

# **CKM Unitarity Triangle:**

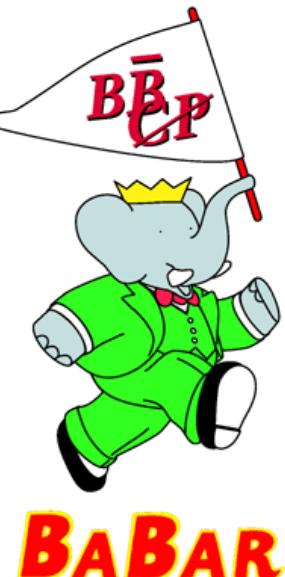
## **Update on Angles from *BaBar***

*Particle Physics Seminar  
Physics Department, Brookhaven National Laboratory*

*Thursday, February 28, 2008*

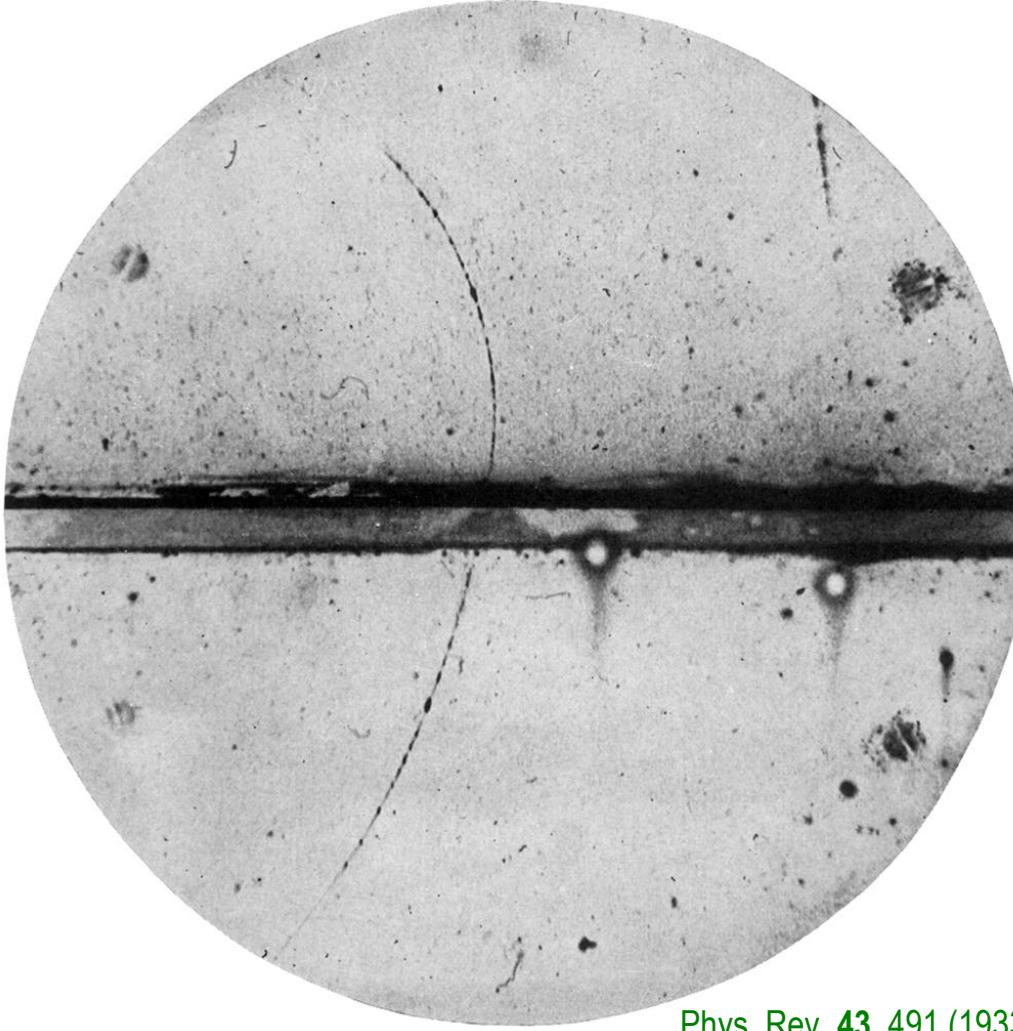
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# Discovery of antimatter

*Each particle, except the truly neutral ones, has an antiparticle*



Phys. Rev. 43, 491 (1933)

FIG. 1. A 63 million volt positron ( $H\rho = 2.1 \times 10^5$  gauss-cm) passing through a 6 mm lead plate and emerging as a 23 million volt positron ( $H\rho = 7.5 \times 10^4$  gauss-cm). The length of this latter path is at least ten times greater than the possible length of a proton path of this curvature.

1928: Dirac predicts antimatter to explain a seemingly unphysical solution to his equations of relativistic quantum mechanics

1932: Anderson discovers positrons in cosmic rays passing through a Wilson chamber in 1.5 T magnetic field, shares 1936 Nobel Prize



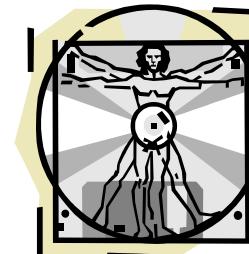
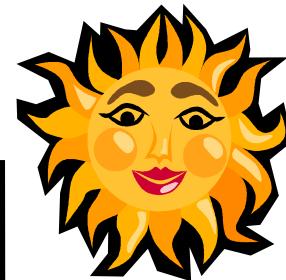
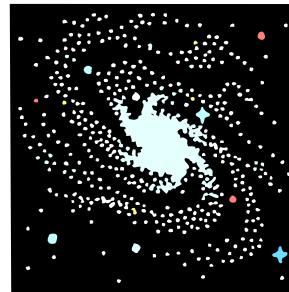
# Matter-Antimatter Asymmetry of the Universe



Very early Universe must have had equal amounts of matter and antimatter. Where did all the antimatter go?

Baryonic asymmetry of the Universe:

$$\frac{N_B - N_{\bar{B}}}{N_\gamma} \simeq \frac{N_B}{N_\gamma} \simeq 5 \times 10^{-10}$$





# Symmetries in Nature

*Symmetries have played a central role in the development of physics:*

Translation in space  $\leftrightarrow$  conservation of linear momentum

Rotation in space  $\leftrightarrow$  conservation of angular momentum

Translation in time  $\leftrightarrow$  conservation of energy

Redefinition of relative phase  $\leftrightarrow$  conservation of electrical charge

# Parity: a discrete symmetry

$$\vec{r} \rightarrow -\vec{r}, \quad \vec{s} \rightarrow +\vec{s}, \quad \vec{L} \rightarrow +\vec{L}$$

$$P |a(E, \vec{p}, \lambda)\rangle = \eta_P |a(E, -\vec{p}, -\lambda)\rangle \quad (\lambda \equiv \vec{s} \cdot \vec{p})$$

**Spatial parity**  $P$  :  $P = P^{-1} = P^\dagger, \quad \eta_P = \pm 1$

$$P(Y_{\ell m}(\vartheta, \varphi)) = Y_{\ell m}(\pi - \vartheta, \pi + \varphi) = (-1)^\ell Y_{\ell m}(\vartheta, \varphi)$$

$$P(\text{fermion}) = -P(\text{antifermion}); \quad P(q \bar{q}') = (-1)^{L+1}$$

**Charge conjugation**

$$C |a(E, \vec{p}, \lambda)\rangle = \eta_C |\bar{a}(E, \vec{p}, \lambda)\rangle$$

$C$  :  $C = C^{-1} = C^\dagger, \quad \eta_C = \pm 1$

*Fermi statistics*

*Spin wavefunction*

*Orbital wavefunction*

$$-1 = (-1)^{S+1} \cdot (-1)^L \cdot C(q \bar{q}) \Rightarrow C(q \bar{q}) = (-1)^{L+S}$$

**Time reversal**  $T$  :  $T |a(E, \vec{p}, \lambda)\rangle = \eta_T \langle a(E, -\vec{p}, \lambda)| ; \quad \eta_T = \pm 1$



# CPT theorem



Lagrangian of any quantum field theory  
that obeys the laws of relativity and causality, conforms to the quantum  
mechanical interpretation of the positive, conserved probability, and is local,  
**is invariant under the combined *CPT* transformation.**

**Consequence:** masses and total decay widths of a particle  
and its antiparticle **must be equal** to all orders of interactions.

**Note:** equality of all *partial* decay widths requires, in addition to  
*CPT*, invariance of the Lagrangian under ***CP***.



