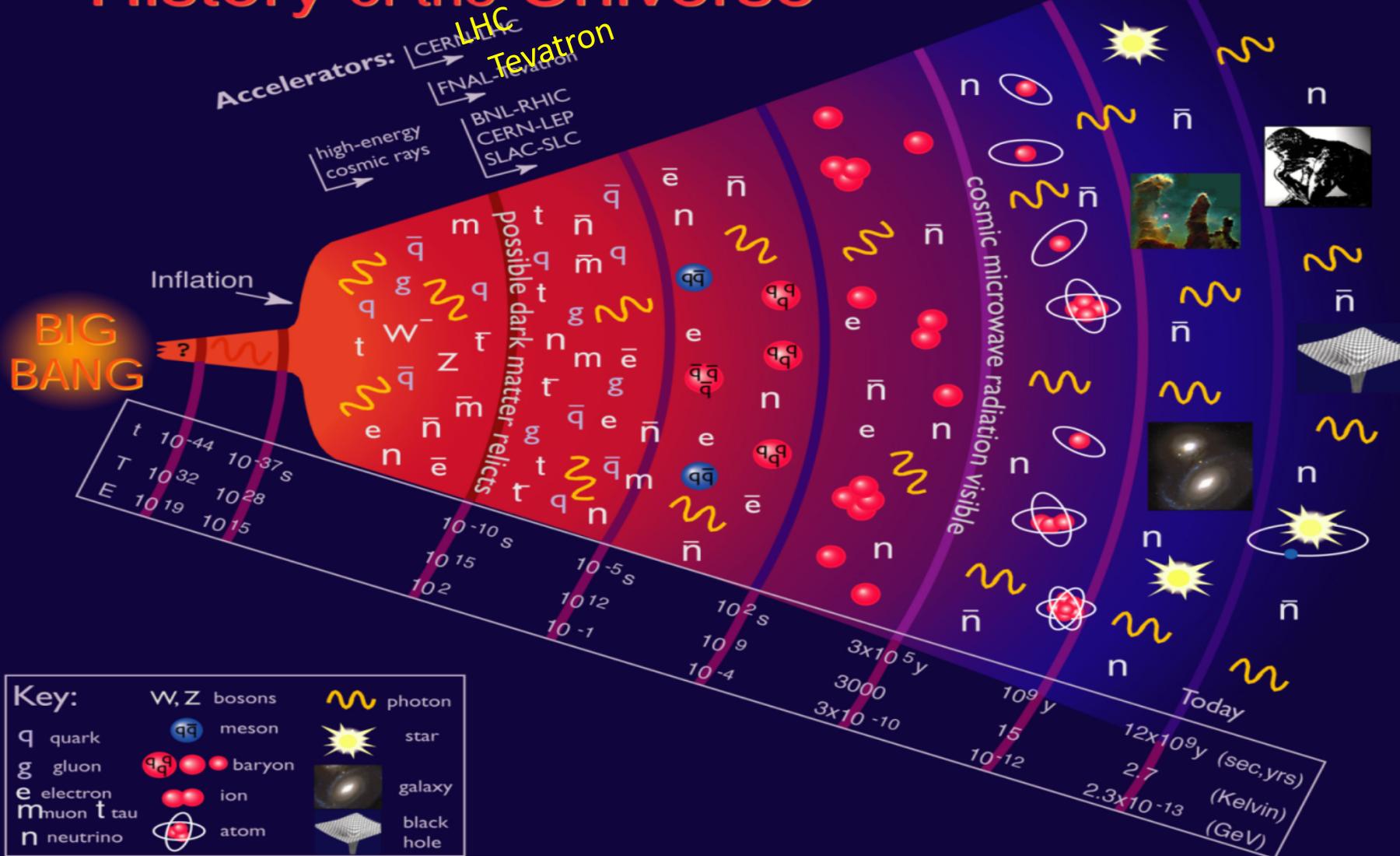
Chicago and Geneva



Theorists and experimentalist have been busy for the last couple of decades



History of the Universe



Particle Data Group, LBNL, © 2000. Supported by DOE and NSF

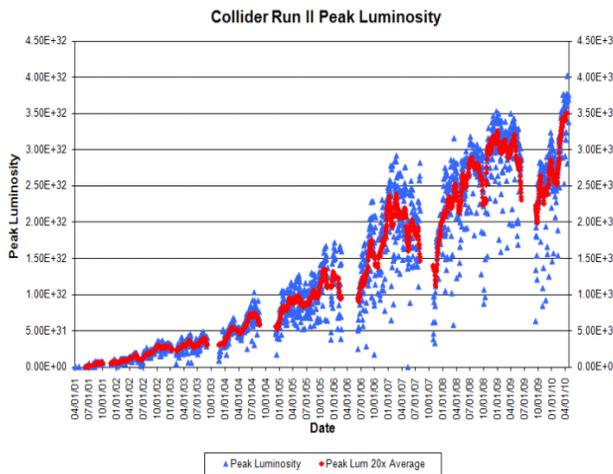
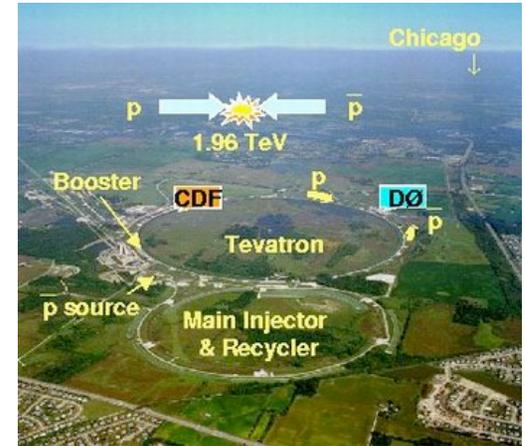
Tevatron

25 years ago, first Tevatron collisions in 1985

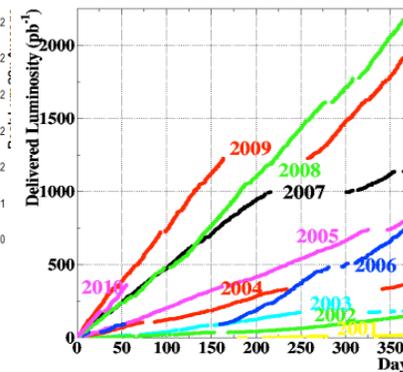
Tevatron expected luminosity $\sim 3 \times 10^{30} \text{ cm}^{-2}\text{s}^{-1}$

Now running at $3 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ almost routinely !

...and this is not the only time when a Tevatron team exceeded its own expectations and projections

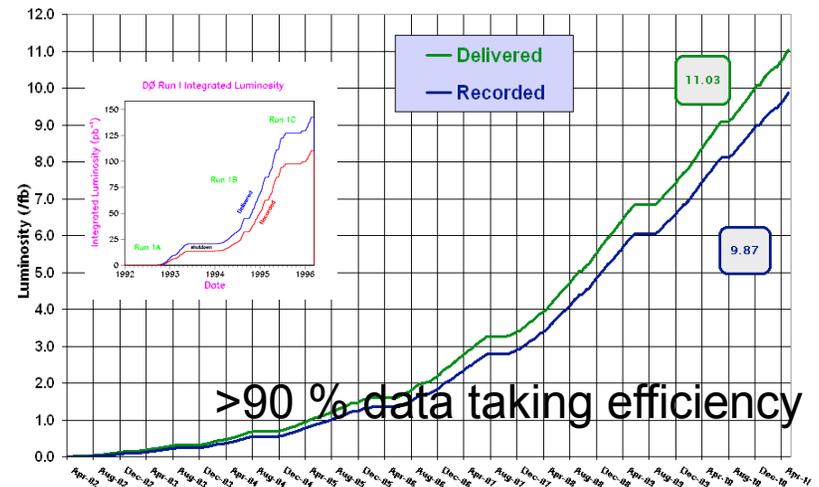


Luminosity Delivered per Calendar Year (CDF Exp)



Run II Integrated Luminosity

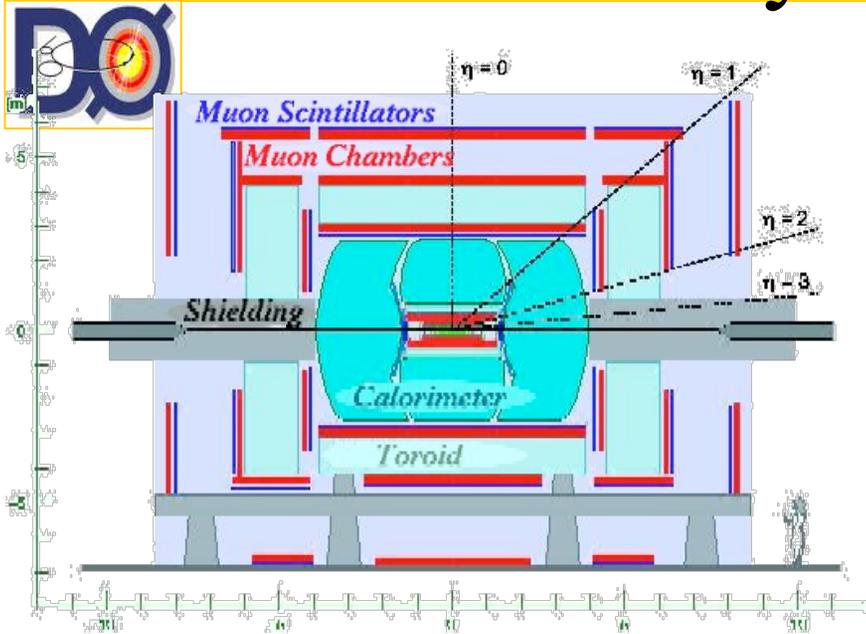
19 April 2002 - 22 May 2011



>90% data taking efficiency

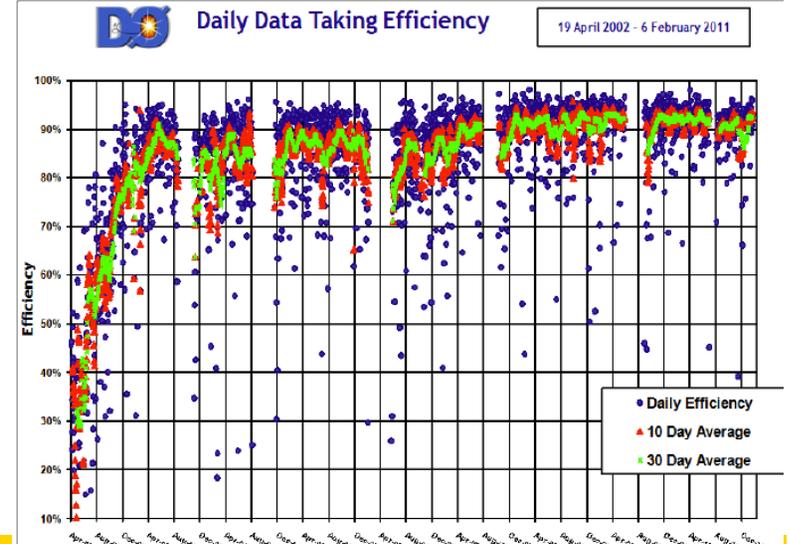
For 25 years, the Tevatron has been the only machine at the frontier... and we have learned much.

Our Eyes - Detectors



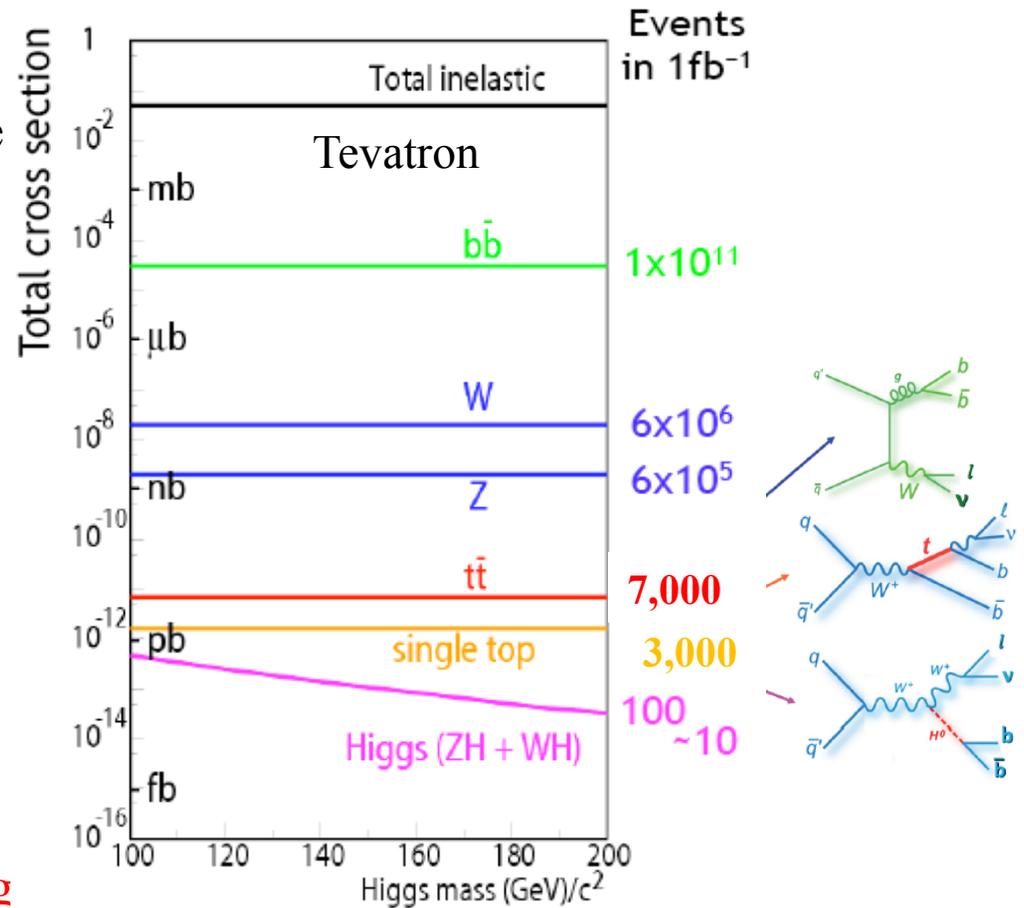
- D0: weighs 5000 tons, is about 12 meters in all three dimensions.
- All purpose detector
 - Good resolution for track momenta, vertex, calorimeter
 - $\sim 90\%$ avg. data taking efficiency

Institutions: 86 total, 37 US, 49 non-US



Production of Fundamental Particles

- **Cross section:**
 - Total inelastic cross section is huge
 - ~60 trillion events in 1 fb^{-1}
 - ~ 2 MHz interaction rate
- **Translate it into rates**
 - bb: 42 kHz
 - Jets with $ET > 40 \text{ GeV}$: 300 Hz
 - W: 3 Hz
 - Top: 2-3 eventst /hour
- **Trigger needs to select the interesting**

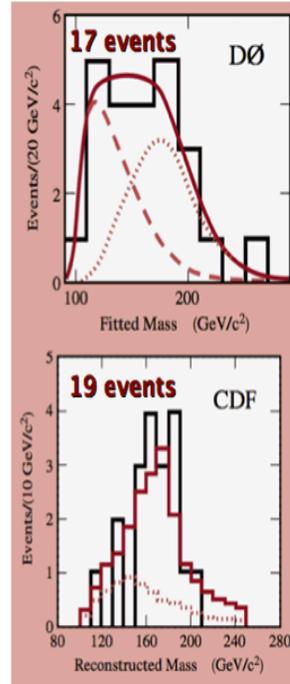


The key is trigger – that is rejecting as much as we can while keeping as many interesting events as possible on tape

Why Look at The Top Quark?

- Was discovered at Fermilab in 1995
- The heaviest known fundamental particle
 - $m_t = 173.3 \pm 1.1 \text{ GeV}$ (<1% precision)
 - Close to a gold atom
 - $\tau = 5 \times 10^{-25} \text{ s} \ll \Lambda_{\text{QCD}}^{-1}$
 - Decays before hadronization
- Mass close to scale of electroweak symmetry breaking
 - Only quark for which coupling to Higgs is significant
 - May shed light on EWSB mechanism
- Top quark plays special role in many of the new physics models

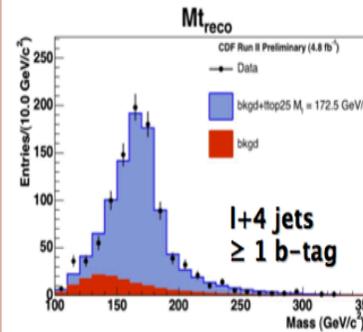
discovery PRL 74, 2632 (1995)
PRL 74, 2626 (1995)



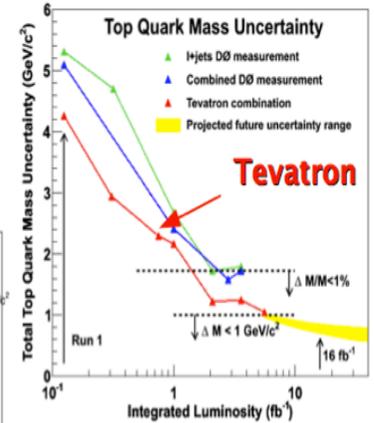
1995, CDF and DØ experiments, Fermilab

today

~1000 events



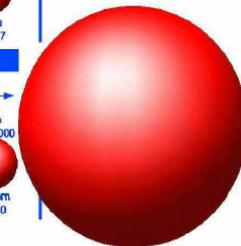
precision



searches

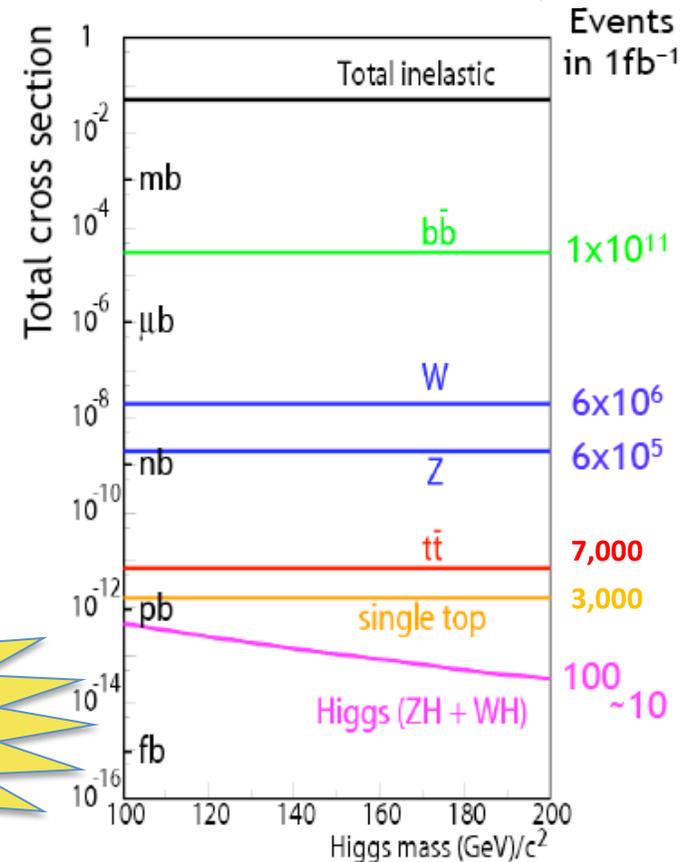
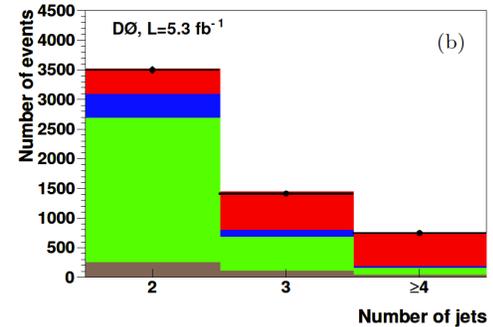


LEPTONS		
Electron Neutrino Mass ~0	Muon Neutrino ~0	Tau Neutrino ~0
Electron .511	Muon 106.7	Tau 1.777
QUARKS		
Up Mass: 5	Charm 1.500	Top ~180,000
Down 8	Strange 160	Bottom 4.250



Why Keep Looking at the Top?