# Discovery of CP violation

Christensen, Cronin, Fitch, Turlay @ AGS (Brookhaven), 1964



$$\begin{cases} K^0 = d \bar{s} \\ \bar{K}^0 = s \bar{d} \end{cases} ; \quad \begin{cases} CP|K^0\rangle = e^{+2i\vartheta} |\bar{K}^0\rangle \\ CP|\bar{K}^0\rangle = e^{-2i\vartheta} |K^0\rangle \end{cases} \quad (\vartheta \text{ is a matter of convention})$$

$$\begin{cases} K_1^0 = |K_{CP=+1}\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle + e^{+2i\vartheta} |\bar{K}^0\rangle) \rightarrow \pi^+ \pi^-, \pi^0 \pi^0 \\ K_2^0 = |K_{CP=-1}\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle - e^{+2i\vartheta} |\bar{K}^0\rangle) \rightarrow \pi^+ \pi^- \pi^0, \pi^0 \pi^0 \pi^0 \end{cases}$$

$$\begin{cases} m_{K^0} = 497.648 \pm 0.022 \text{ MeV} \\ m_{K_L^0} - m_{K_S^0} = (3.483 \pm 0.006) \times 10^{-6} \text{ eV} \end{cases} ; \quad \begin{cases} \tau_{K_S^0} = (0.8953 \pm 0.0005) \times 10^{-10} \text{ sec} \\ \tau_{K_L^0} = (5.116 \pm 0.020) \times 10^{-8} \text{ sec} \end{cases}$$

$$\begin{cases} \text{Br}(K_S^0 \rightarrow \pi^+ \pi^-) = 69.20 \pm 0.05 \% \\ \text{Br}(K_S^0 \rightarrow \pi^0 \pi^0) = 30.69 \pm 0.05 \% \\ \text{Br}(K_S^0 \rightarrow \pi^+ \pi^- \pi^0) = 3.5_{-0.9}^{+1.1} \times 10^{-7} \\ \text{Br}(K_S^0 \rightarrow 3\pi^0) < 1.2 \times 10^{-7} \end{cases} ;$$

PDG 2007 data

$$\begin{cases} \text{Br}(K_L^0 \rightarrow 3\pi^0) = 19.51 \pm 0.12 \% \\ \text{Br}(K_L^0 \rightarrow \pi^+ \pi^- \pi^0) = 12.54 \pm 0.05 \% \\ \text{Br}(K_L^0 \rightarrow \pi^+ \pi^-) = (1.966 \pm 0.010) \times 10^{-3} \\ \text{Br}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.64 \pm 0.06) \times 10^{-4} \end{cases}$$

↑ CP violating decays ↑

Through the CPT Theorem, CP violation implies the existence of T violation



# Sakharov's three conditions



**The three conditions necessary to produce the baryonic asymmetry of the Universe:**



(photo circa 1943)

А. Д. Сахаров, *Письма в ЖЭТФ*, 5, № 1, 32-35, 1 января 1967  
A. D. Sakharov, *Soviet Journal of Experimental and Theoretical Physics, Letters to the Editor*, 5, No. 1, 24-27, 1st January 1967

**1. Baryon number violation** (proton decay)

**2. C and  $CP$  violation**

By far the strongest argument for existence of sources of  $CP$  violation in nature is the very fact that we are here today!

**3. Departure from thermal equilibrium**

# The Quark Mixing Matrix

**The only Standard-Model source of  $CP$  violation in the quark sector**



The Cabibbo-Kobayashi-Maskawa matrix relates the electroweak ( $q'$ ) and the mass ( $q$ ) quark eigenstates:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2 / 2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2 / 2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4) + iO(\lambda^6)$$

$$V^\dagger V = 1 \Rightarrow V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

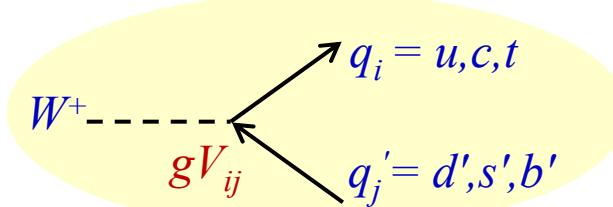
the “unitarity triangle”

$$\alpha \equiv \arg \left[ -\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right]$$

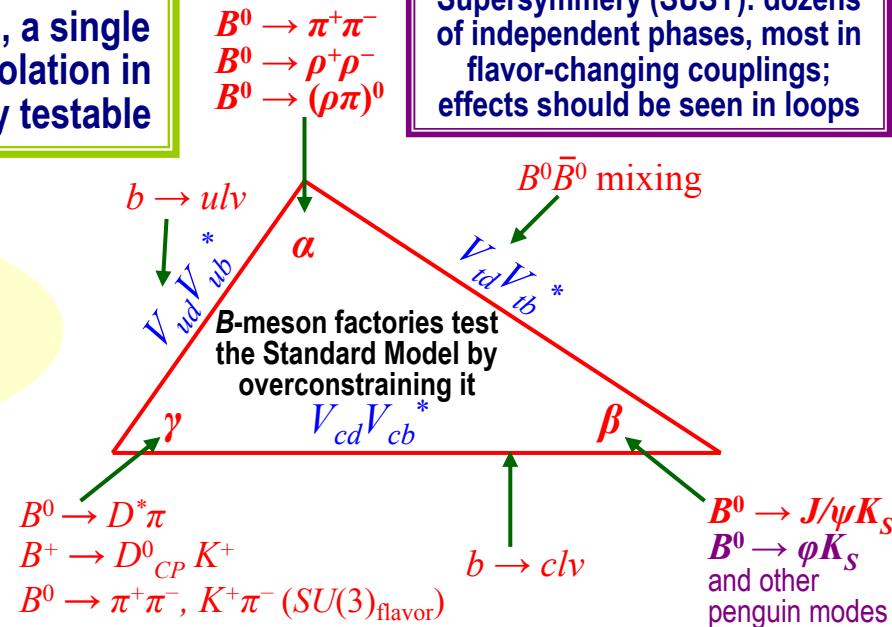
In the Kobayashi-Maskawa model, a single phase is responsible for all  $CP$  violation in meson decays, making it uniquely testable

$$\beta \equiv \arg \left[ -\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right]$$

$$\gamma \equiv \arg \left[ -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right]$$



CKM mechanism alone is far too small to account for the baryon asymmetry of the universe: Gavela et.al, Nucl. Phys. **B 430**, 382 (1994)



# Time evolution of the $B^0$ meson

The time-dependent rate for  $\bar{B}^0$  ( $f_+$ ) or  $B^0$  ( $f_-$ ) decays to a final state  $f$  (neglecting the lifetime difference between the mass eigenstates  $B_{Heavy}$  and  $B_{Light}$ ):

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} [1 \mp C_f \cos(\Delta m \Delta t) \mp S_f \sin(\Delta m \Delta t)]$$

where

$S$  and  $C$  is what we measure

$$|B_{L/H}\rangle = p |B^0\rangle \pm q |\bar{B}^0\rangle, \quad \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f},$$

from mixing,  $\approx e^{-2i\beta}$

$$S_f = \frac{-2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2}, \quad C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

$a_f$  is the time-evolution asymmetry:

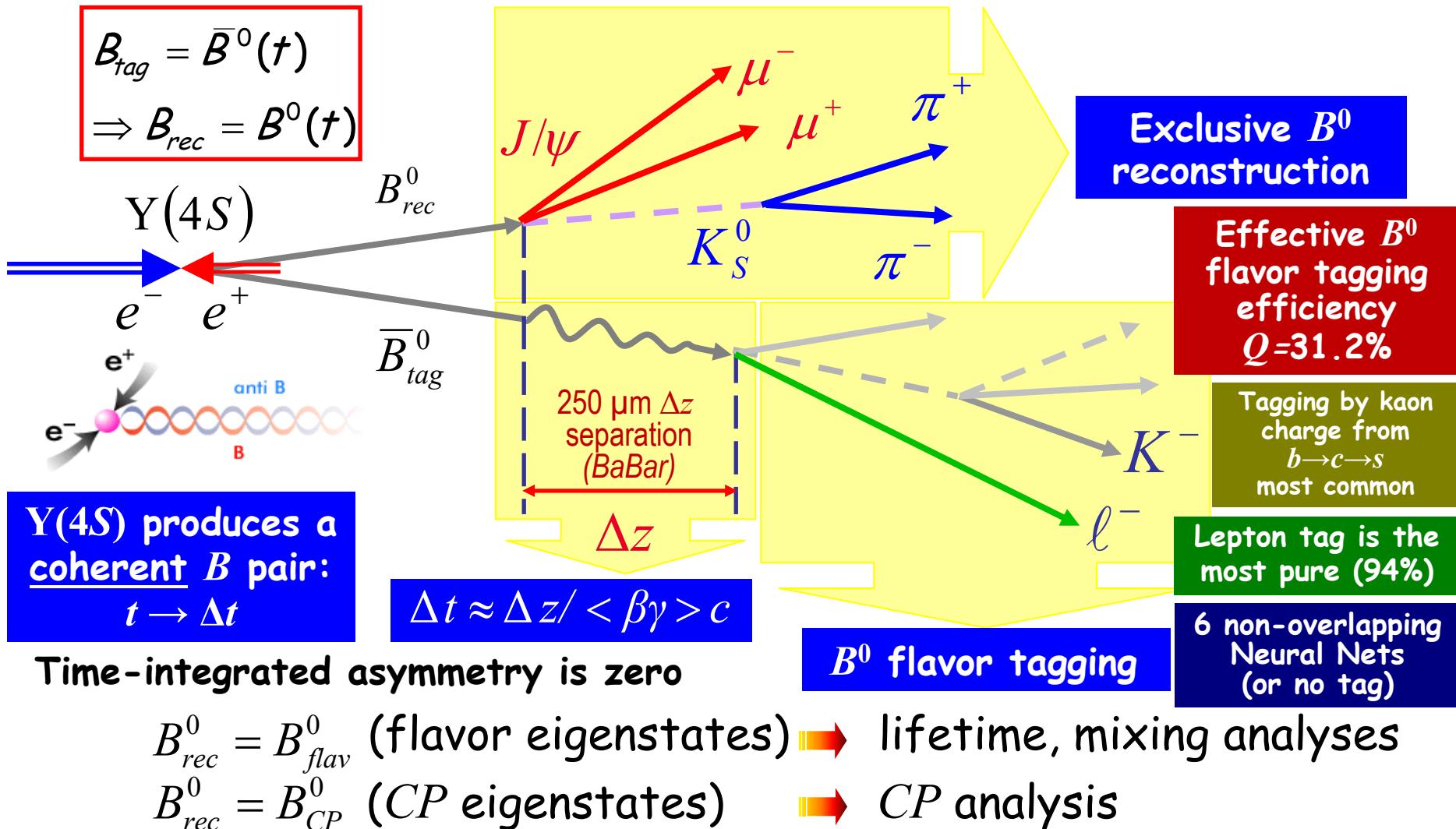
$$a_f(\Delta t) = \frac{f_+(\Delta t) - f_-(\Delta t)}{f_+(\Delta t) + f_-(\Delta t)}$$

If  $f$  is a  $CP$  eigenstate,  $f_{CP}$ , we have  $CP$  violation if  $\lambda_f \neq \pm 1$ :

- $|q/p| \neq 1$  ( $CP$  violation in mixing, very small)
- $|\bar{A}_f/A_f| \neq 1$  (direct  $CP$  violation, small in  $b \rightarrow c\bar{c}s\bar{s}$ )
- $\operatorname{Im}(\lambda_f) \neq 0$  (interference between mixing and decay)

*B. Aubert et al. (BaBar Collaboration)  
Phys. Rev. Lett. 96, 251802 (2006)*

# Time-dependent $CP$ analysis at a $B$ -meson factory



# PEP-II performance

Y(4S) CM energy: 10.580 GeV

Beam energies:

electrons: 9.0 GeV

positrons: 3.1 GeV

Beam currents:

electrons: 2.05 A

positrons: 3.03 A

Number of bunches: 1722

Beam size at IP: 125  $\mu\text{m}$  x 4  $\mu\text{m}$

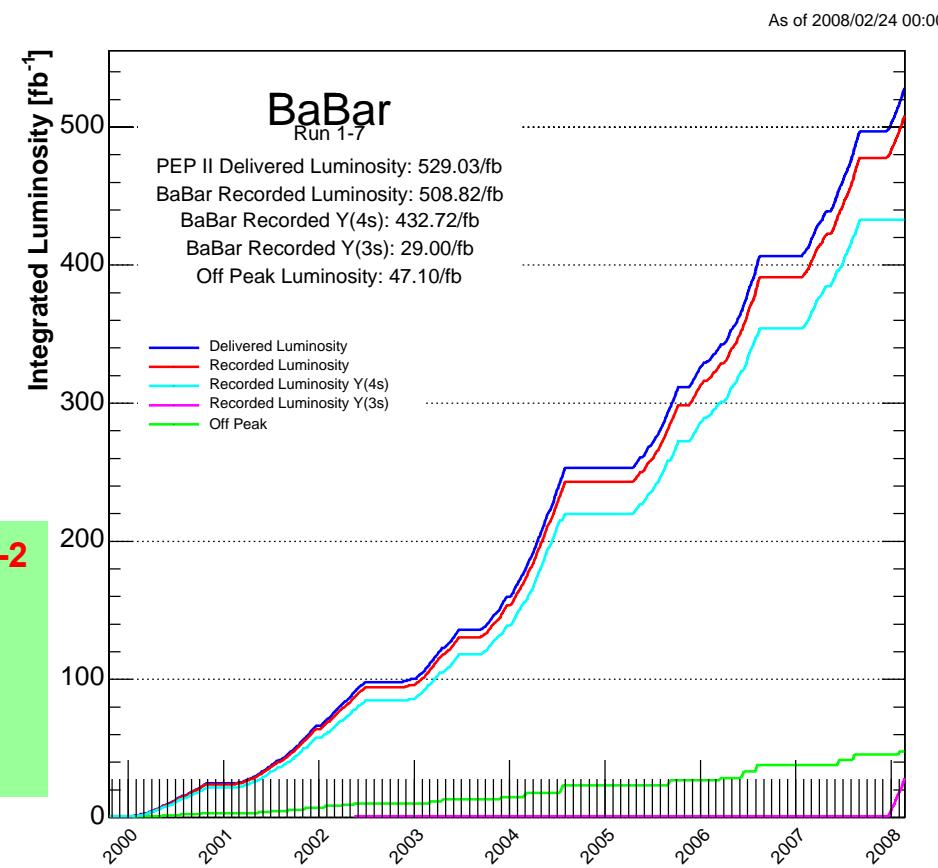
**Peak luminosity:  $12.1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$**

(design:  $3 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ )

**Best 24 hours:  $911 \text{ pb}^{-1}$  delivered**

(design:  $135 \text{ pb}^{-1}/\text{day}$ )

Y(4S) operation concluded on December 21, 2007  
 Y(3S):  $30 \text{ fb}^{-1}$  (done)  
 Y(2S):  $20 \text{ fb}^{-1}$  (in progress)