- Even more than a decade after its discovery, our sample consists of ~ 1000 top quark events
 - Many of the measurements of top quark properties are still statistics limited



Lot of room for surprises!

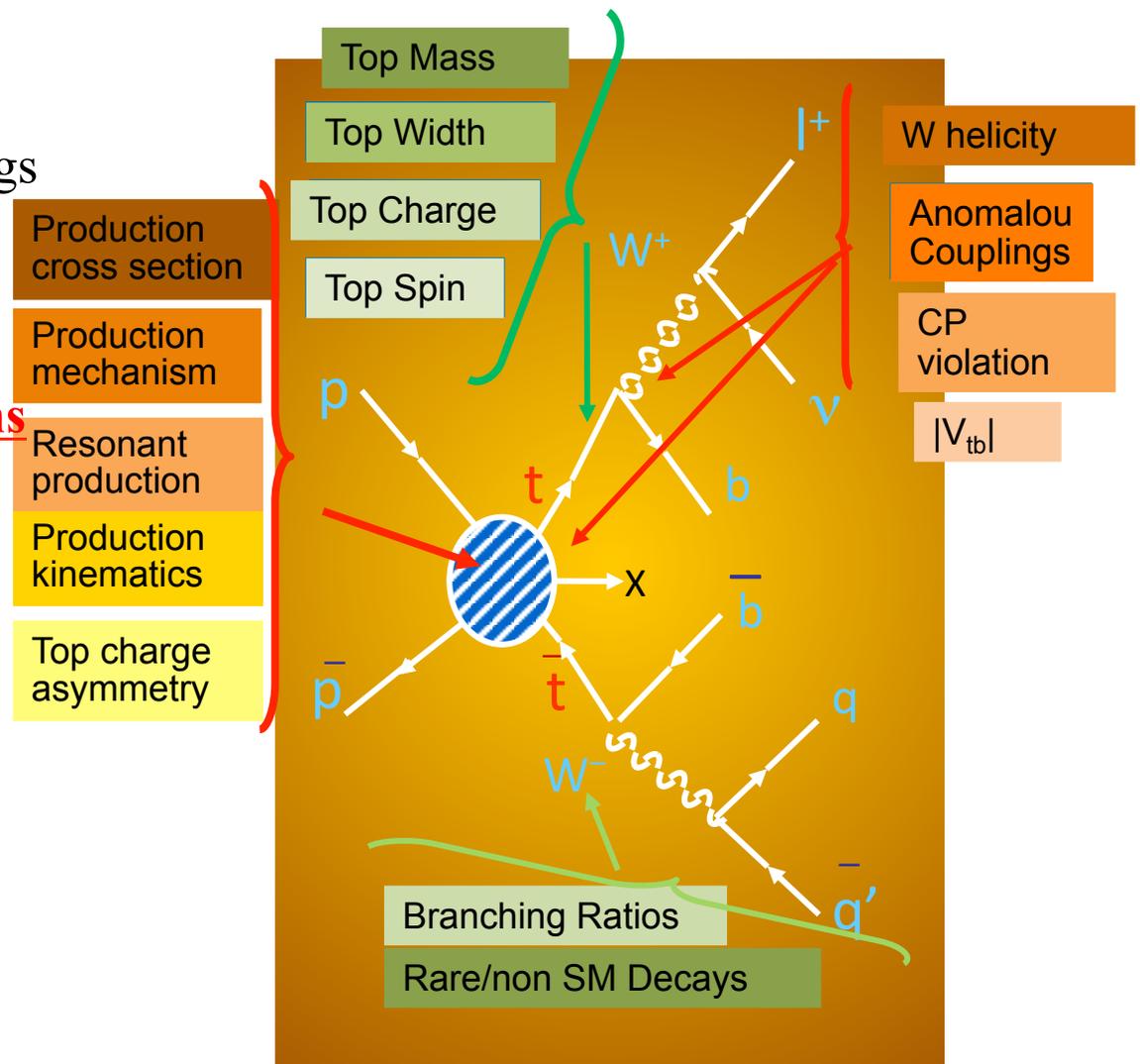
Are recent excess hint of something?

Why we Love to Talk About Top?

- Top quark is the heaviest known elementary particle
- Strongest coupling with the Higgs boson

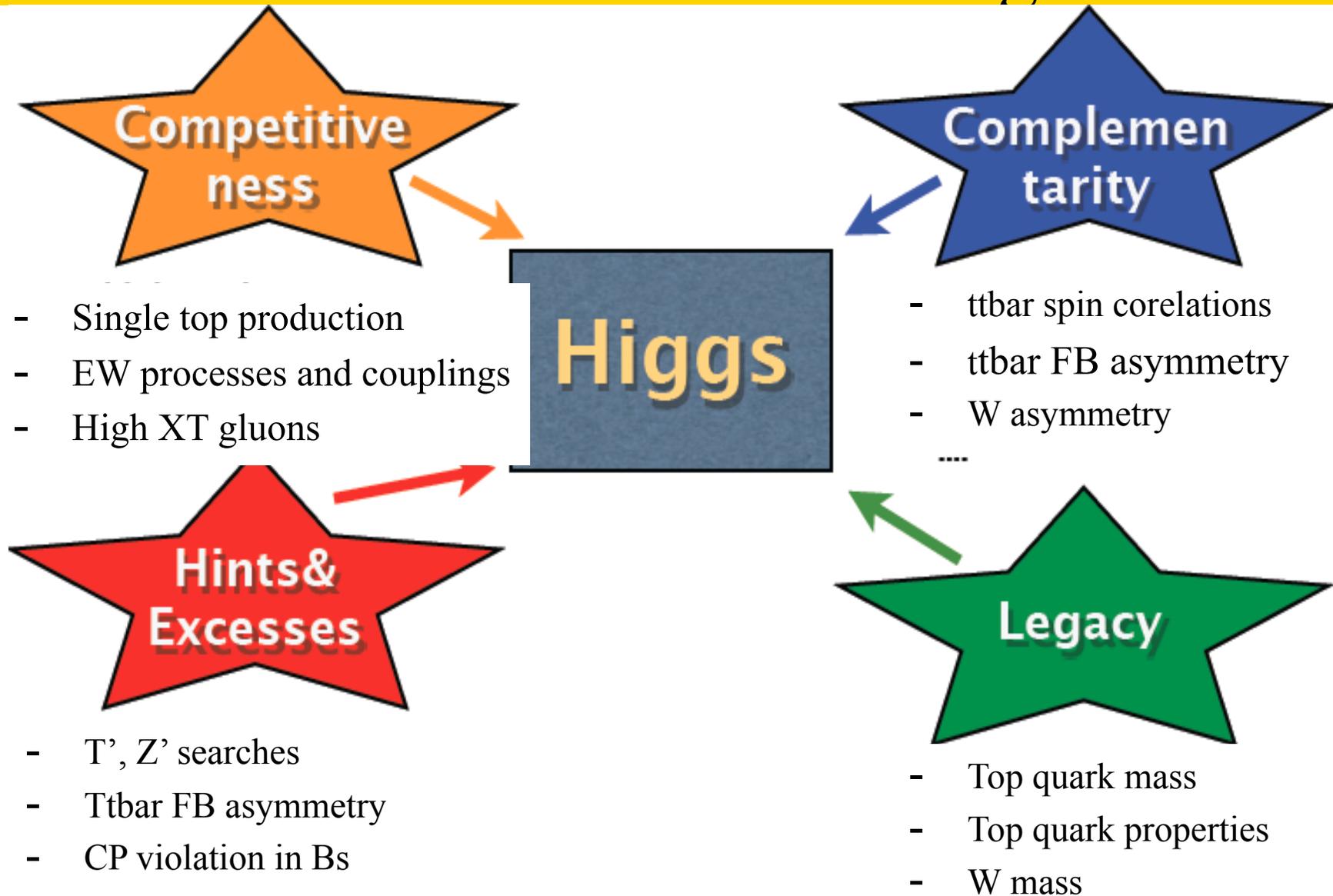
Can help answer many questions

- Higgs boson mass?
- More than three fermion generations?
- Charged Higgs bosons?
- New massive particles?
- Do all quarks have the expected couplings?
- Unknown unknowns??



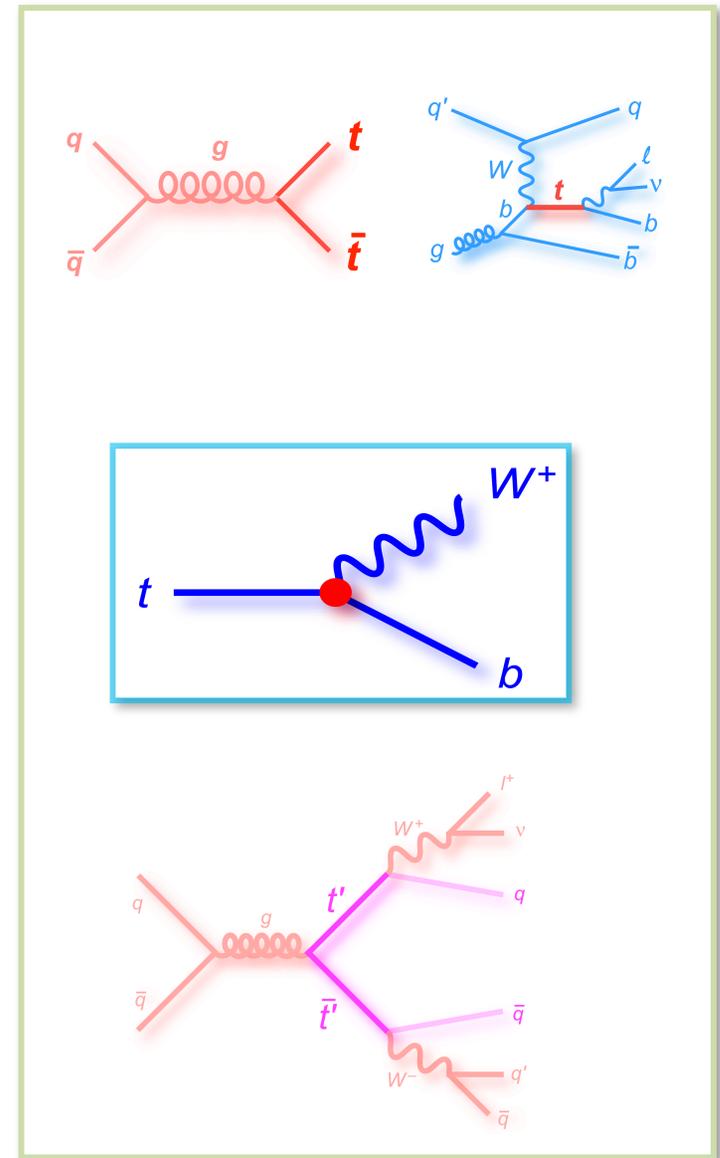
Simply put: top quark sector is one of the best places to look for new physics

Tevatron's Research Program



Things I will Talk About Today

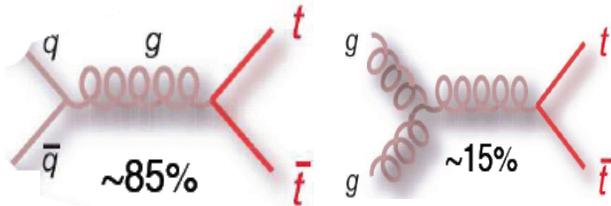
- **New physics in properties**
 - Cross section
 - Mass
 - Width
 - Spin
 - Forward backward asymmetry
- **New physics in couplings**
 - Wtb couplings
 - W helicity
- **New Physics in the form of new particles**
 - $t\bar{t}$ resonances
 - 4th generation? (looking for t')
 - Color flow



Top Quark Production at Tevatron

Top quark pair production

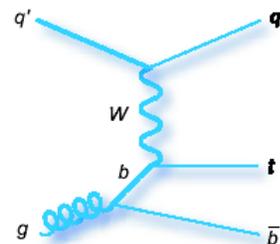
$$\sigma_{tt} \sim 7.5 \text{ pb}$$



Single Top quark production

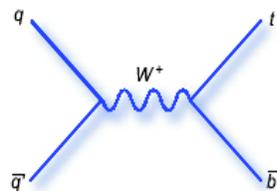
t-channel

$$\sigma \sim 2 \text{ pb}$$



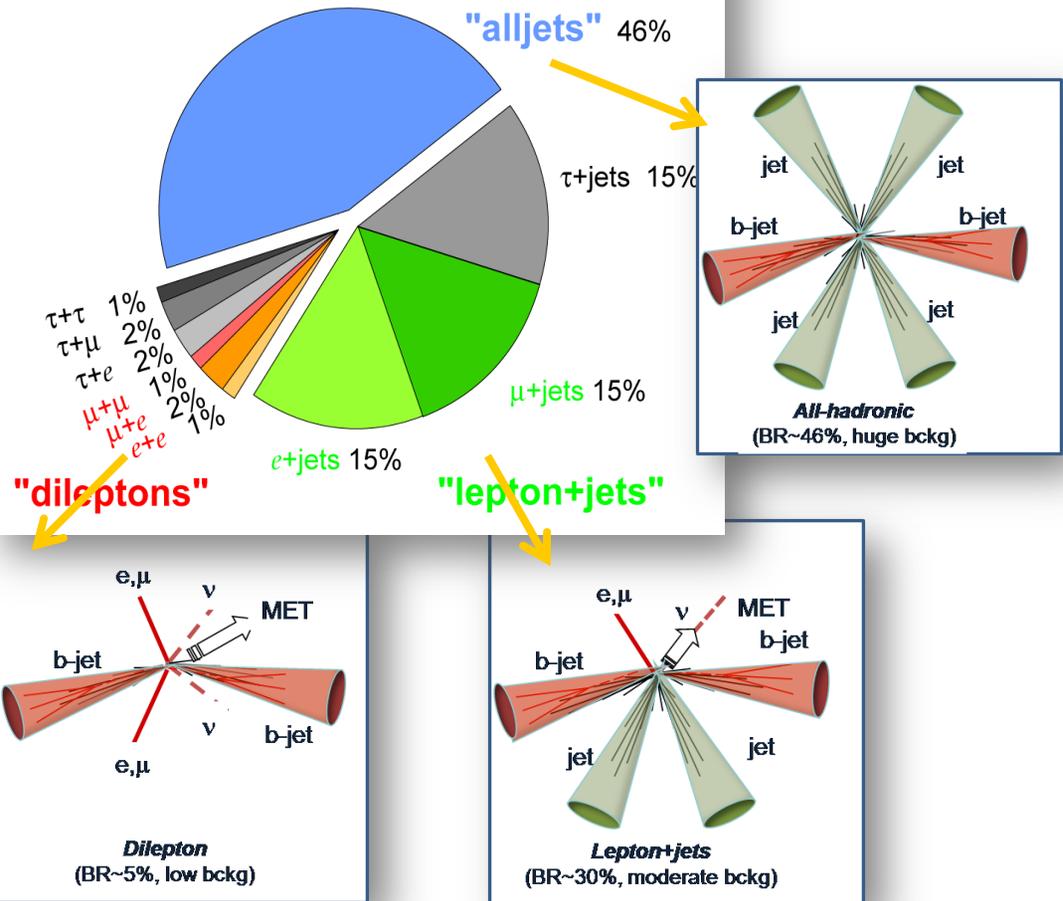
s-channel

$$\sigma \sim 1 \text{ pb}$$



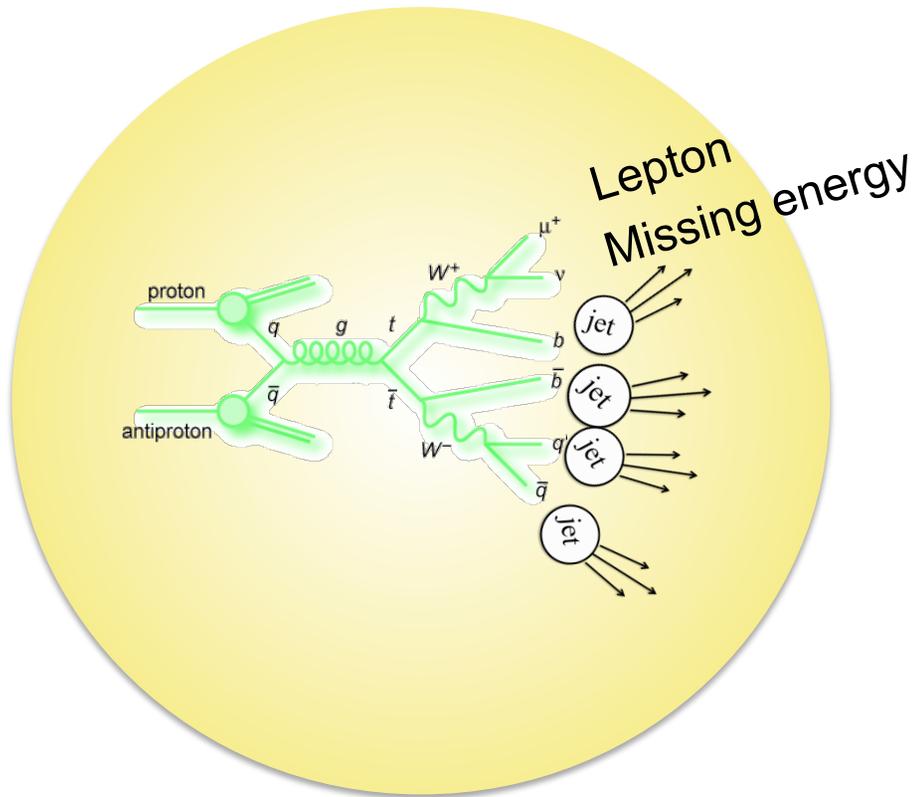
Within Standard Model $t \rightarrow Wb \sim 100\%$

Top Pair Branching Fractions

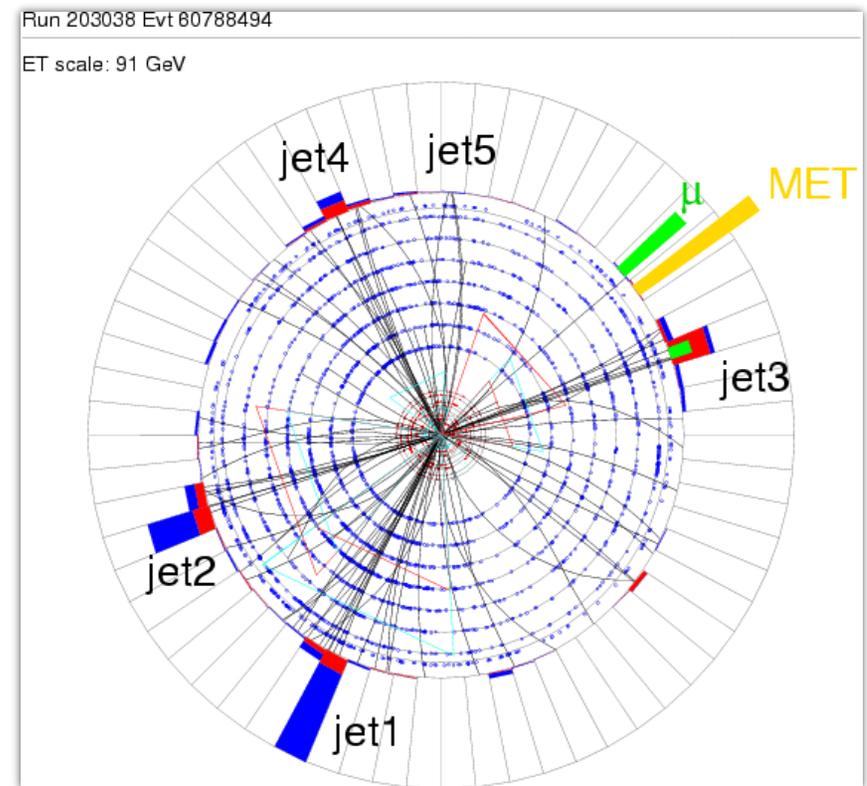


What our "Eyes" See

Theory world

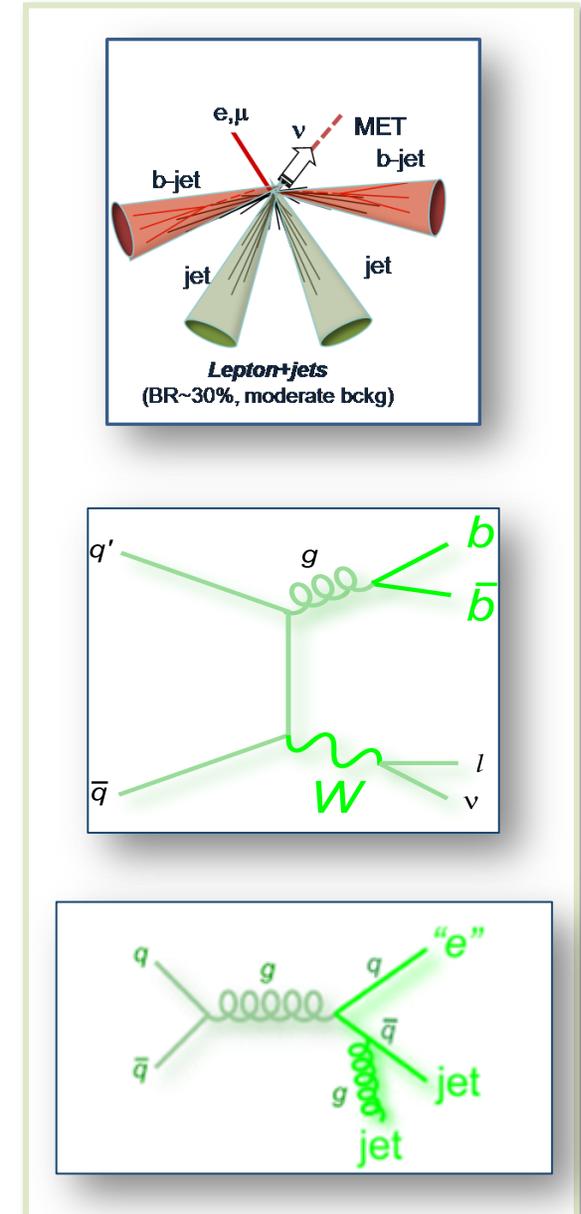


Dectector world

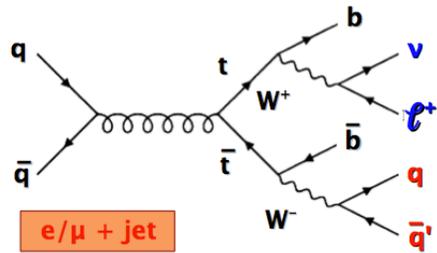


Background

- Dominant Backgrounds
 - Dominant backgrounds arise from W +jets and multijet production (ℓ +jets channel) and Z +jets WW +jets (dilepton channel)
 - When searching for new physics in top sector, SM top quark production itself becomes the dominant background
- Signal and Background Modeling
 - The SM top pair samples are generated with ALPGEN for the matrix elements and parton showers followed by PYTHIA for the hadronization
 - Single top quarks production is modeled using SINGLETOP based on COMPHEP
 - Other backgrounds are also modeled using ALPGEN or PYTHIA except multijet background which is determined from data



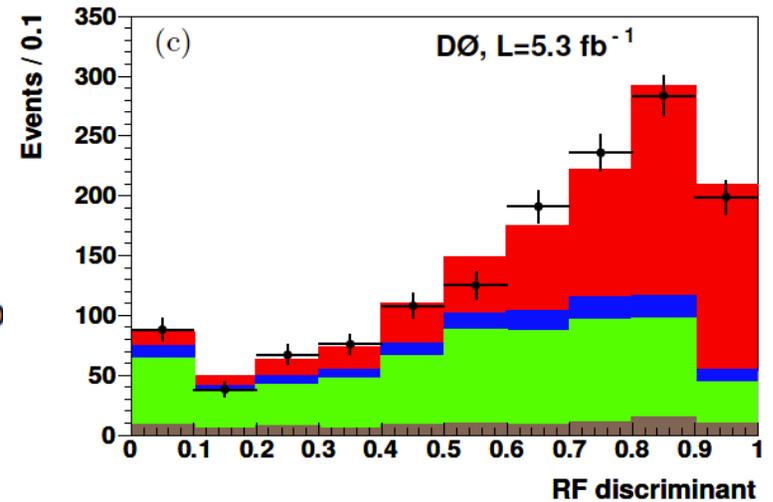
Top Pair Cross Section



$$\sigma_{t\bar{t}} = \frac{N_{data} - N_{bck}}{\epsilon L A}$$

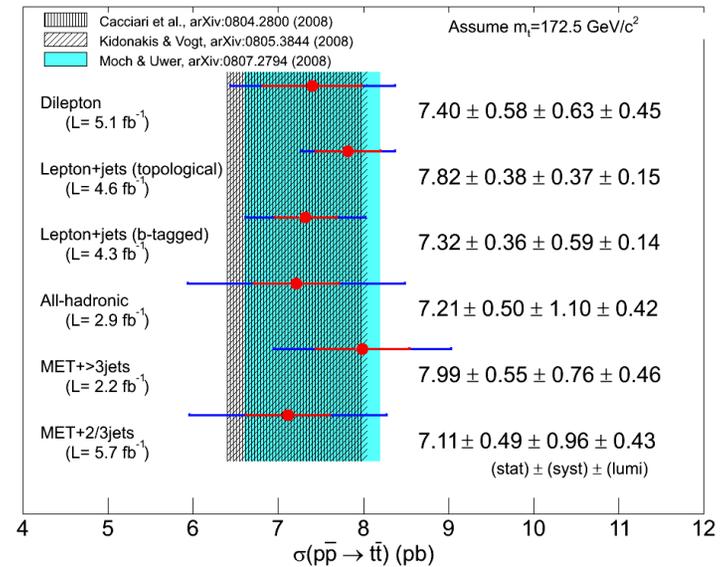
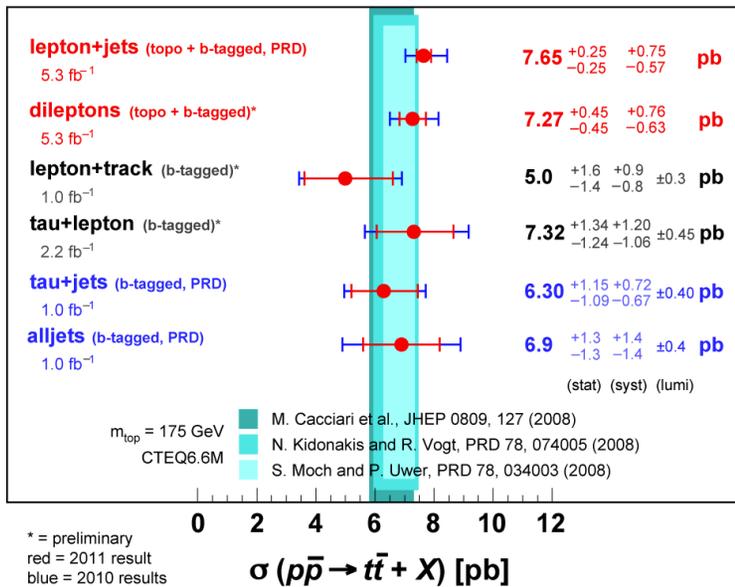
$$\sigma_{t\bar{t}} = 7.78^{+0.77}_{-0.64} (\text{stat} + \text{syst} + \text{lumi}) \text{ p}$$

With 5.3 fb⁻¹, for a mass of 172.5 GeV



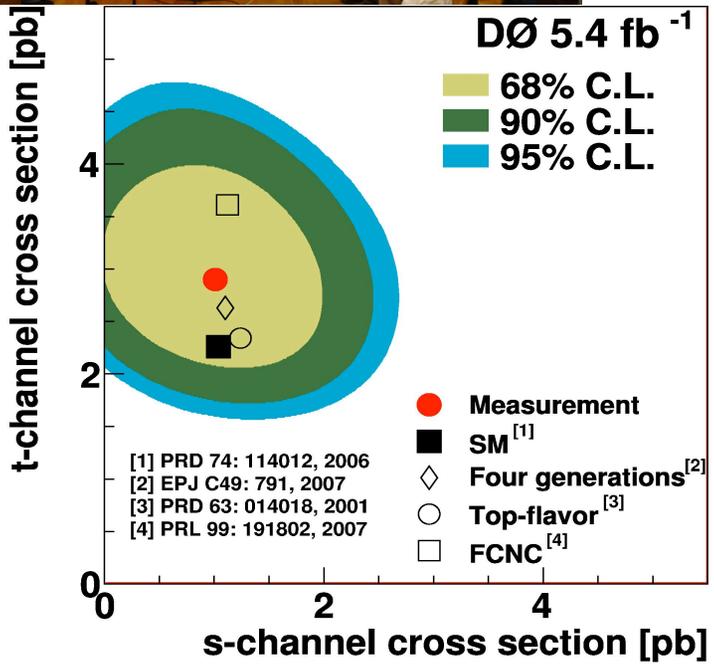
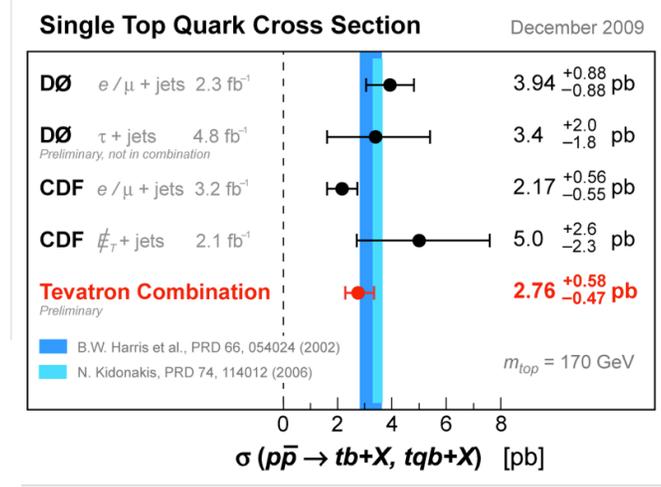
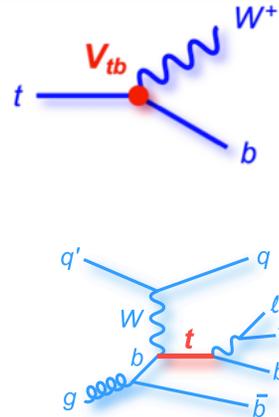
arXiv.org:1101.0124
DØ Run II

March 2011

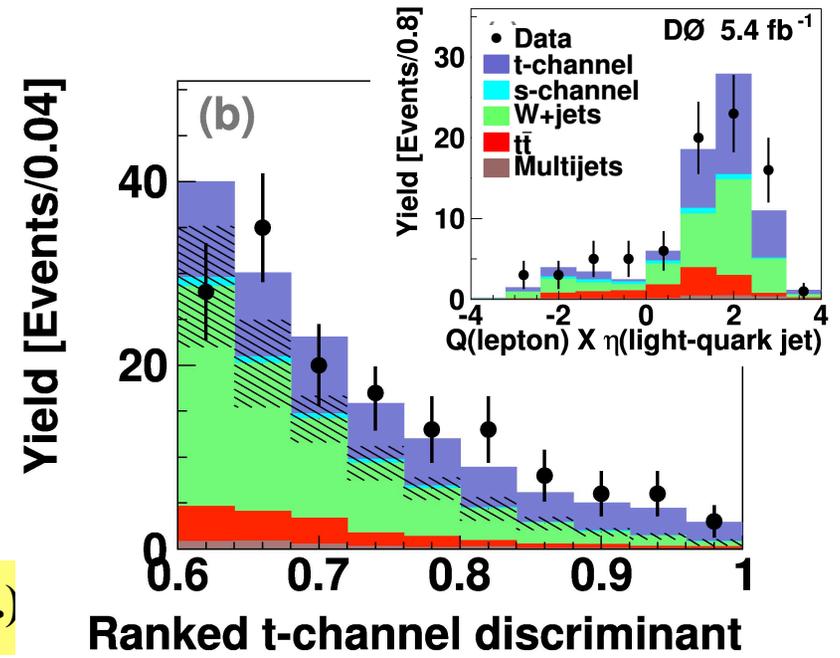


Single Top Cross section

2009

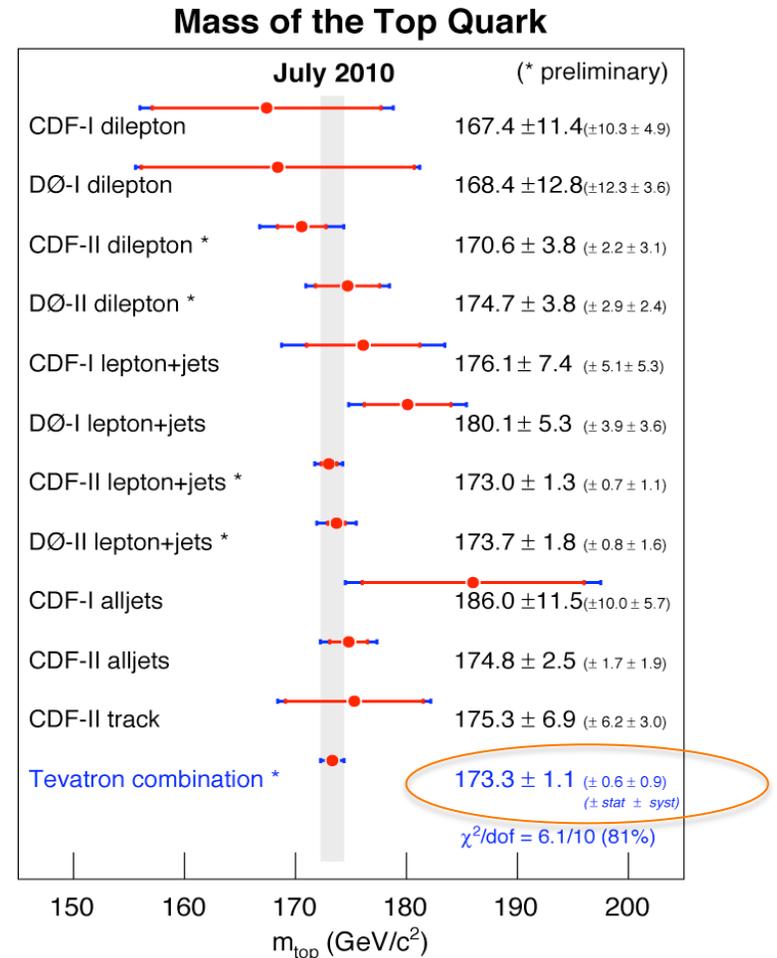
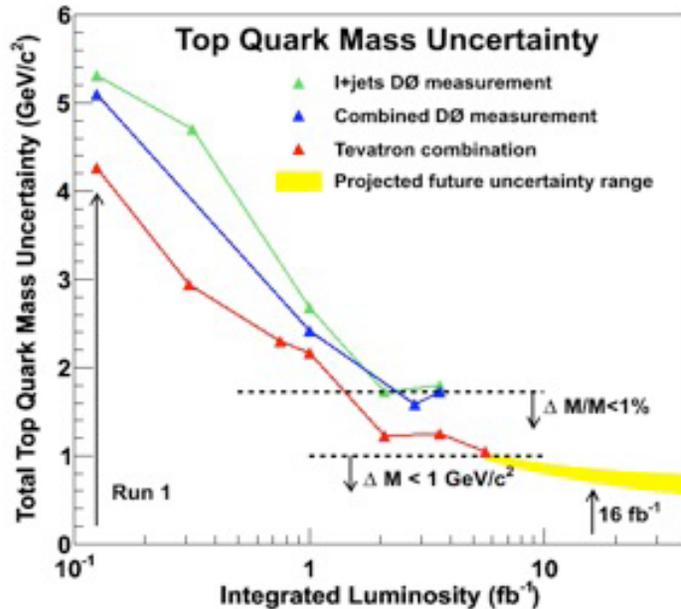