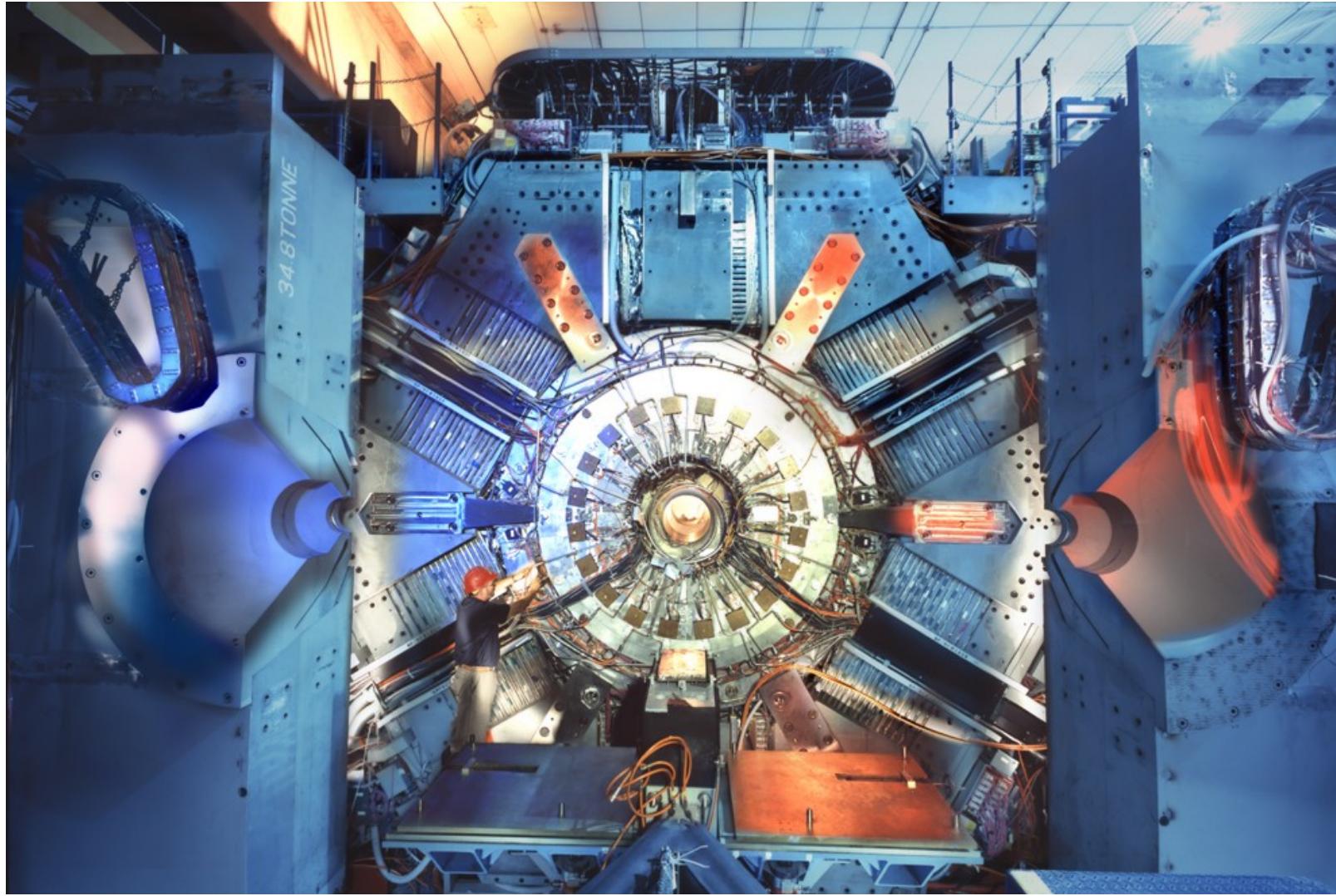




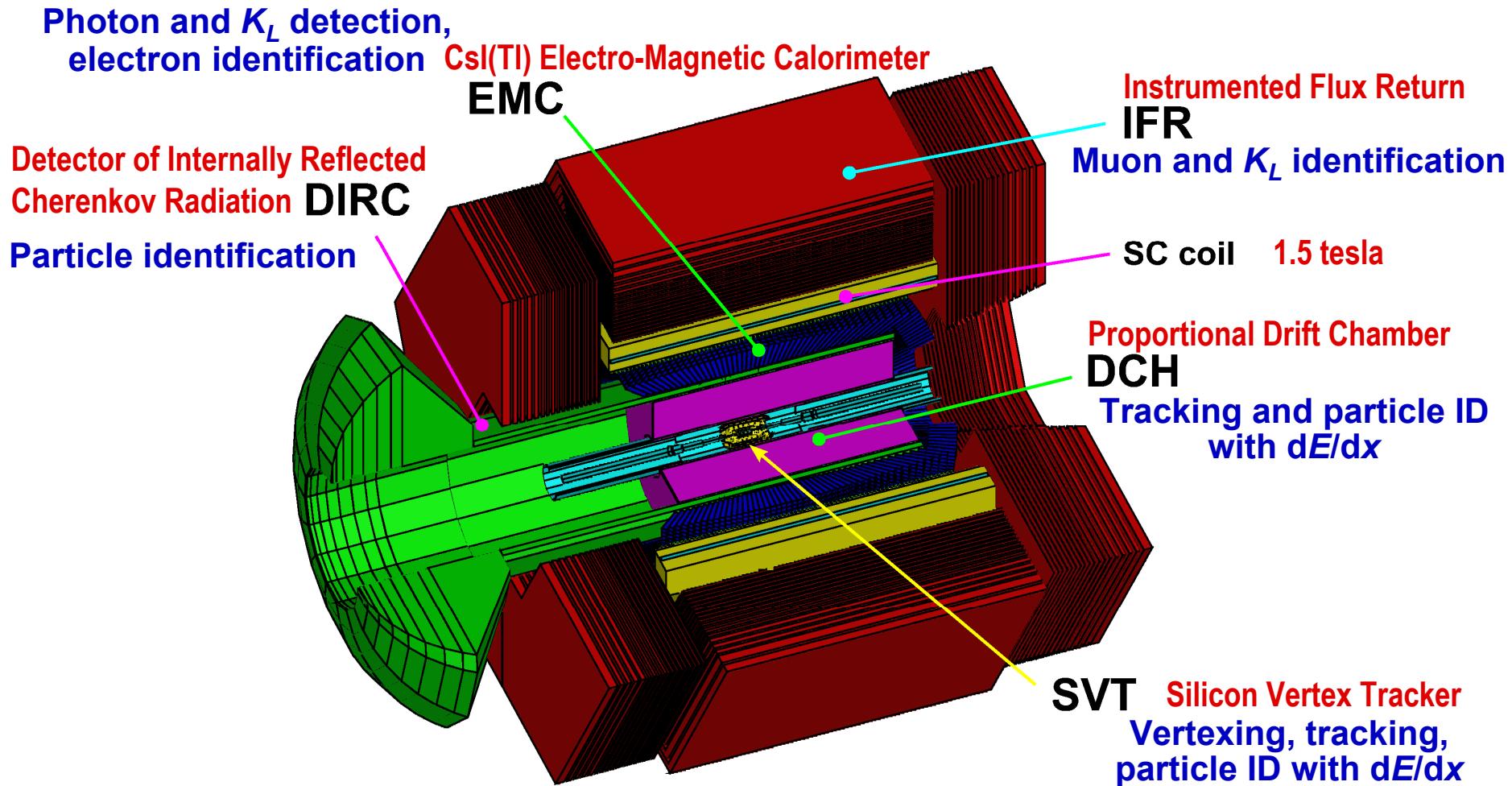
BABAR



# The BaBar detector



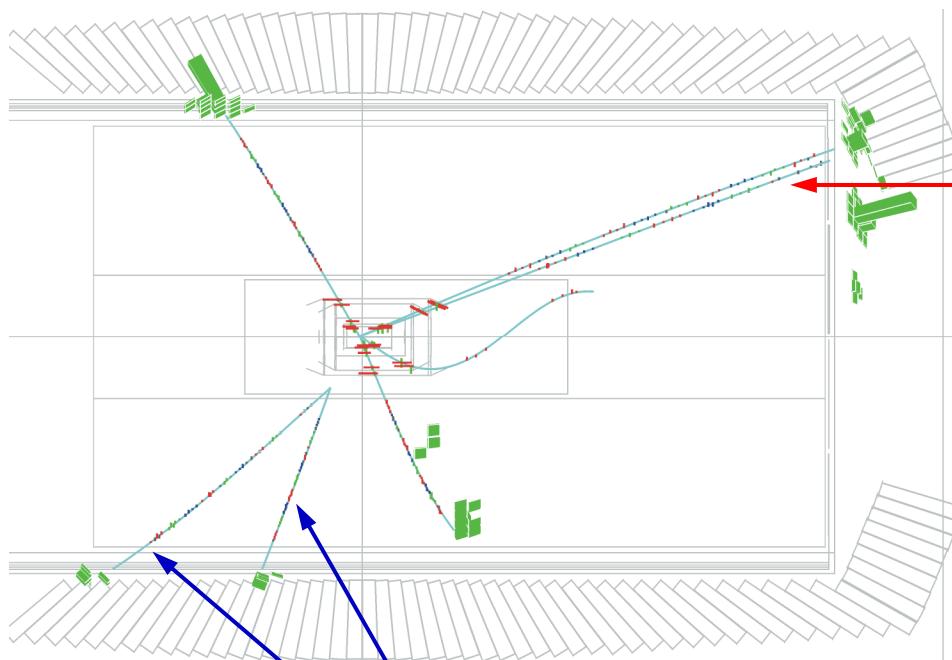
# The BaBar detector



Note that electron ID and muon ID are largely orthogonal to pion/kaon/proton separation with DIRC+DCH+SVT

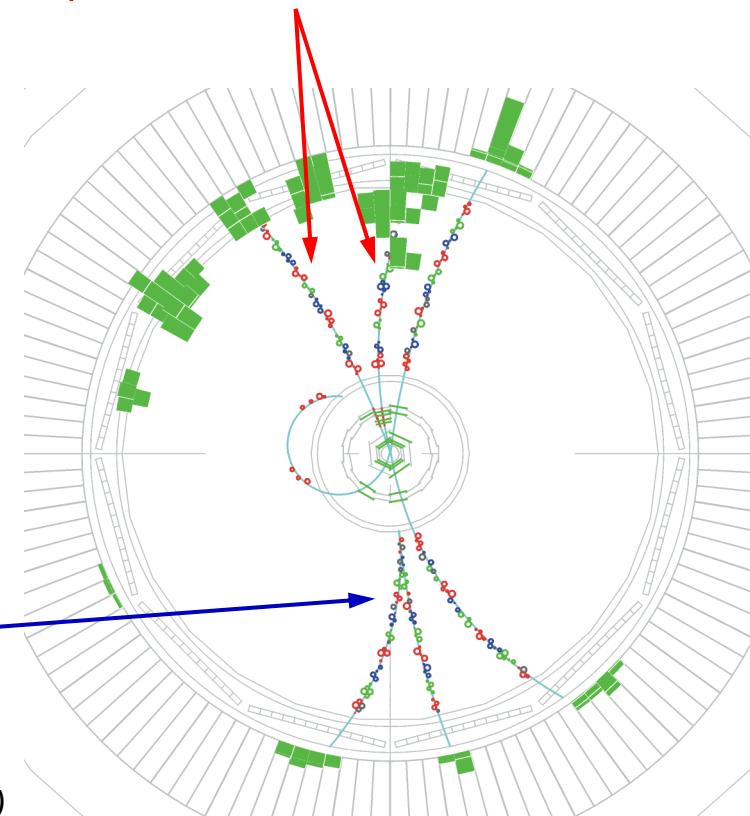
# Example of a $B$ -decay event in BaBar

$$B^0 \rightarrow \phi K_S$$



only the hits that correspond to reconstructed tracks and neutral candidates are shown  
(noise hits are removed)