$\sigma_{tqb} = 2.90 \pm 0.59 \text{ pb (5.5 std. dev.)}$



Top Quark Mass

- Top quark mass is measured directly
 - in different channels
- Dilepton, lepton+jets, all jets channels
- using a variety of techniques by both CDF and DØ
- Both experiments are in agreement



Measured top mass = $173.3 \pm 1.1 \text{ GeV}$

We have long exceeded the Tevatron goal of $\delta M = 2 \text{ GeV}$

Top Quark Mass

$$\mathcal{L} = \dots - \bar{\psi} M \psi \left(1 + \frac{H}{v}\right) \dots$$

- **LO QCD: free parameter**
- **NLO QCD: dependent on the renormalisation scale M**

"Bare" parameters of QCD:
 $g_s, m_u, m_d, m_s, m_c, m_b, m_t$

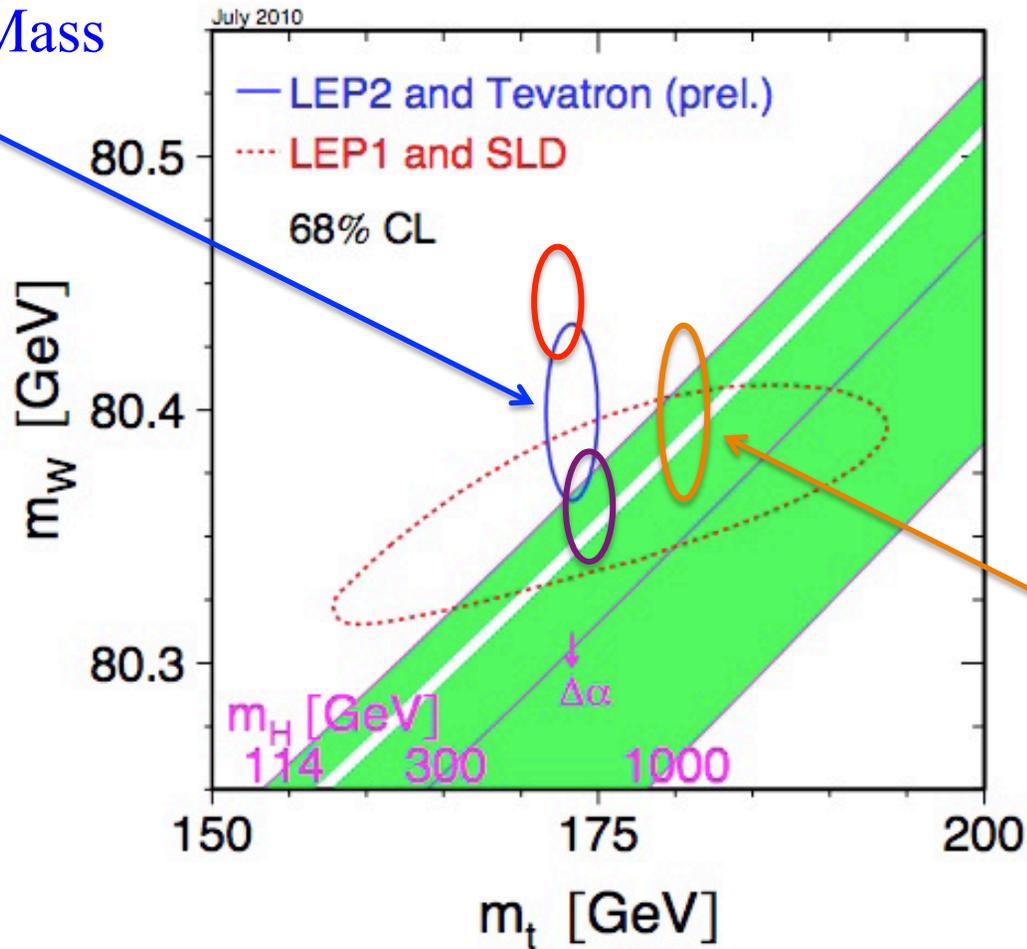
Renormalised parameters of QCD:
 $g_s(M), m_u(M), m_d(M), m_s(M), m_c(M), m_b(M), m_t(M)$

the concept of quark mass is convention-dependent!

There are theoretical arguments that our measured mass from MC is closer to the pole mass within 1GeV. But how close?

SM Self Consistency

Pole Mass



With Tevatron 10 fb^{-1} :

W mass uncertainty = 15 MeV

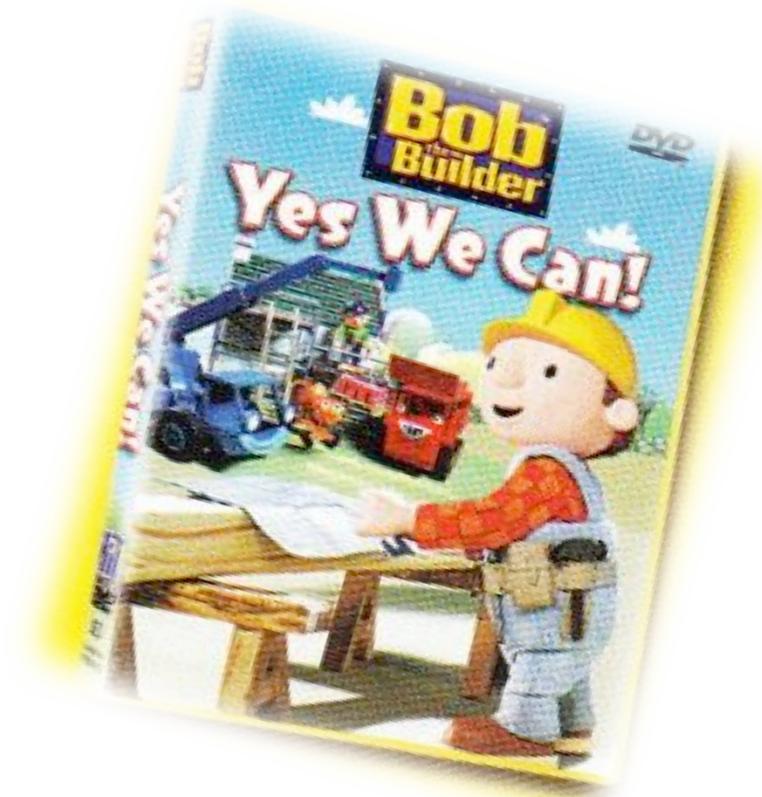
Top mass uncertainty = 1 GeV

World average
interpreted as
MS mass

The top mass depends on M_H through loop diagrams ($M_t \sim \log M_H$).

Can we do Anything about it?

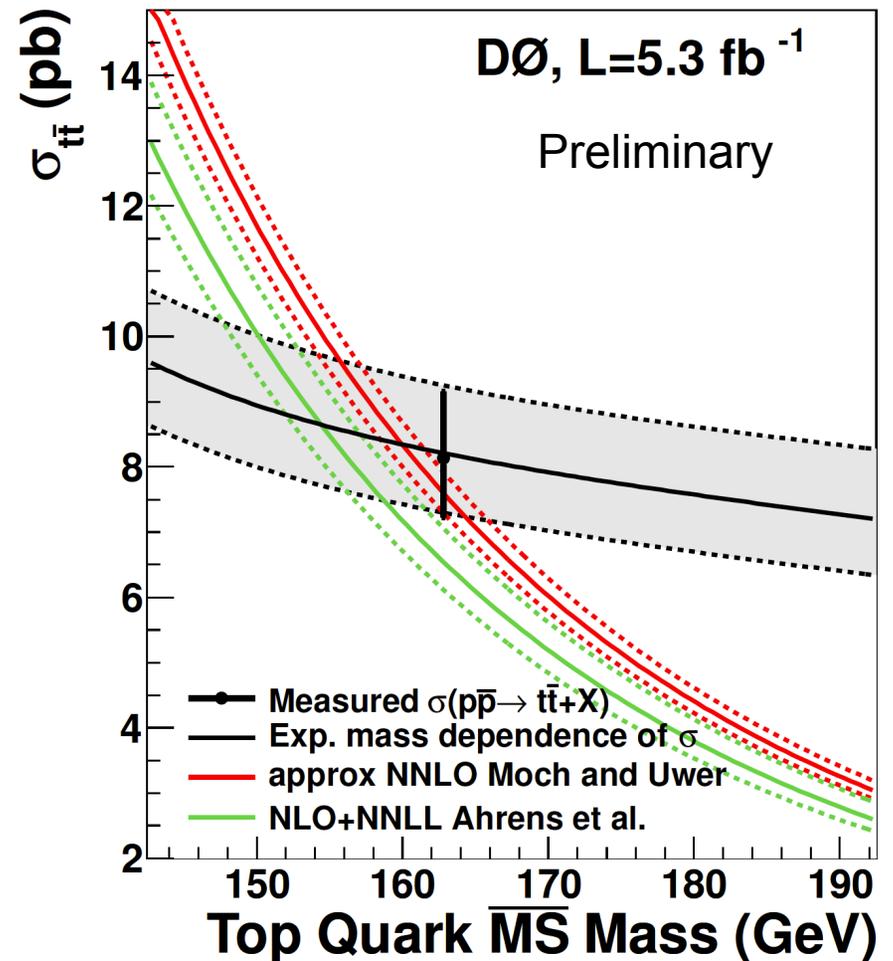
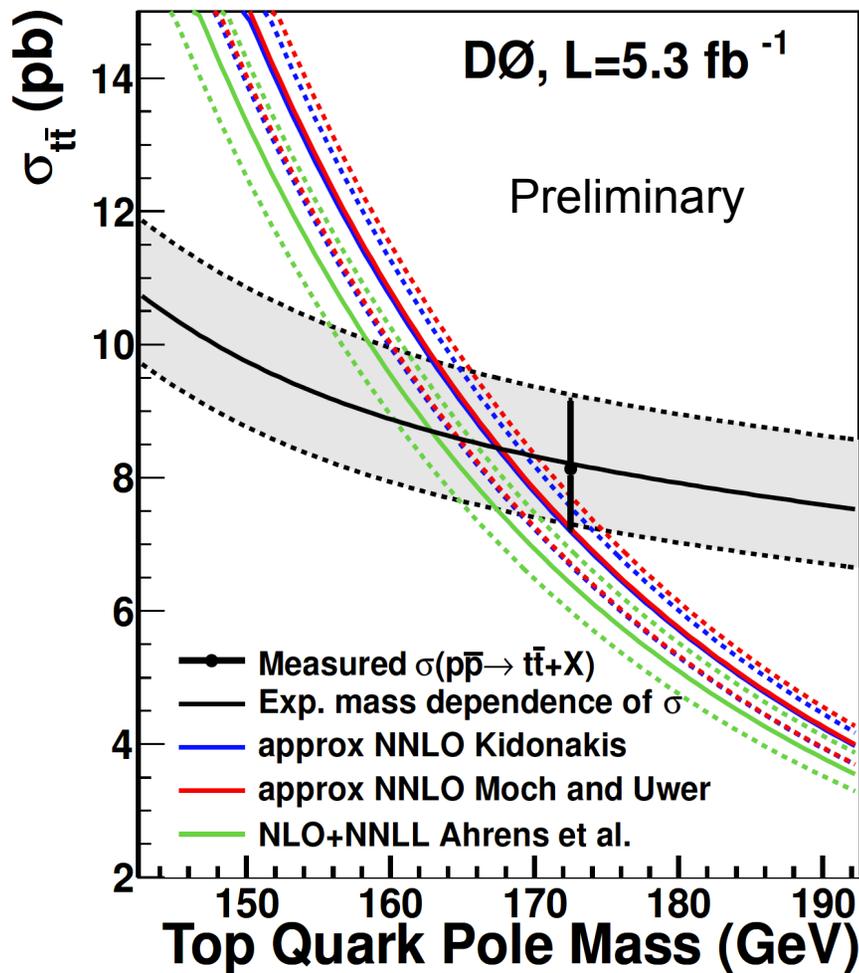
Yes we can!



No! it's not Obama....

Top Quark Mass from Cross Section

Compare the experimental value for cross-section as function of top mass with theoretical calculations in pole and $\overline{\text{MS}}$ schemes



Top Quark Mass from Cross Section

- We extract the most probable top quark mass values in pole and MS-bar schemes and corresponding 68% CL bands

Theoretical Calculation	Measured Mass	
	Pole mass	MS-bar mass
NLO+NNLL	163.0+5.4 -4.9	154.4+5.2-4.5
Approx. NNLO	167.5+5.4-4.9	159.9+5.1-4.4

NNLO approx Moch and Uwer
NLO+NNLL Ahrens et al.

Directly measured top quark mass = 173.3 ± 1.1 GeV

- For the first time the top quark MS-bar mass is extracted taking the mass dependence of the measured top-antitop cross section correctly into account

Top Quark Width

SM predicts ~ 1.5 GeV ($M_t = 175$ GeV)



CDF Template based top width measurement

- Upper limit placed on top width

$$0.4 \text{ GeV} < \Gamma_{\text{top}} < 4.4 \text{ GeV} @ 68\% \text{ CL}$$

$$\Gamma_{\text{top}} < 7.5 \text{ GeV} @ 95\% \text{ CL}$$



- Use t-channel single top quark production and top decay branching ratio measurements

$$\sigma(t\text{-channel}) \mathcal{B}(t \rightarrow Wb) = 3.14_{-0.80}^{+0.94} \text{ pb}$$

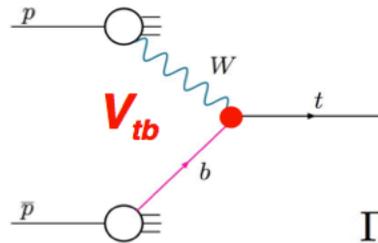
$$\mathcal{B}(t \rightarrow Wb) = 0.962_{-0.066}^{+0.068}(\text{stat}) \quad {}_{-0.052}^{+0.064}(\text{syst})$$

$$\Gamma(t \rightarrow Wb) = \sigma(t\text{-channel}) \frac{\Gamma(t \rightarrow Wb)_{\text{SM}}}{\sigma(t\text{-channel})_{\text{SM}}}$$

t-channel cross section:

$$\sigma(t\text{-channel}) = 2.14 \pm 0.18 \text{ pb}$$

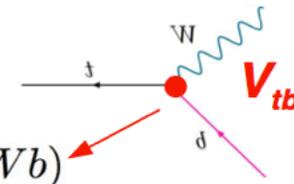
NLO, $m_t = 170$ GeV



partial decay width:

$$\Gamma(t \rightarrow Wb) = 1.26 \text{ GeV}$$

NLO, $m_t = 170$ GeV



$$\Gamma_t = \frac{\Gamma(t \rightarrow Wb)}{\mathcal{B}(t \rightarrow Wb)}$$

$\bar{t}\bar{t}$ production

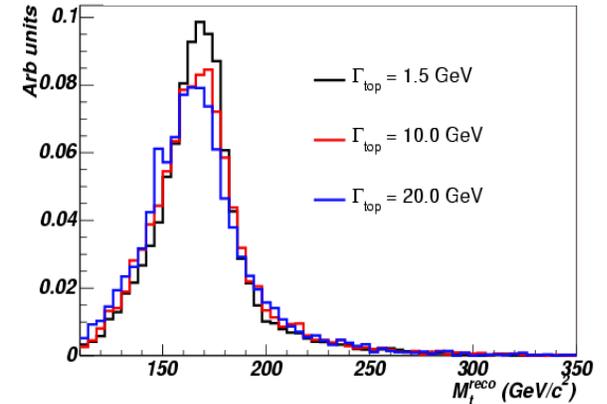
assume that coupling in top production and decay is the same

$$\Gamma_t = 1.99_{-0.55}^{+0.69} \text{ GeV}$$

$$\tau_t = (3.2_{-0.9}^{+1.3}) \times 10^{-25} \text{ s}$$

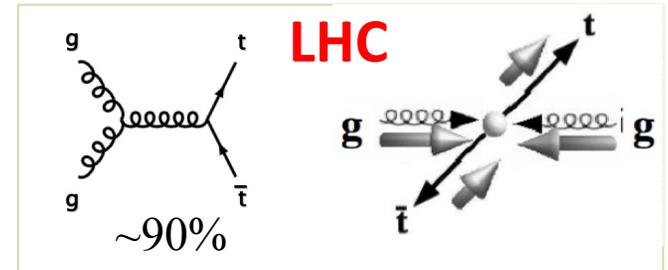
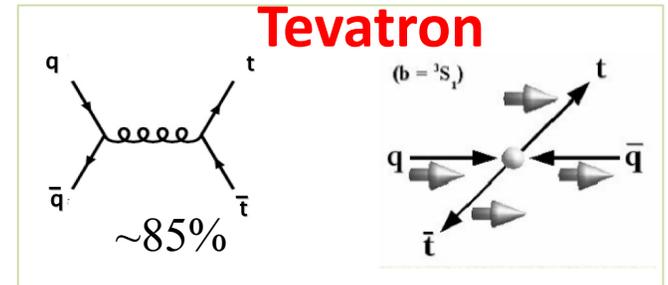
\Rightarrow most precise determination

Lepton+Jets with 4.3fb^{-1}



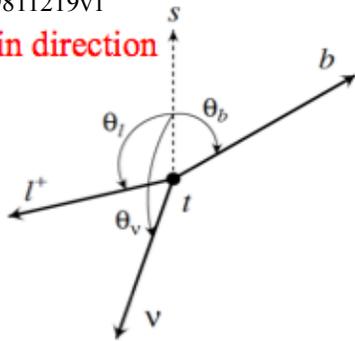
Spin Correlation in $t\bar{t}$ Events

- In top pair production at hadron colliders, their spins are expected to be correlated
- Observation of spin correlation will place upper limit on top quark life time
- Scenarios beyond the standard model predict changes in production and decay dynamics to change effect of spin correlation
- Complementary to LHC



arXiv:hep-ph/9811219v1

Spin direction



Decay product	Correl Coeff.
b	-0.40
$\nu_\ell, u, \text{ or } c$	-0.33
$\bar{\ell}, \bar{d}, \text{ or } \bar{s}$	1.00

- Maximum correlation for charged lepton or down type quark
 - Use dilepton decay channel
- Choosing the beam momentum vector as the quantization axis

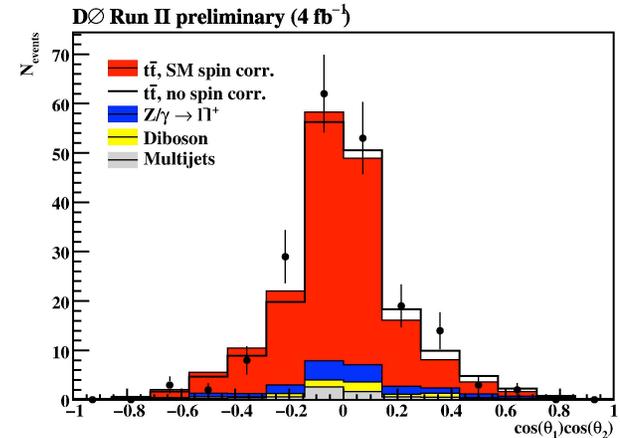
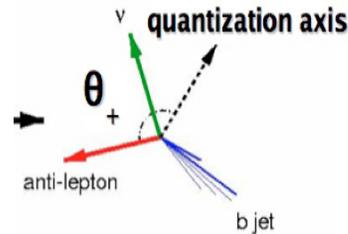
The NLO QCD prediction

$$C = 0.777 + 0.027 - 0.042$$

Measuring Spin Correlations

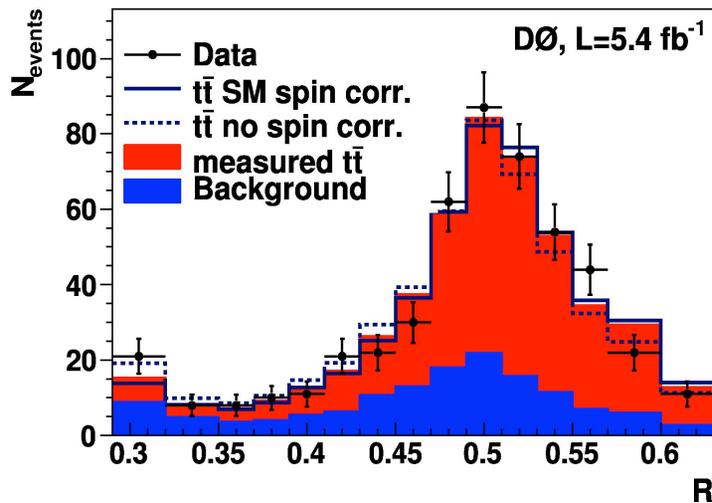
- Using templates

$$C = \frac{N(\uparrow\uparrow) + N(\downarrow\downarrow) - N(\uparrow\downarrow) - N(\downarrow\uparrow)}{N(\uparrow\uparrow) + N(\downarrow\downarrow) + N(\uparrow\downarrow) + N(\downarrow\uparrow)}$$



$$C = 0.10^{+0.45}_{-0.45} \text{ (stat+syst)}$$

- Using matrix element spin of the top



$$R = \frac{P_{\text{sgn}}(H = c)}{P_{\text{sgn}}(H = u) + P_{\text{sgn}}(H = c)}$$

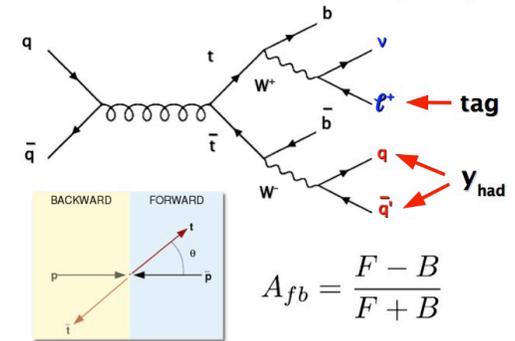
Exclude the hypothesis that the spins of the t \bar{t} are uncorrelated at the 97.7% C.L.

A_{fb} in Top Quark Events

- SM predicts no asymmetry in LO in QCD – NLO prediction is $2 \pm 1\%$

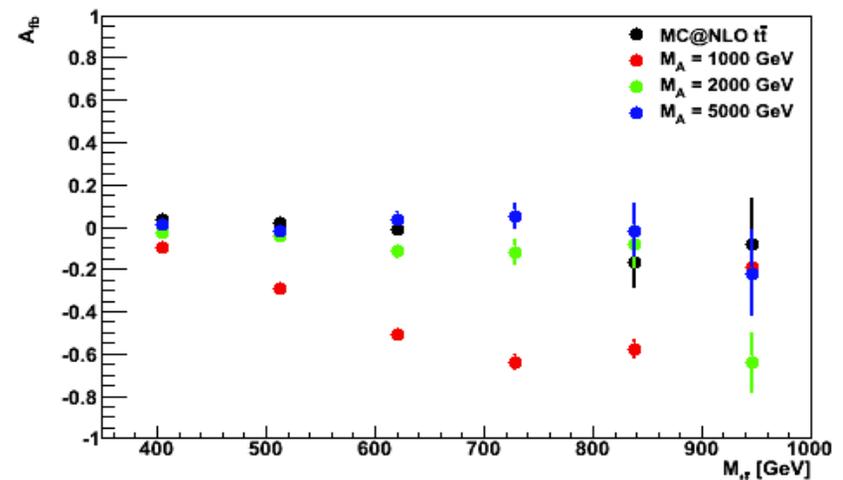
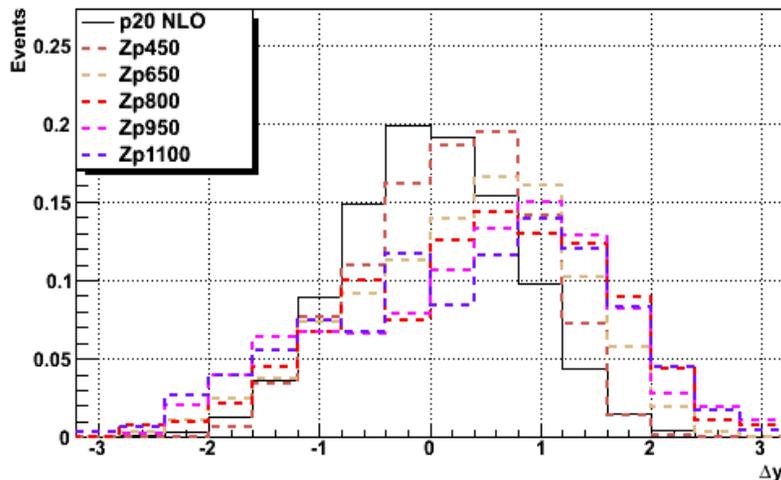
$$A_{fb} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$$

- Large measured asymmetry would indicate new physics



The asymmetry gives us a window into many types of potential new physics: $Z' \rightarrow t\bar{t}$, Axiguons and extra dimensions.

For Axiguons, can potentially get a limit of 2 TeV or more.



The Tevatron A_{fb} measurements are complimentary to the LHC

A_{fb} in Top Quark Events



arXiv:1101.0034v1 [hep-ex]

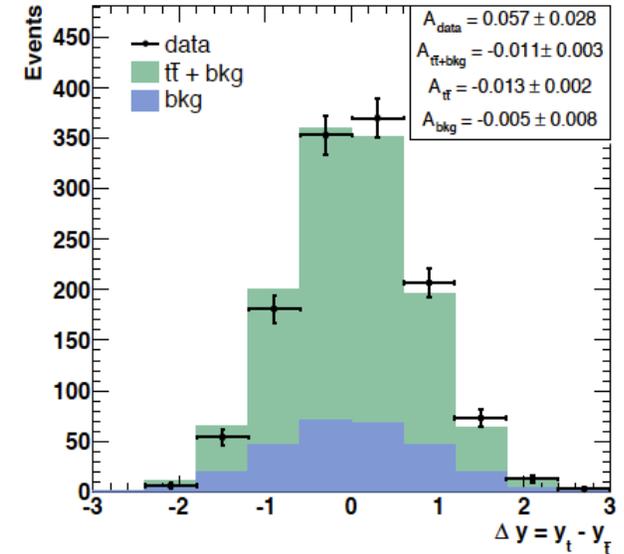
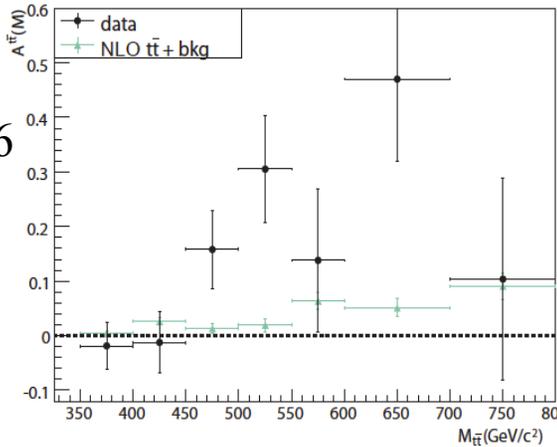
MCFM predictions of 0.039 ± 0.006

$$A_{fb}^{t\bar{t}}(|\Delta y| < 1.0) = 0.026 \pm 0.118$$

$$A_{fb}^{t\bar{t}}(|\Delta y| \geq 1.0) = 0.611 \pm 0.256$$

$$A_{fb}^{t\bar{t}}(M_{t\bar{t}} < 450 \text{ GeV}/c^2) = -0.116 \pm 0.153$$

$$A_{fb}^{t\bar{t}}(M_{t\bar{t}} \geq 450 \text{ GeV}/c^2) = 0.475 \pm 0.114$$

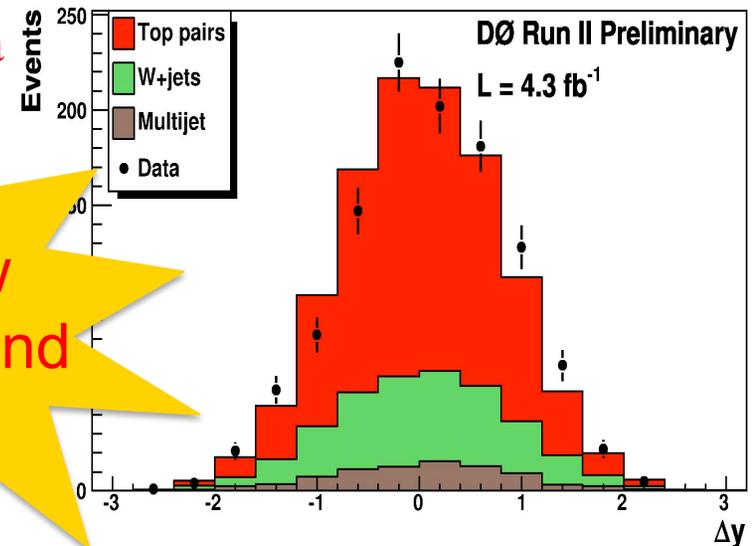


current preliminary result:

$A_{fb} = 8 \pm 4(\text{stat}) \pm 1(\text{syst})\%$ for 4.3 fb^{-1} of data

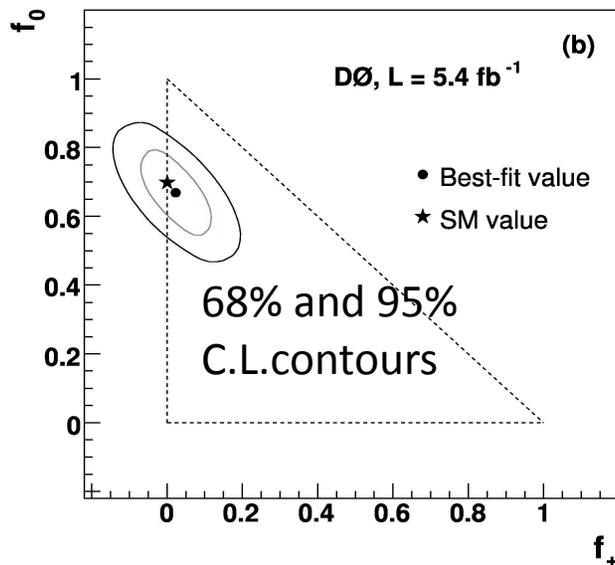
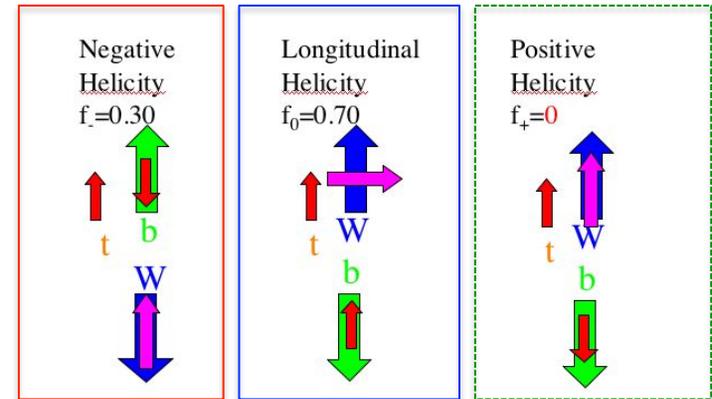
Disagreement between top pair p_T for data and simulation

Hint of new physics beyond SM?

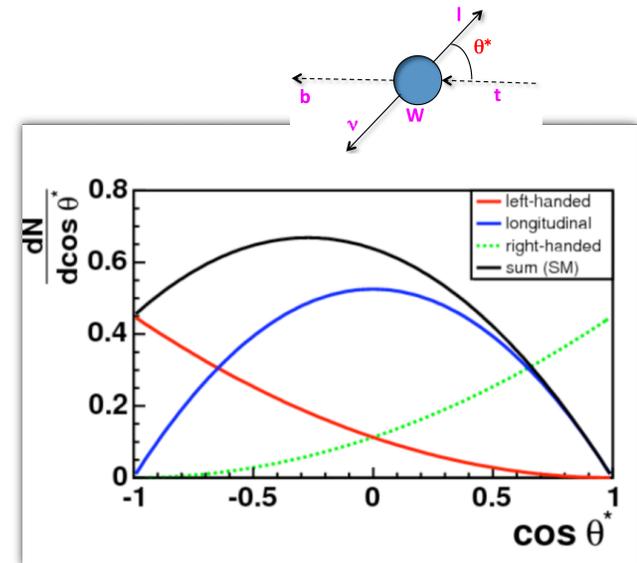


W Boson Helicity

- Model-independent measurement of the W boson helicity from $t \rightarrow Wb$ decays in top pair production
- In the SM, the top quark decays via the $V - A$ charged-current interaction, almost always to a W boson and a b quark