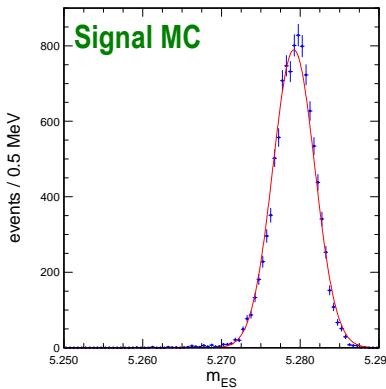
$$\phi \rightarrow K^+ K^-$$



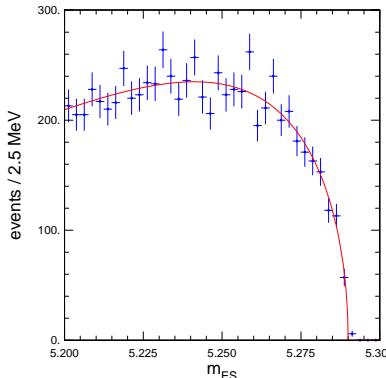
# Common discriminating variables: kinematics

A pair of weakly correlated variables that reflect energy and momentum conservation:  
peaking for fully reconstructed  $B$  decays, smooth for combinatorial background

$$m_{\text{ES}} \equiv \sqrt{E_{\text{CM beam}}^2 - p_{\text{CM } B}^2} = m_B$$

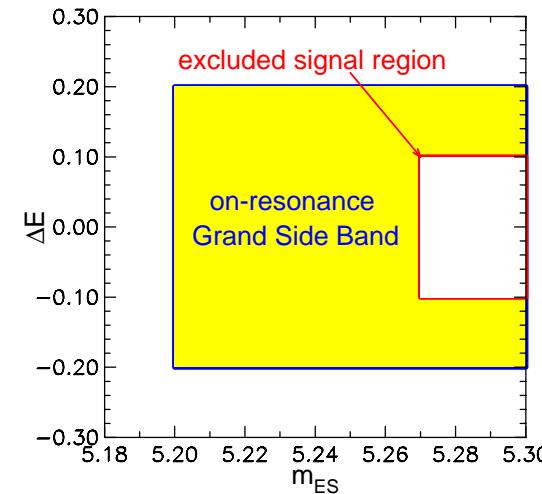


**resolution  $\sim 2.6 \text{ MeV}/c^2$**   
*determined by the beam energy spread*

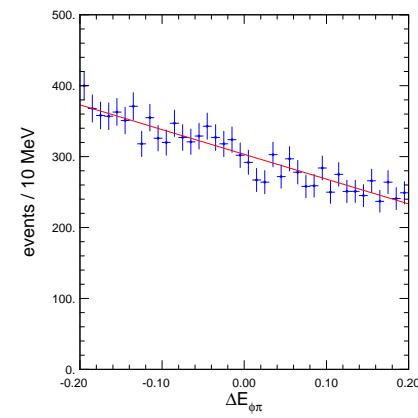
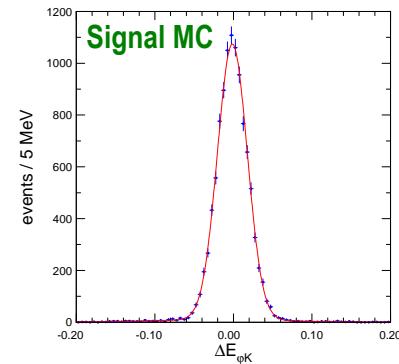


$$\Delta E \equiv E_{\text{CM } B} - E_{\text{CM beam}} = 0$$

**resolution  $\sim 15\text{--}80 \text{ MeV}$**   
*depending on the number of tracks and presence of neutrals in the final state*

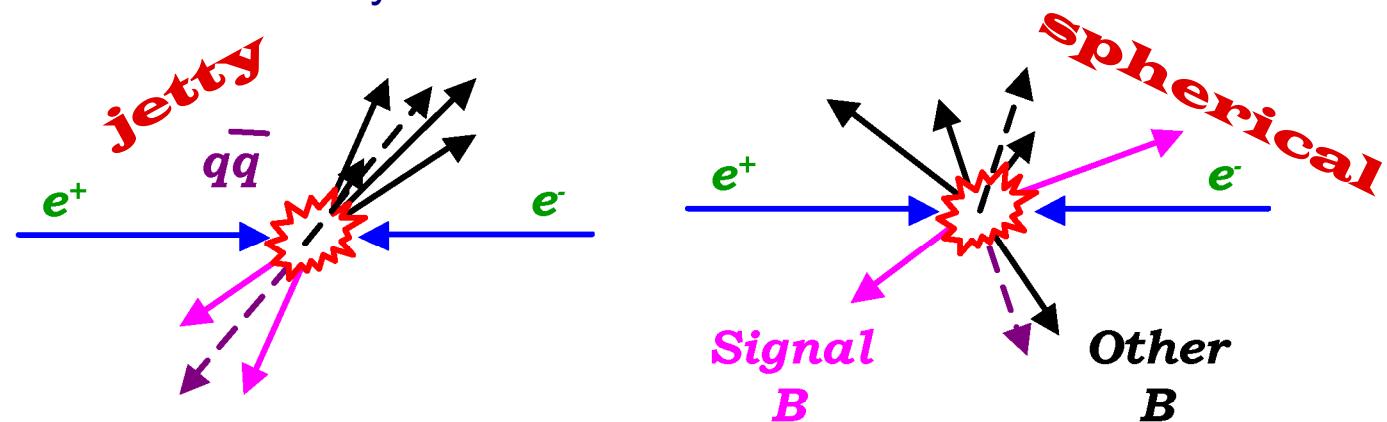


**continuum background in the Grand Side Band**



# Common discriminating variables: event shape

- The principal source of background to rare  $B$  decays: random track/neutral combinations from quark-pair ( $udsc$ ) production in the continuum:
  - total  $udsc$  cross section  $\sim 3.4$  nb, compared to  $\sim 1.1$  nb for  $\Upsilon(4S)$
  - $udsc$  events have jet-like topology, while  $B$  decays are nearly spherical in CM
  - several topological variables are employed to suppress this background
- Backgrounds from  $\tau^+\tau^-$  production and two-photon physics are usually negligible
- Backgrounds from other  $B$  decays tend to be small



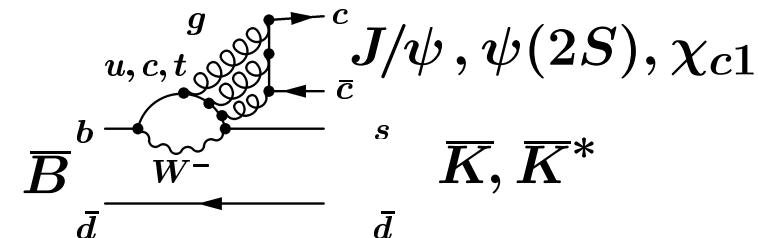
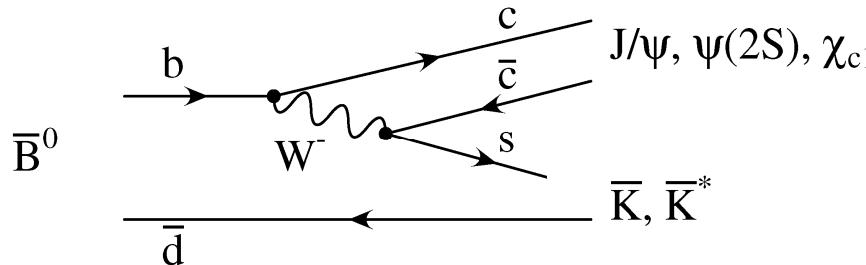
Analyses are blind until the methodology has been finalized and frozen

# $\sin 2\beta$ in “golden” $b \rightarrow c\bar{c}s$ modes:



The highest-precision test of the KM mechanism of  $CP$  violation in meson decays

Golden-mode branching fractions are  $O(10^{-3})$



“Golden” modes: color-suppressed tree dominates; the  $t$ -quark penguin has the same weak phase as the tree (none). In Standard Model, therefore,

$$S_{\text{golden}} = \eta_{CP} \times \sin 2\beta, \quad C_{\text{golden}} = 0 \quad (\eta_{CP} = \pm 1)$$