The most precise such measurement



$$f_0 = 0.490 \pm 0.106 \text{ (stat.)} \pm 0.085 \text{ (syst.)}$$

$$f_+ = 0.110 \pm 0.059 \text{ (stat.)} \pm 0.052 \text{ (syst.)}$$

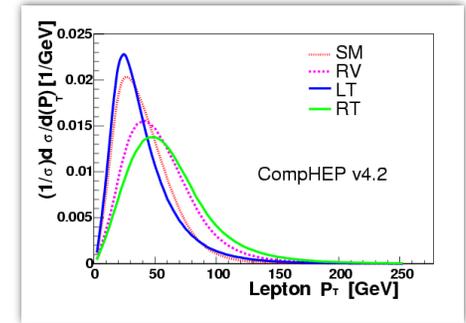
W Helicity and Anomalous Couplings

- General Analysis of Single Top Production and W Helicity in Top Decay

Ren, Larios, and C. P. Yuan (PLB 631, 126 (2005))

$$L_{tWb} = \frac{g}{\sqrt{2}} W_{\mu}^{-} \bar{b} \gamma^{\mu} (f_1^L P_L + f_1^R P_R) t - \frac{g}{\sqrt{2} M_W} \partial_{\nu} W_{\mu}^{-} \bar{b} \sigma^{\mu\nu} (f_2^L P_L + f_2^R P_R) t + h.c.$$

where, in the SM $f_1^L \approx 1, f_2^L = f_1^R = f_2^R = 0$



- Combine W helicity measurement in top pair decays (PRL 100, 062004 (2008))

with

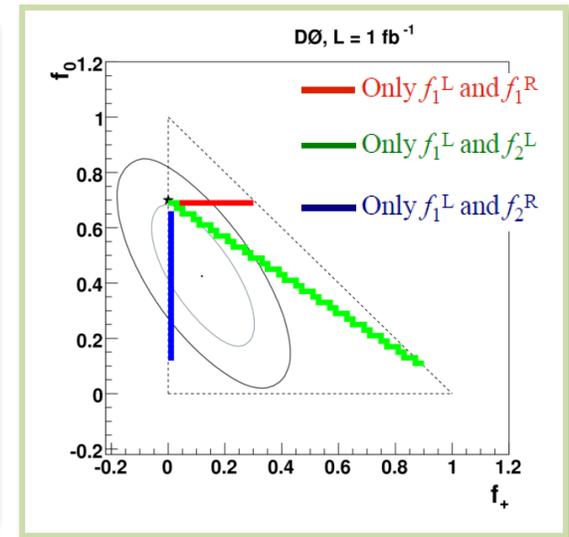
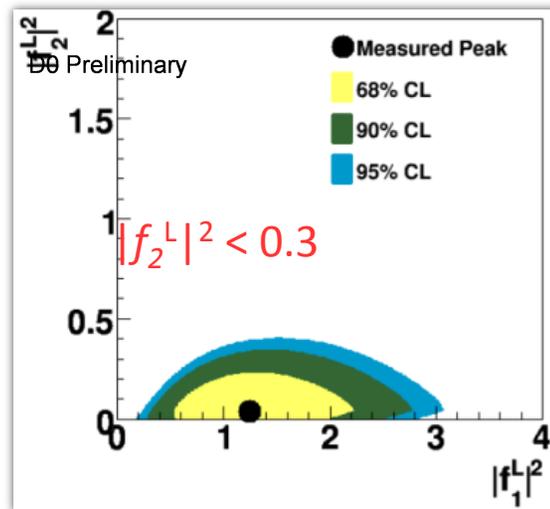
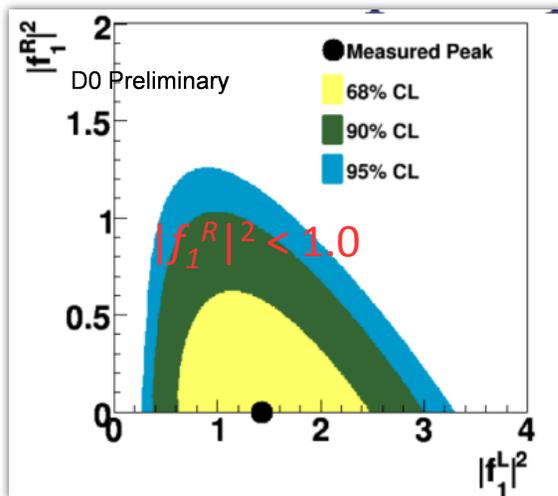
- Anomalous couplings measurement in single top (PRL 101, 221801 (2008))

$$f_{0, \text{meas}} = f_0(f_1^L, f_2^L, f_1^R, f_2^R)$$

$$f_{+, \text{meas}} = f_+(f_1^L, f_2^L, f_1^R, f_2^R)$$

$$\Delta\sigma_{s, \text{meas}} = \Delta\sigma_s(f_1^L, f_2^L, f_1^R, f_2^R)$$

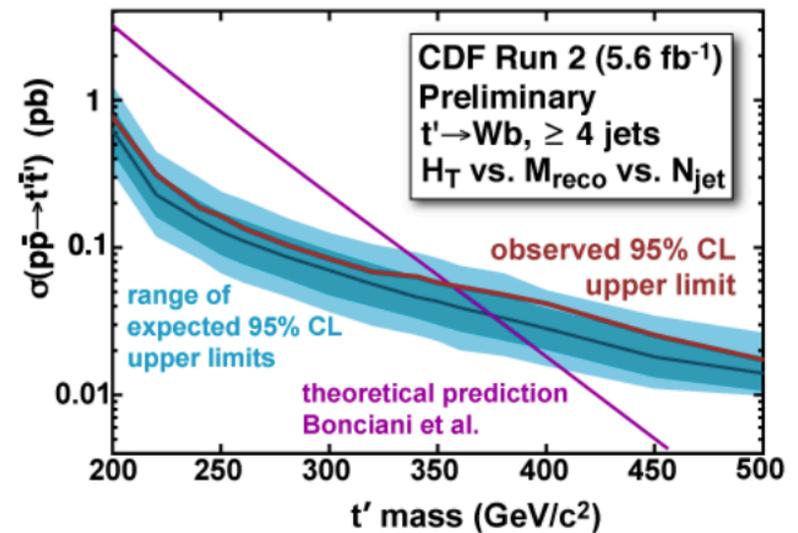
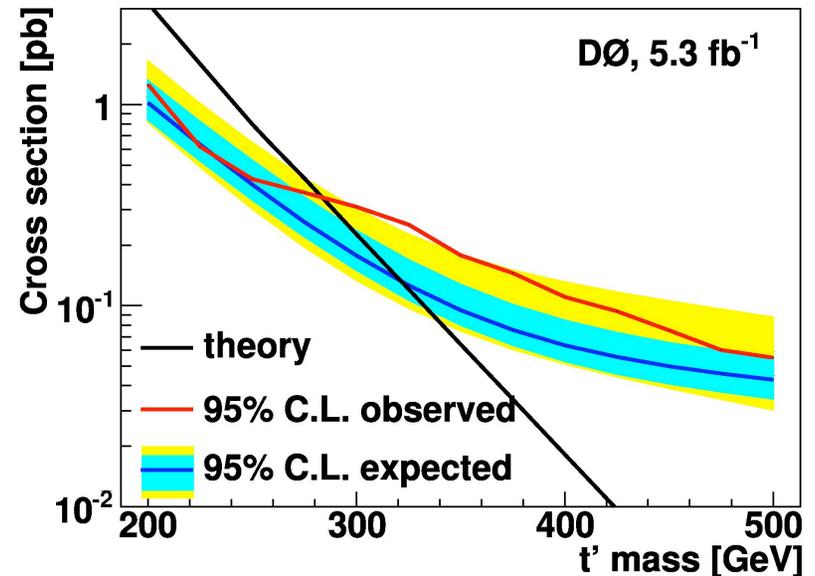
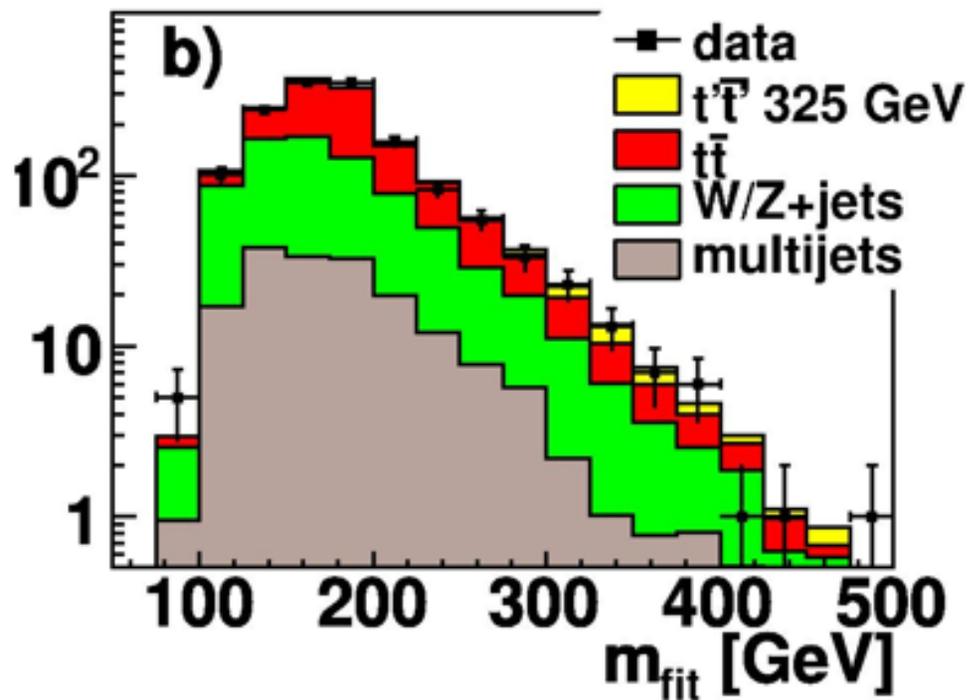
$$\Delta\sigma_{t, \text{meas}} = \Delta\sigma_t(f_1^L, f_2^L, f_1^R, f_2^R)$$



Search for 4th Generation Heavy Quark

Search for fourth generation quark, t'

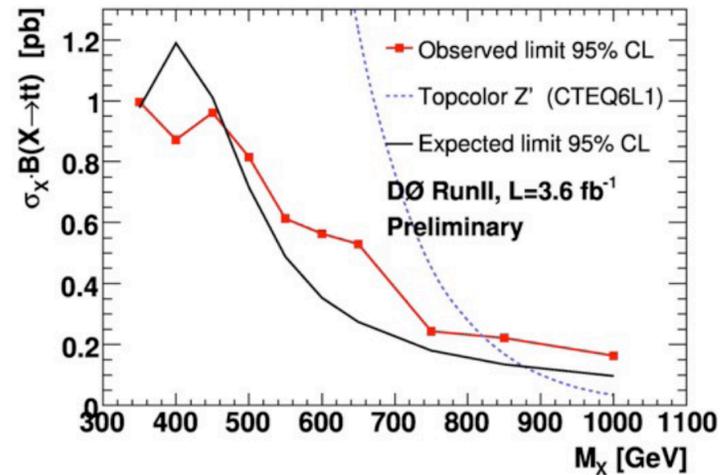
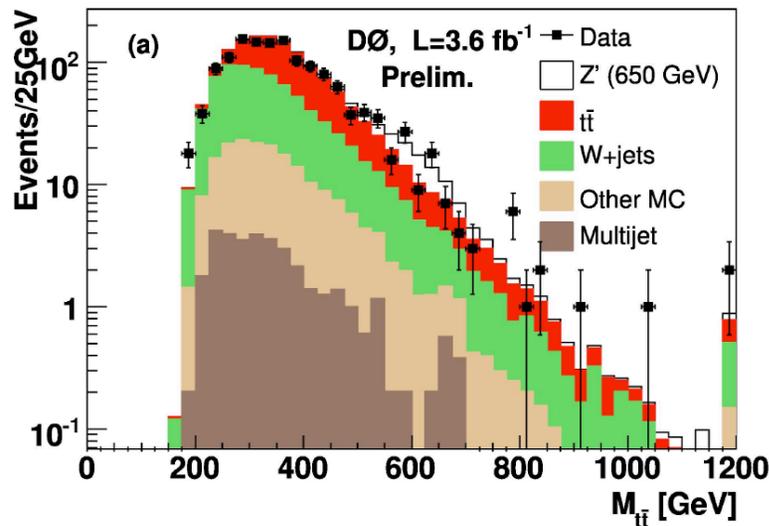
- More massive than top quark
- assume $m_{t'} - m_b < m_W$ and $B(t' \rightarrow Wb) = 100\%$
- @10TeV 200/pb muon+jets only CMS can exclude $M_{t'} < 400$ GeV



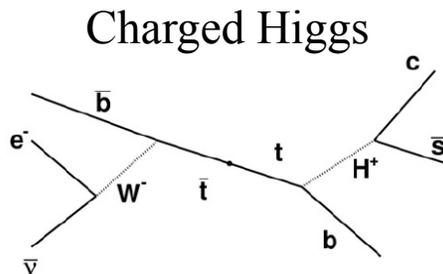
Search for Heavy Resonances

- **Top-antitop resonance**

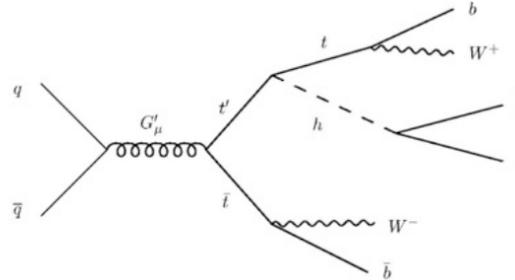
- Search for excess in $t\bar{t}$ invariant mass distributions from Z' boson
- Analysis just started but since basic selection and systematics samples can be reused from t' analysis we should have a publication soon



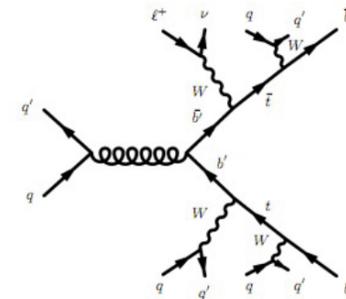
- **Possible future searches with $t\bar{t}$ signatures**



$t\bar{t}H$ search



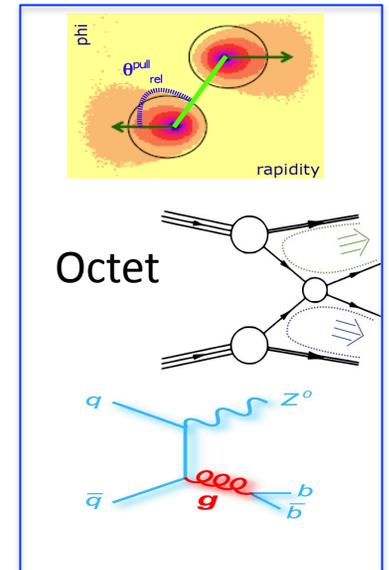
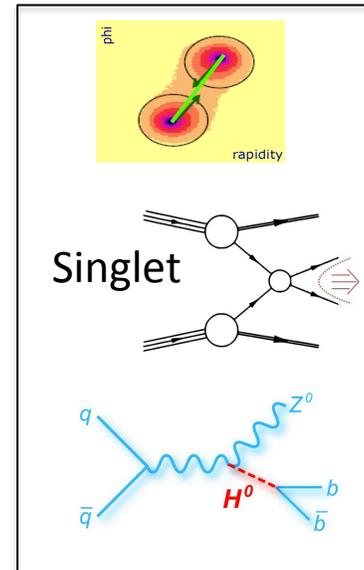
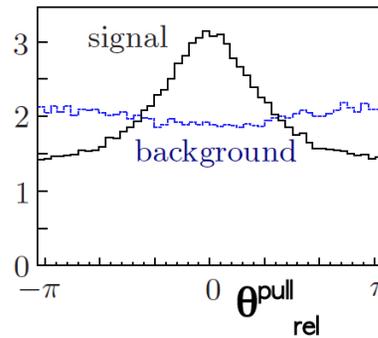
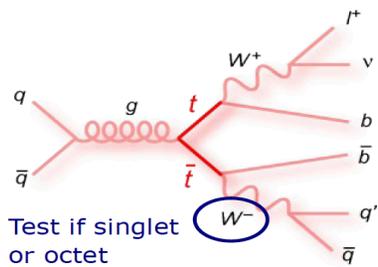
b' search



Color Flow

Gallicchio, Schwartz, PRL 105, 02200(2010)

- Jet shape influenced by color flow
- Shape influenced by direction of color flow!
 - Distinguish processes with same final state

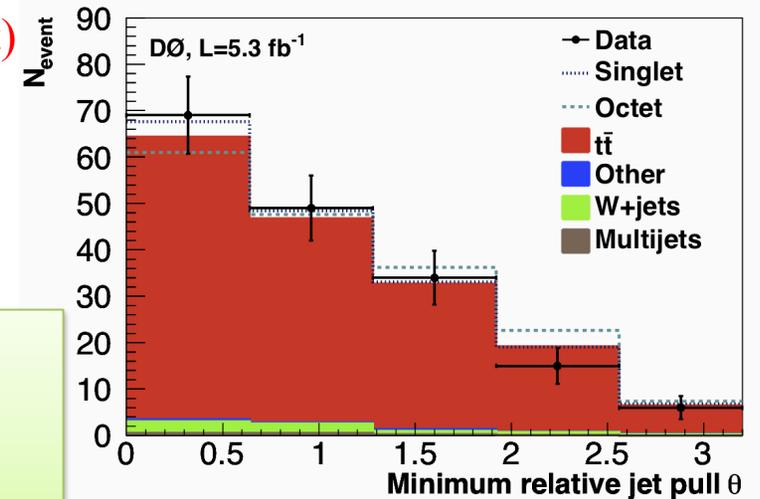


Fraction of singlet = $0.56 \pm 0.38(\text{stat+syst}) \pm 0.19(\text{MC stat})$

Expected: Exclude octet “W” @ 99% C.L.

Expect $f_{\text{Singlet}} = 1$ in SM

First study of color flow in $t\bar{t}$ events
 First extraction of f_{Singlet}
 (using only color flow information)



Summary – A tribute to Tevatron

- The Tevatron has taken us far in understanding the SM
- The degree of sophistication of object algorithms, analysis techniques and tools developed at the Tevatron will be used by next generations. These advances will of course migrate to the LHC experiments.
- The legacy of the Tevatron will be in its discovery and elucidation of the top quark, W & Z physics and perturbative QCD. It still has a critical role to play in the Higgs story.

Tevatron could exclude or discover Higgs in the entire mass range favored by the electroweak fits

Tevatron has already shown how “almost impossible” can be made possible!