Theoretical uncertainties:

- an example of a model-independent, data-driven calculation:  
assuming  $SU(3)_{\text{flavor}}$  invariance, use  $B^0 \rightarrow J/\psi \pi^0$  data to constrain penguin pollution in  $J/\psi K^0 \Rightarrow \Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta = 0.000 \pm 0.012$

M. Ciuchini, M. Pierini, L. Silvestrini,  
Phys. Rev. Lett. **95**, 221804 (2005)

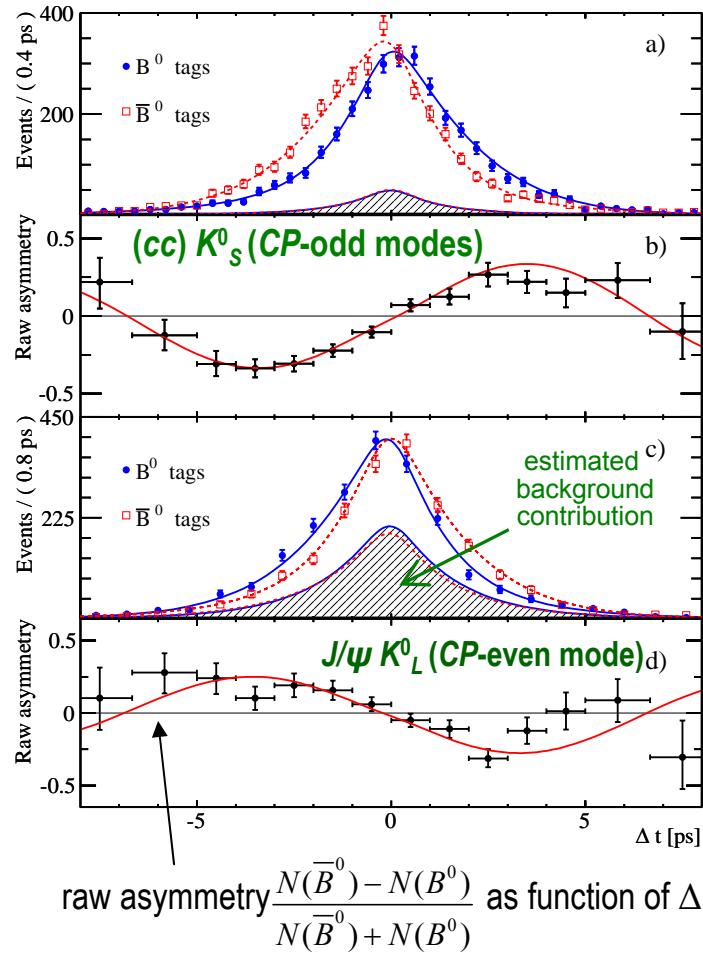
- theoretical estimates of the biases due to  $u$ - and  $c$ -quark penguins, etc.:
  - $\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-3})$
  - $\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-4})$

H. Li, S. Mishima, JHEP 0703:009 (2007) [hep-ph/0610120]

H. Boos et al., Phys. Rev. D **73**, 036006 (2006)

# Latest on $\sin 2\beta$ in “golden” modes

CP Violation in  $B$  mesons first observed here, in 2001



*BaBar* with  $384 \times 10^6 BB$  pairs: PRL 99, 171803 (2007)

$$\sin 2\beta = 0.714 \pm 0.032 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

$J/\psi K_s (\pi^+ \pi^-)$	$0.702 \pm 0.042 \pm 0.020$
$J/\psi K_s (\pi^0 \pi^0)$	$0.617 \pm 0.103 \pm 0.036$
$\psi(2S) K_s$	$0.947 \pm 0.112 \pm 0.062$
$\chi_{c1} K_s$	$0.759 \pm 0.170 \pm 0.037$
$\eta_c K_s$	$0.778 \pm 0.195 \pm 0.093$
$J/\psi K^*$	$0.477 \pm 0.271 \pm 0.155$
$J/\psi K_s$	$0.686 \pm 0.039 \pm 0.015$
$J/\psi K_L$	$0.735 \pm 0.074 \pm 0.067$
$J/\psi K^0$	$0.697 \pm 0.035 \pm 0.016$
All	$0.714 \pm 0.032 \pm 0.018$

CP violation in Standard Model is not small, it is  $O(1)$ .  
 Smallness of CPV in kaon decays is due to flavor suppression.  
 CP-violating phases in New Physics can also be  $O(1)$ .

*Belle* with  $535 \times 10^6 BB$  pairs: PRL 98, 031802 (2007)

$$\sin 2\beta = 0.642 \pm 0.031 \text{ (stat)} \pm 0.017 \text{ (syst)}$$

# Decays dominated by gluonic penguins:

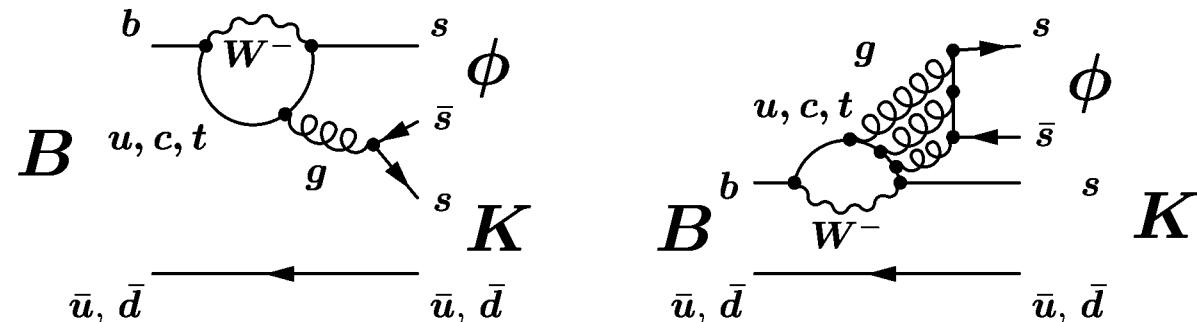
$B^0 \rightarrow \eta' K^0, \varphi K^0, K^+ K^- K_S, K_S \pi^0, K_S K_S K_S, \omega K_S, f_0 K_S, \text{etc.}$



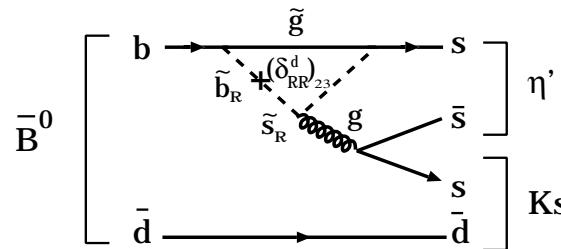
For example, consider

$B^0 \rightarrow \varphi K^0$  or  $K_S K_S K_S$

$$b \rightarrow S\bar{S}S$$



- Tree-level SM contributions are absent
- All other SM contributions are strongly suppressed
- SM penguins dominated by top-quark loops
  - ⇒ in SM, direct  $CP$  violation is small, ~1%
  - ⇒ and time-dependent  $CP$  violation is the same as in the “golden” charmonium- $K^0$  modes
- Great sensitivity to non-SM physics in the loops!



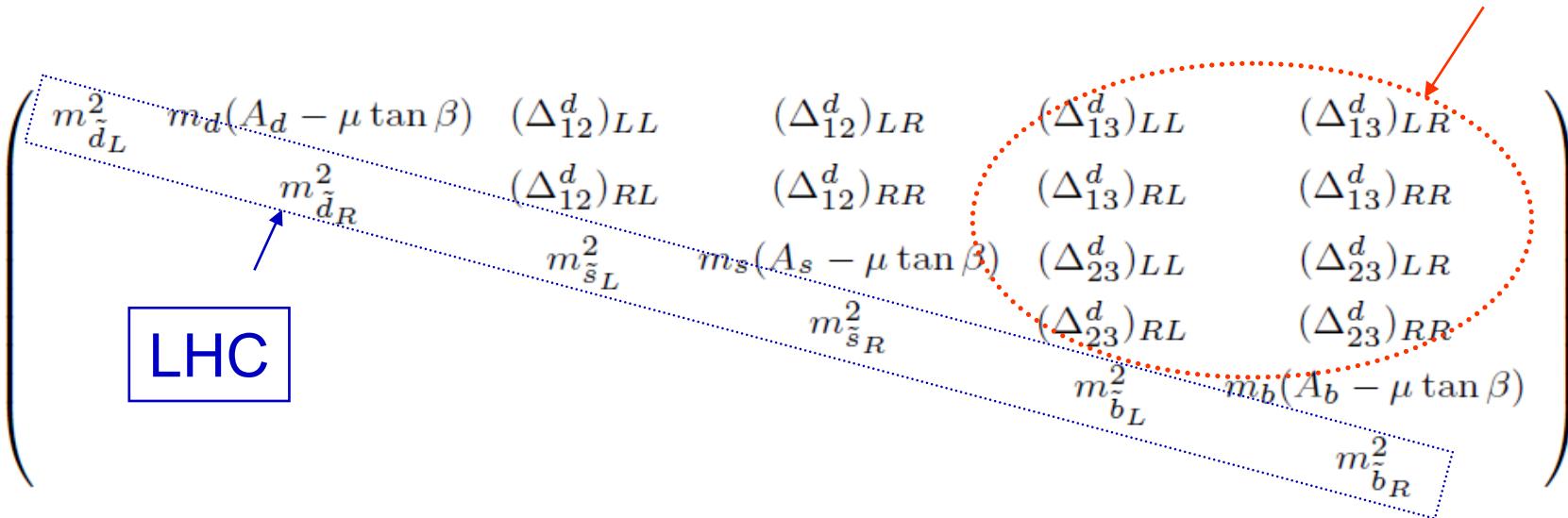
It is not easy for New Physics to hide in penguin-dominated decays unless its flavor and/or mass structure is very special