- May be some hint of new physics?(only part of data delivered has been analysed yet)

..... as far as top quark is concerned while LHC will be able to test most of the properties in detail, the legacy mass measurement and complimentary measurements at the Tevatron will still be relevant

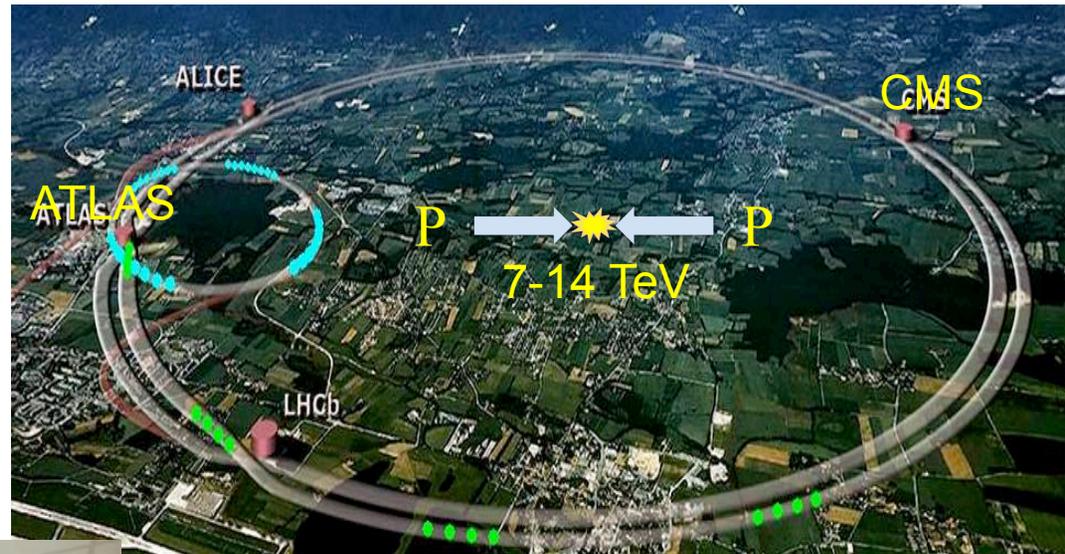
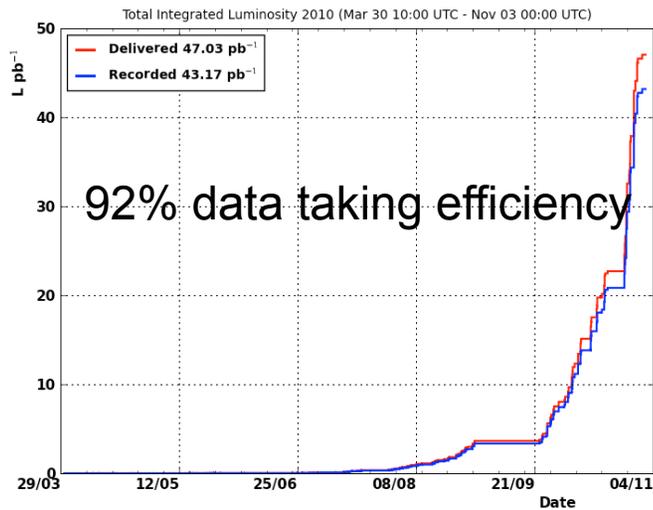
- It is a great time to be a physicist
- We had two revolutions at the turn of last century – these revolutions changed the way we look at our universe
- There are again many questions unanswered and hints will come from experiments
- With Tevatron producing exciting results, LHC finally coming online and many other experiments from under ground to outer space are giving me hope that revolution is in the air

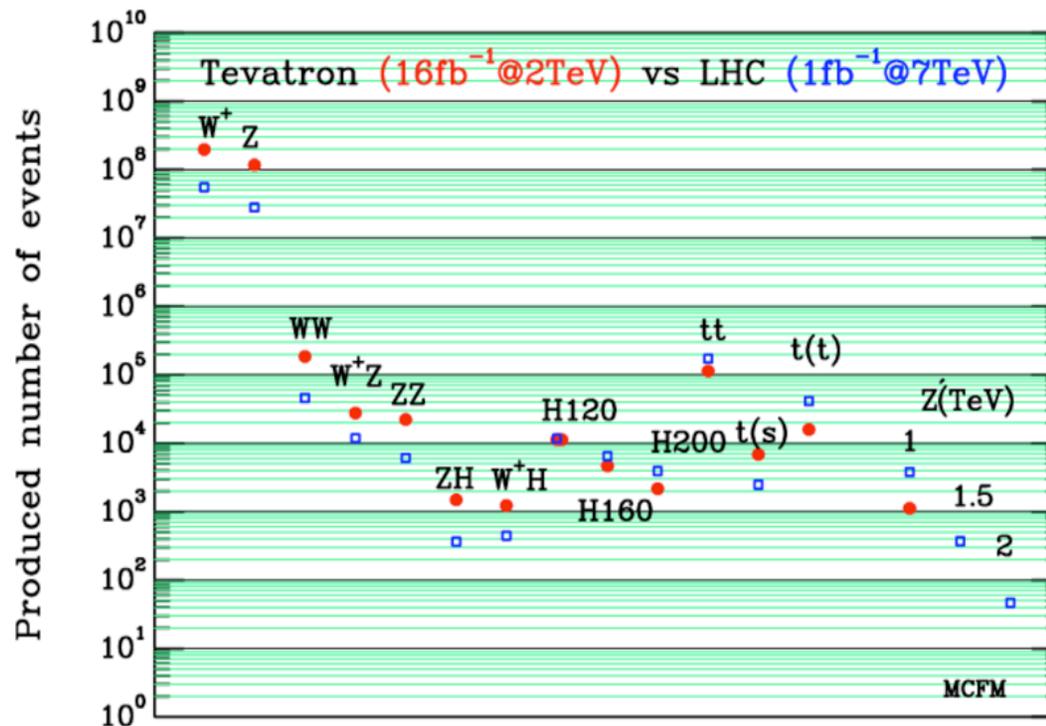
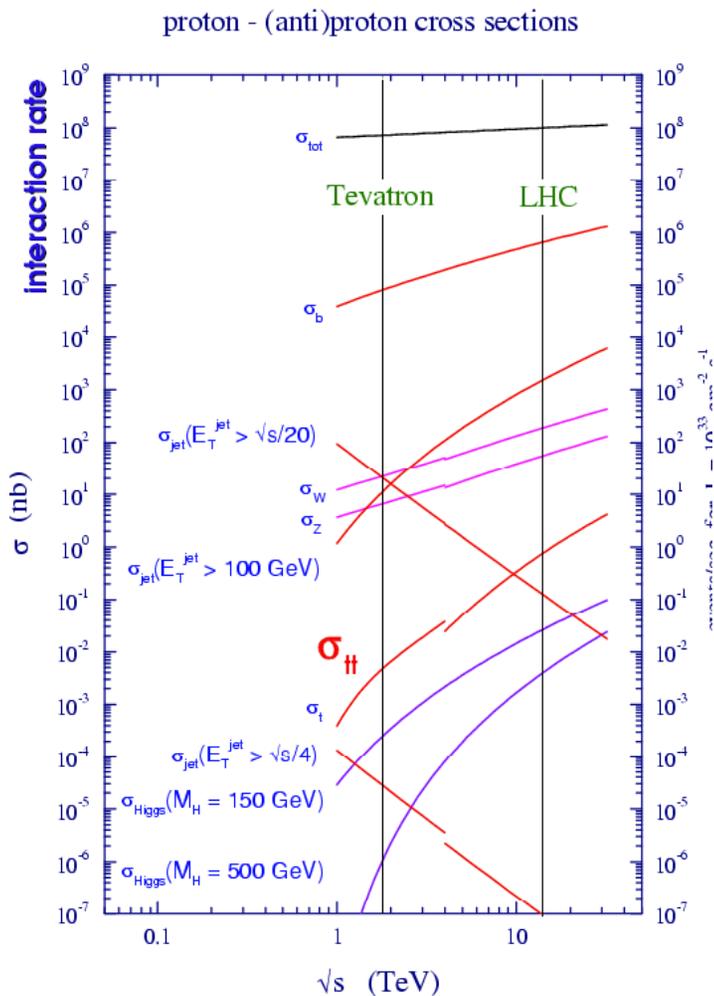
Good luck to us all!!!!



LHC

Conceived in the 1980s and approved for construction by the CERN Council in late 1994.





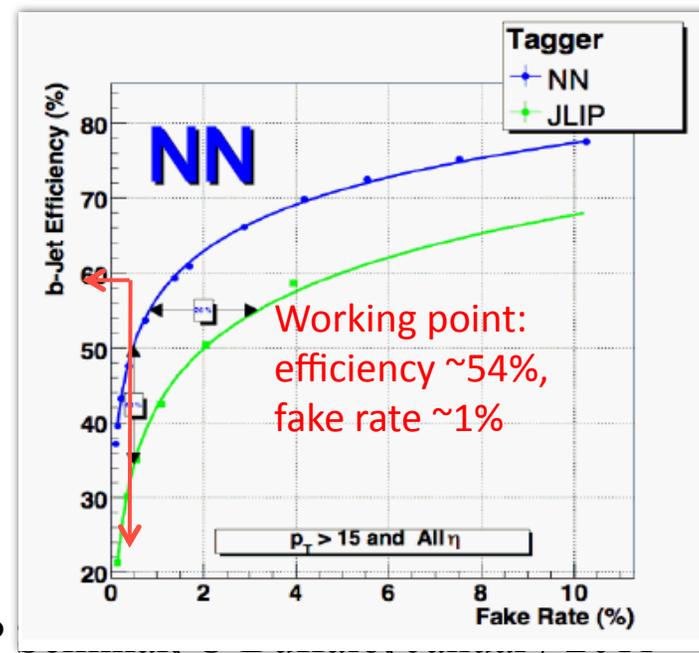
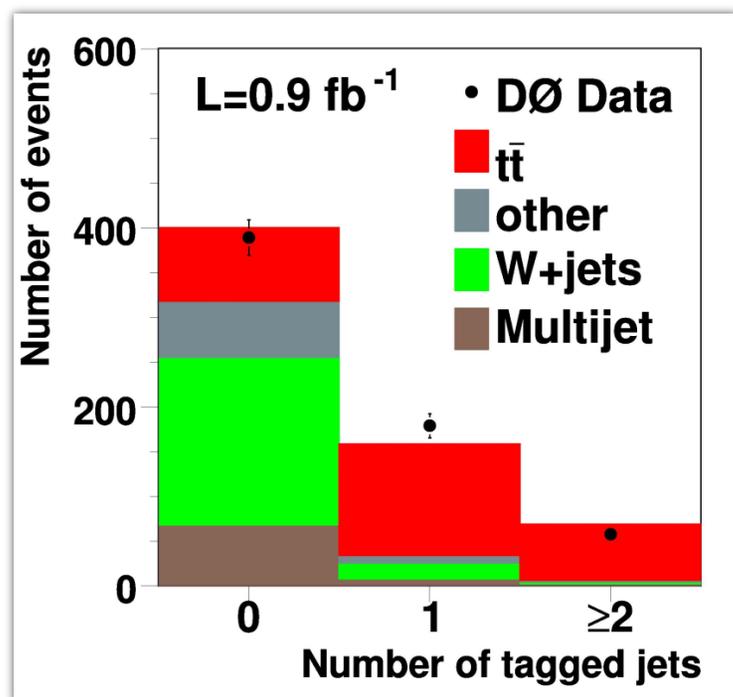
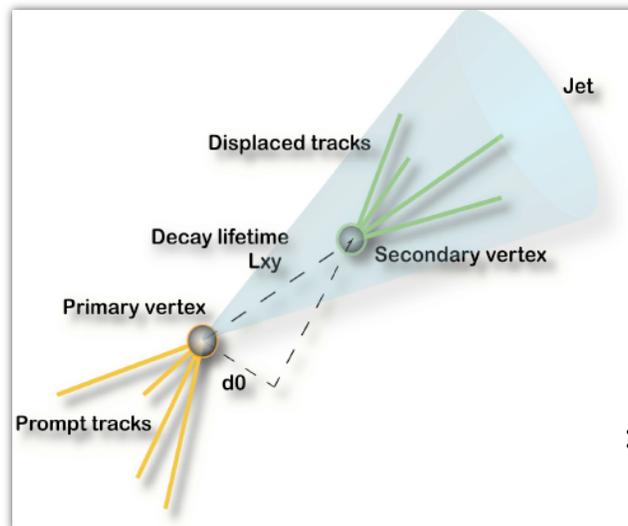
Standard model $t\bar{t}$ cross section at 14TeV is $\sim 886\text{pb}$

- Expected number of top pairs $\sim 9 \times 10^6$ / year
- Total number of pairs seen at CDF is ~ 35000

similar size of electroweak samples: top, W, Z

B Jet Identification

- B -hadron lifetime $\tau \sim 1$ ps
 - B -hadron travels $L_{xy} \sim 1$ mm before decay
- Combine properties of reconstructed secondary vertices and displaced tracks in 7-variable network



Shabnam Jabeen (Brown University)

HEP

$$A_C = \frac{N_t(p) - N_{\bar{t}}(p)}{N_t(p) + N_{\bar{t}}(p)}$$

Charge asymmetry: number tops and anti-tops
in a given direction (proton beam)

$$A_{fb} = \frac{N_t(p) - N_t(\bar{p})}{N_t(p) + N_t(\bar{p})}$$

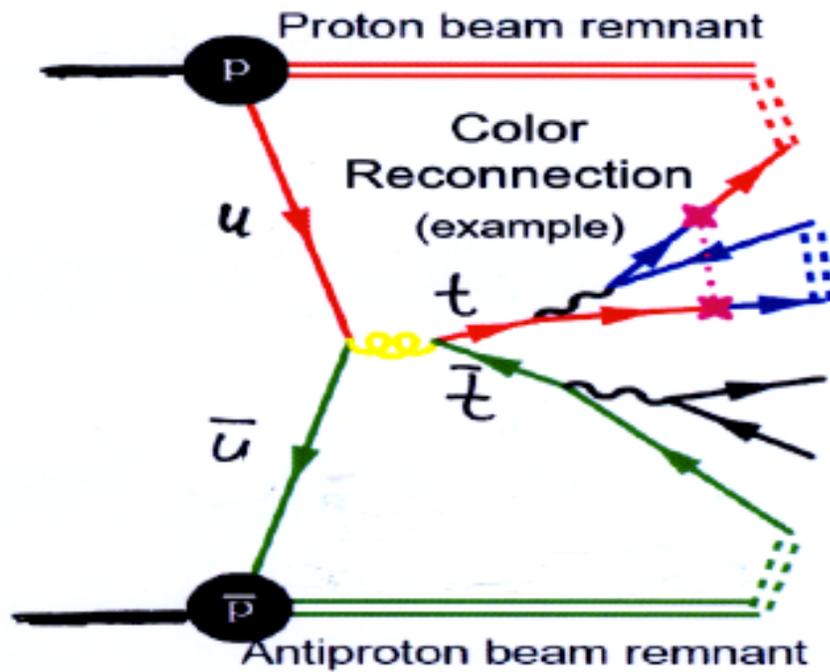
Forward-backward asymmetry: number of top
and anti-top quarks moving for or against a
given direction

For CP invariant system $N_{\bar{t}}(p) = N_t(\bar{p})$

$$A_C = A_{fb}$$

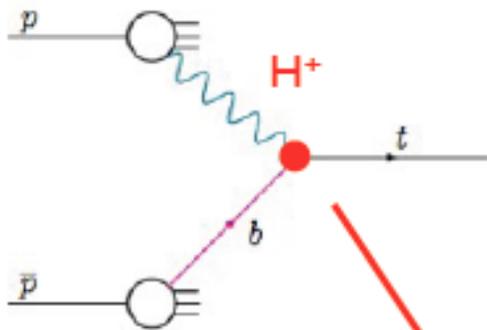
$$A_{fb} = \frac{N^{\Delta y > 0} - N^{\Delta y < 0}}{N^{\Delta y > 0} + N^{\Delta y < 0}}$$

$$\Delta y = y(\text{top}) - y(\text{anti-top})$$

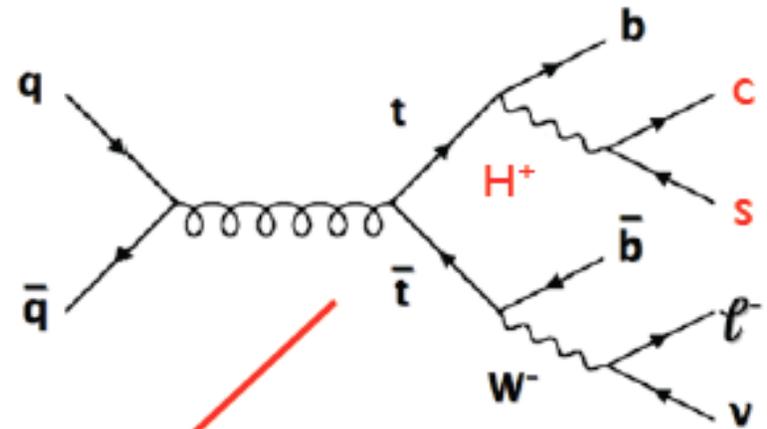


example: charged Higgs with $m_{H^+} < m_t - m_b$

t-channel cross section



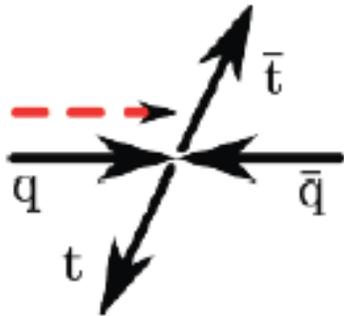
branching ratio $t \rightarrow Wb$



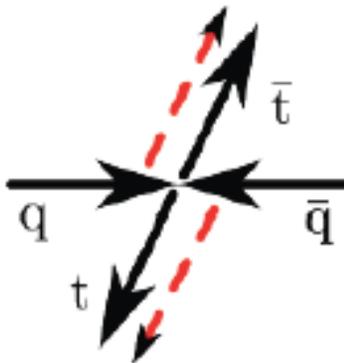
increase

$\neq 1$

$$\Gamma_t = \frac{\sigma(t\text{-channel}) \Gamma(t \rightarrow Wb)_{SM}}{\mathcal{B}(t \rightarrow Wb) \sigma(t\text{-channel})_{SM}}$$

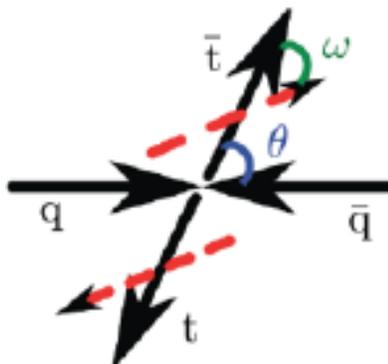


beamline: $A = 0.777$ at NLO
 best for production at threshold



helicity: $A = -0.352$ at NLO
 use direction of (anti)top quark in $t\bar{t}$ rest frame to quantize the spin

Helicity angle: angle between decay product momentum in top rest frame and top quark momentum in $t\bar{t}$ rest frame

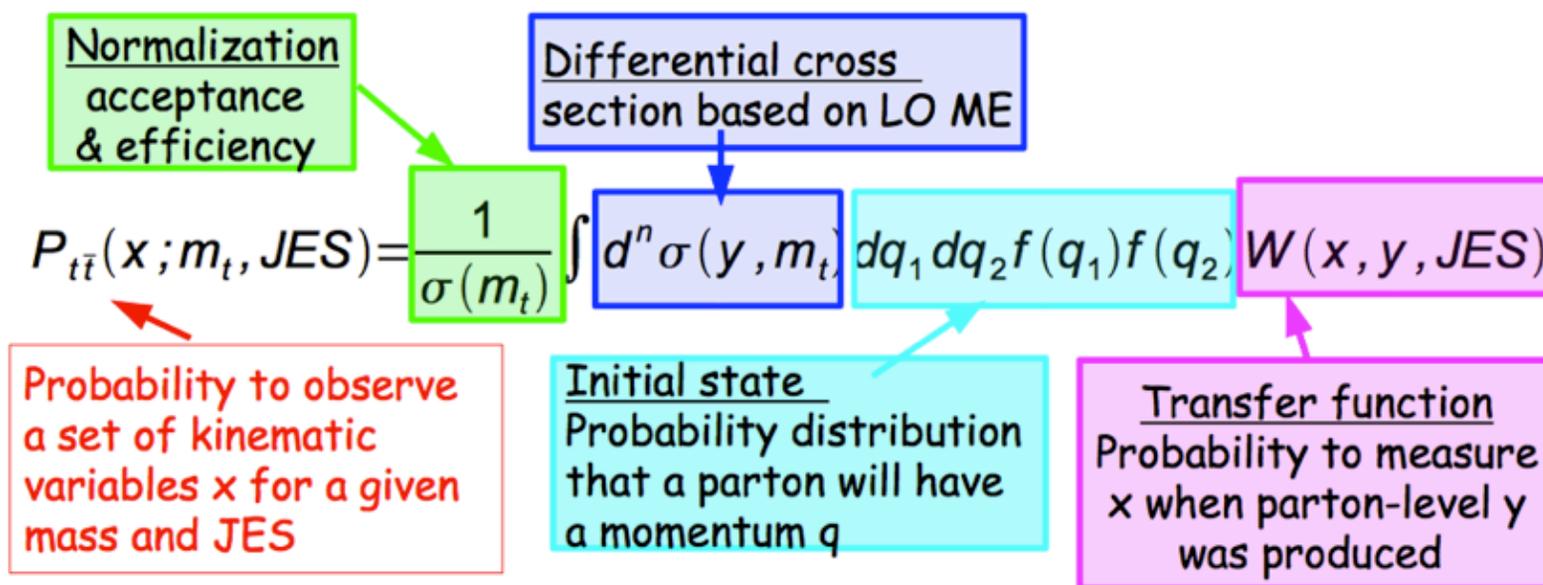


$$\tan \omega = \sqrt{1 - \beta^2} \tan \theta$$

off-diagonal: $A = 0.782$ at MCNLO
 good for pairs above threshold

Bernreuther, Brandenburger, Si and Uwer et al., Nucl. Phys. B 690, 81 (2004)

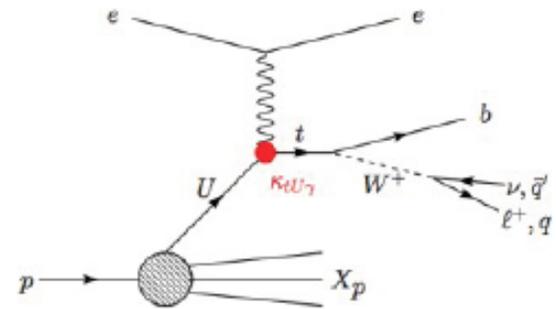
ME method details



- Integrate over unknown q_1, q_2, y
- The jet energy calibration (JES) is a free parameter in the fit, constrained in-situ by the mass of hadronically decaying W

$$\mathcal{P}_{\text{event}}(x; m_t, JES) = f_t \mathcal{P}_{t\bar{t}}(x; m_t, JES) + (1 - f_t) \mathcal{P}_{bkg}(x, JES)$$

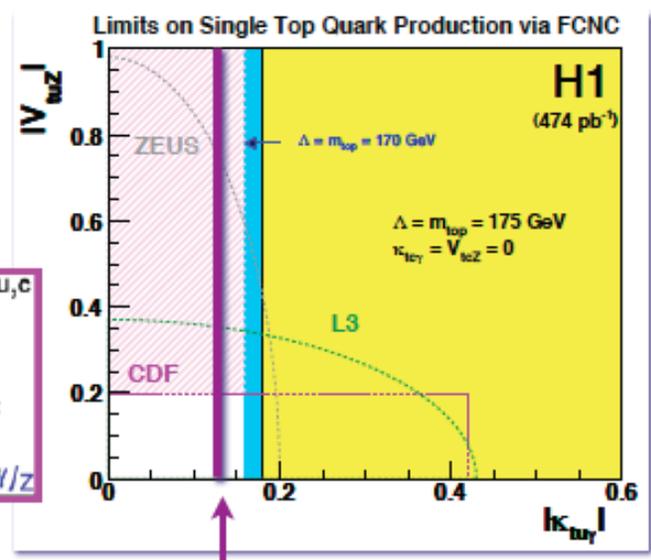
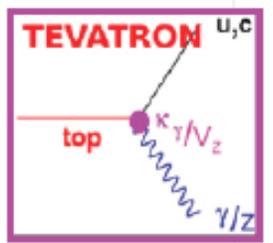
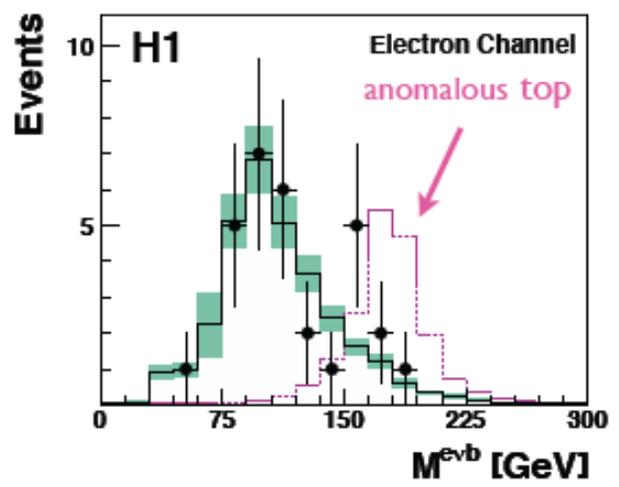
- ❑ Use the same selection as for W
- ❑ SM production is strongly suppressed
- ❑ Can be enhanced by FCNC
 - ▶ coupling of t to up-type quark U via γ or Z
- ❑ Background: single W production



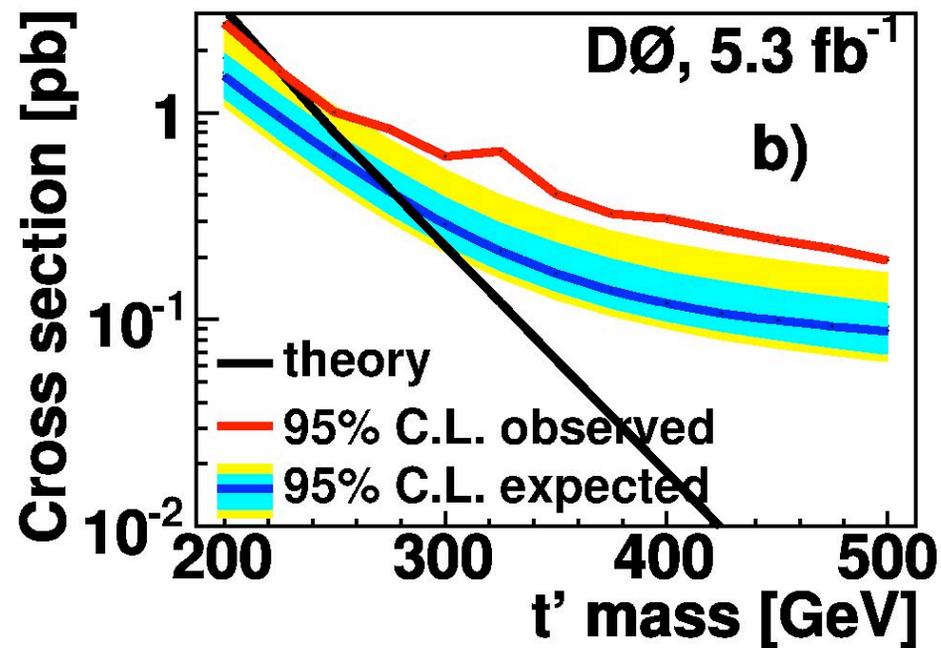
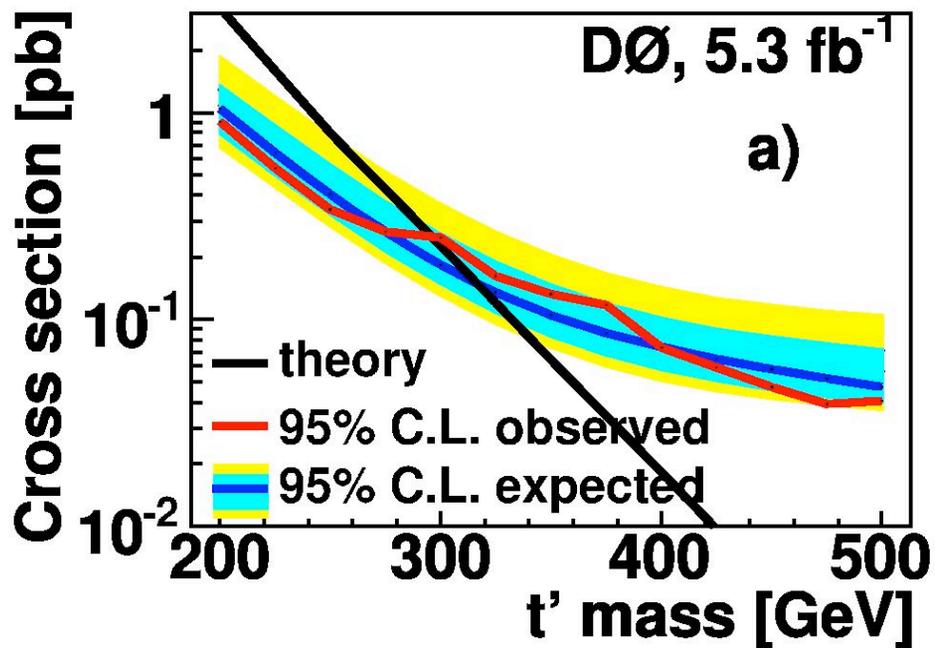
$$\sigma(ep \rightarrow etX) < 0.25 \text{ pb}$$

$$\sigma(ep \rightarrow etX) < 0.23 \text{ pb}$$

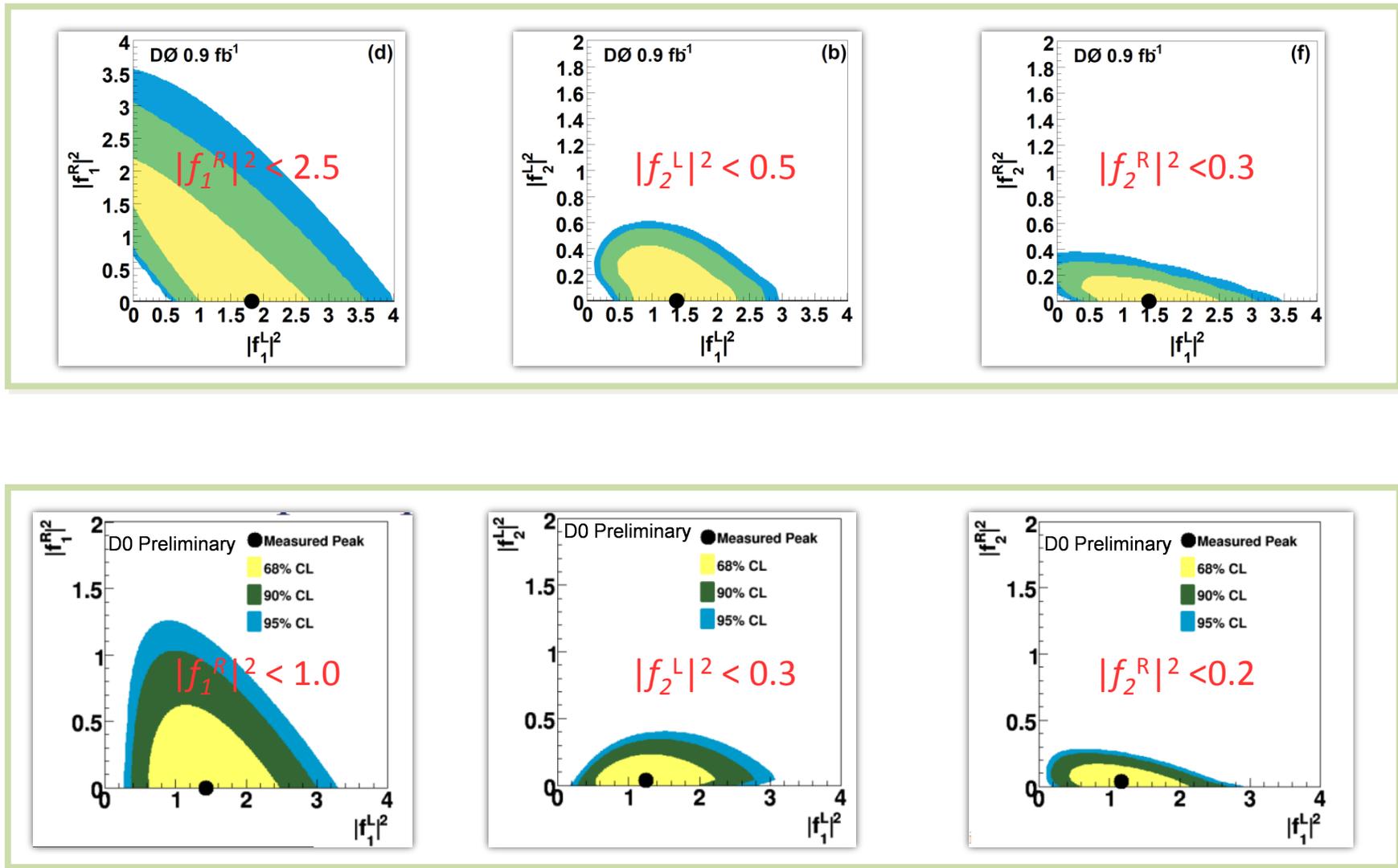
 474 pb⁻¹
 277 pb⁻¹



HERA I+HERA II, ZEUS, 359 pb⁻¹
 $\sigma < 0.13 \text{ pb}, \kappa_{tu\gamma} < 0.13$



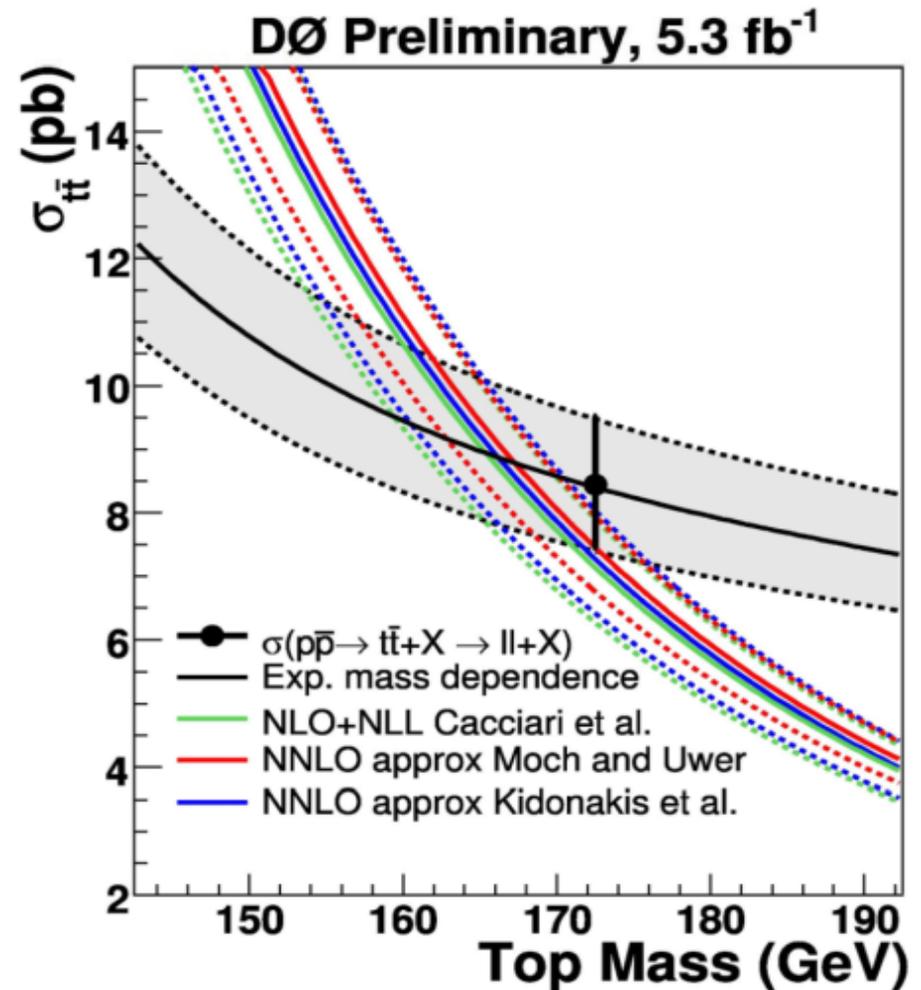
W Helicity and Anomalous Couplings



Top Quark Mass from Cross Section

- The Top quark cross section measurement allows for an indirect measurement of the top mass using the top-mass dependence of the cross section
- This dependence is different for different top mass schemes
 - so we can investigate these differences experimentally

Pole mass and \overline{MS} mass can be converted into one another



Top Quark Mass from Cross Section

- The experimental cross section is fitted as a function of the top quark mass

$$\sigma_{t\bar{t}}(m_t^{\text{MC}}) = \frac{1}{(m_t^{\text{MC}})^4} [a + b (m_t^{\text{MC}} - m_0) + c (m_t^{\text{MC}} - m_0)^2 + d (m_t^{\text{MC}} - m_0)^3]$$

- A joint likelihood is calculated

Gaussian uncertainties for experimental measurement

Renormalization and factorization scale uncertainties on theory calculations are taken to be flat and changed from m_t to $m_t/2$ and $2m_t$

PDF uncertainties are taken to be Gaussian

$$L(m_t) = \int f_{\text{exp}}(\sigma|m_t) (f_{\text{scale}}(\sigma|m_t) \star f_{\text{PDF}}(\sigma|m_t)) d\sigma$$

- Input MC mass is assumed to be pole mass
Measurement is repeated by assuming input MC mass is MS-bar mass instead
Difference is taken as additional uncertainty