# Decays dominated by gluonic penguins: Indirect limits on squark mixing



## B-meson factories



Complementarity with the LHC is part of the physics case for a “Super B Factory”

New Physics near the electroweak scale (i.e., accessible at the LHC) that has a generic flavor-violation structure is ruled out by  $K^0\bar{K}^0$ ,  $B^0\bar{B}^0$ ,  $B_s^0\bar{B}_s^0$  mixing and  $b\rightarrow s\gamma$ ,  $b\rightarrow sg$  measurements (“*the New Physics flavor problem*”). Flavor-blind New Physics is unnatural because Standard Model contains flavor violation in the Yukawa couplings. For supersymmetry, a solution is Minimal Flavor Violation, possibly with SM-like loop suppression

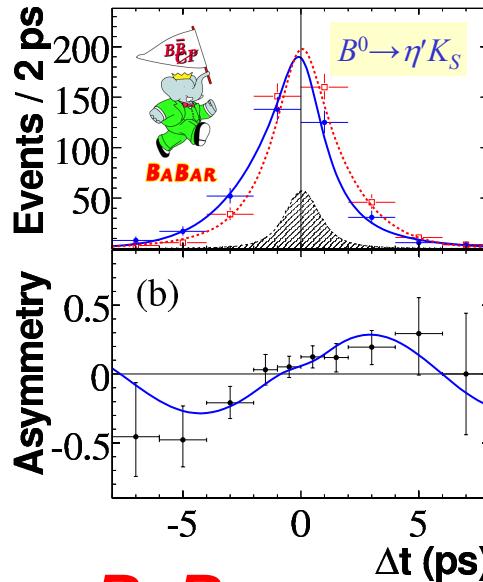


# The highest-statistics penguin-dominated mode:

$$B^0 \rightarrow \eta' K_S$$



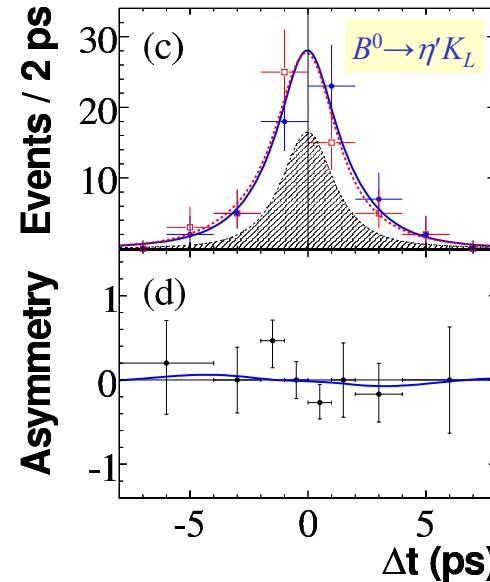
Back-to-back:  
 BaBar: Phys.Rev.Lett. **98** (2007) 031801  
 Belle: Phys.Rev.Lett. **98** (2007) 031802



**BaBar**

$$S_{\eta' K^0} = +0.58 \pm 0.10 \pm 0.03 \quad (5.5\sigma)$$

$$C_{\eta' K^0} = -0.16 \pm 0.07 \pm 0.03$$



**Belle**

$$S_{\eta' K^0} = +0.64 \pm 0.10 \pm 0.04 \quad (5.6\sigma)$$

$$C_{\eta' K^0} = +0.01 \pm 0.07 \pm 0.05$$

Measurements of  $S$  in  $B^0 \rightarrow \eta' K^0$  by *BaBar* and then *Belle* are the **second** observations of  $CP$  violation in  $B$  mesons (Fall 2006)

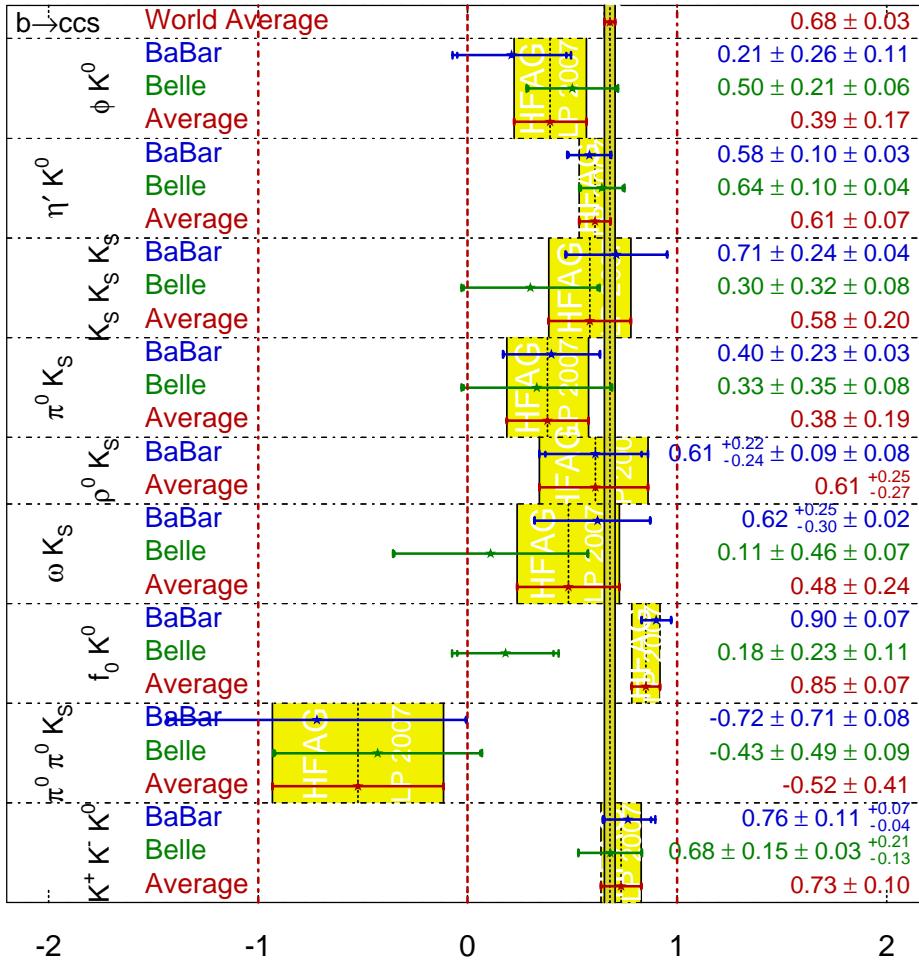
# The world-average $\sin 2\beta$ in penguin modes is $2.2\sigma$ less than in the “golden” modes

In 2004, the difference was  $3.7\sigma$ ...



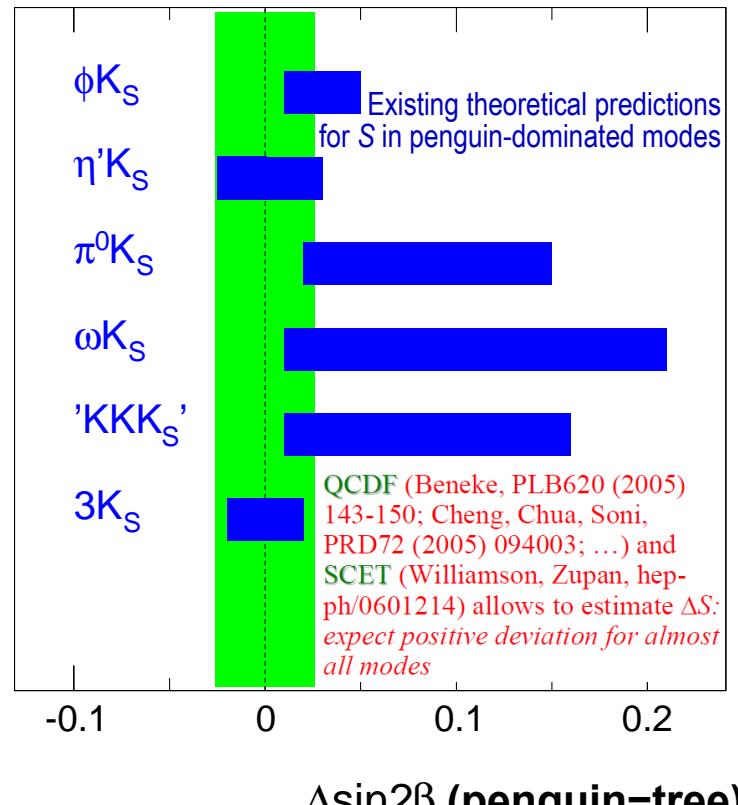
$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFAG  
LP 2007  
PRELIMINARY



This is a very naive average

$$\langle \sin 2\beta_{\text{golden}} \rangle = 0.680 \pm 0.025$$

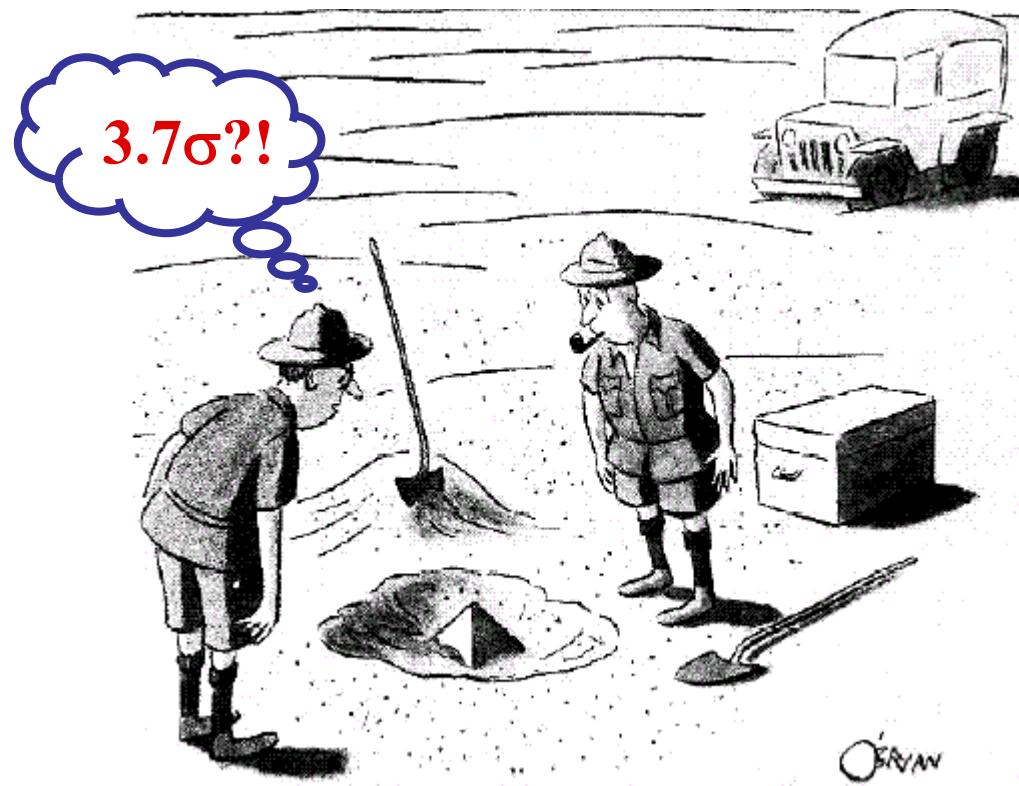


$$\langle \sin 2\beta_{\text{peng}} \rangle_{\text{naive}} = 0.56 \pm 0.05 (\chi^2 = 19/16 \text{ dof})$$

<http://www.slac.stanford.edu/xorg/hfag/triangle/summer2007/index.shtml>



# What do we make of this discrepancy?



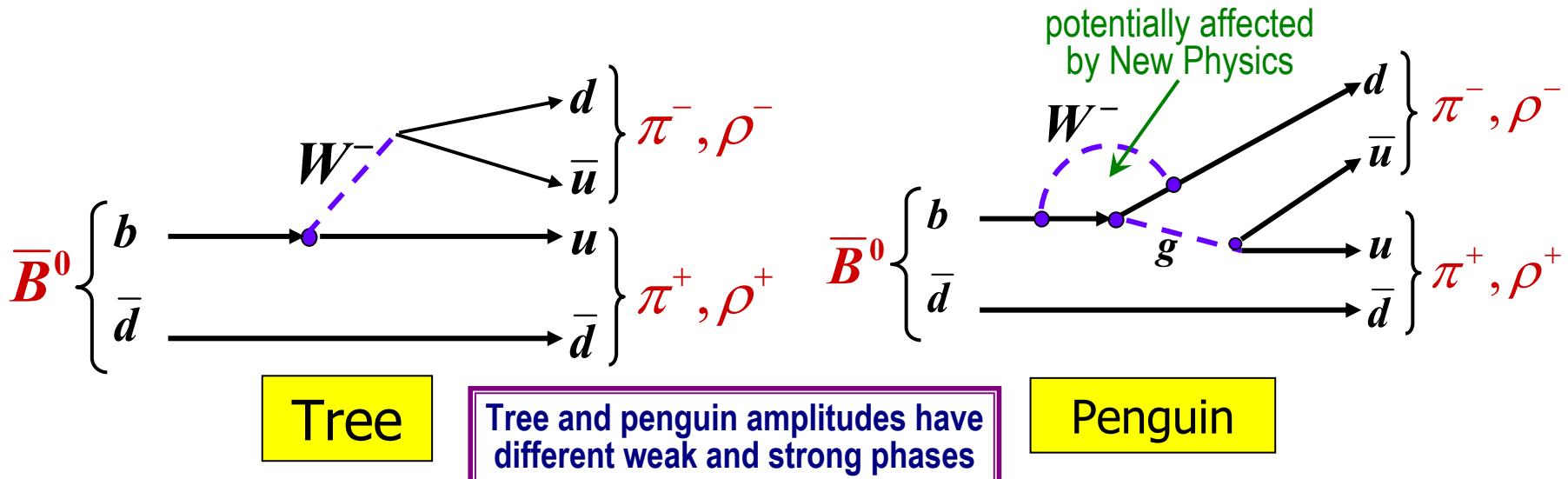
*"This could be the greatest discovery of the century.  
Depending, of course, on how far down it goes..."*

# Measuring $\alpha$

$\mathcal{A}_{CP}(t)$  in  $b \rightarrow u\bar{u}d$  decay to a  $CP$  eigenstate at the tree level:

Measure  $180^\circ - \beta - \gamma = \alpha \equiv \arg \left[ \frac{-V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right]$  (in SM)

**Penguins:**  $\mathcal{A}_{CP}(t) \Rightarrow \sin(2\alpha_{\text{eff}})$ ;  $\alpha_{\text{eff}} = \alpha - \Delta\alpha$ ; direct  $\mathcal{A}_{CP} \neq 0$



# SU(2) isospin analysis in $B \rightarrow \pi\pi, \rho\rho$

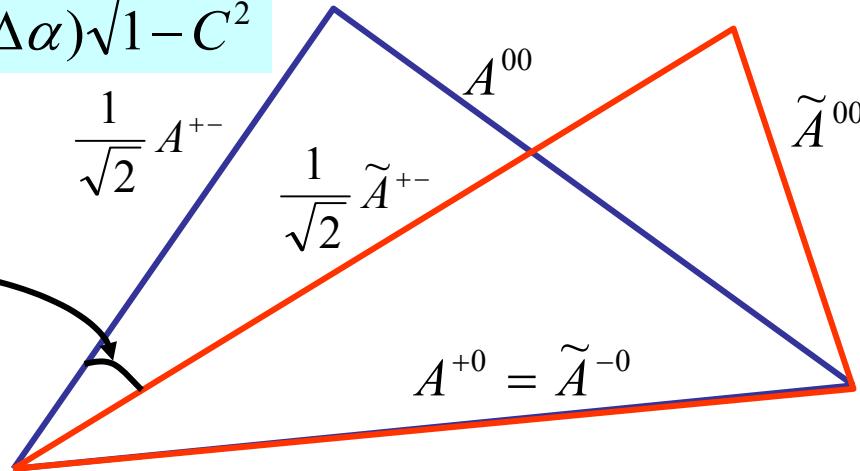


Determines relative phase between  $B^0$  mixing and the tree, independent of the EW model

M. Gronau, D. London, Phys. Rev. Lett. **65**, 3381 (1990)

$$S = \sin(2\alpha + 2\Delta\alpha)\sqrt{1 - C^2}$$

$2\Delta\alpha$



In  $B \rightarrow \rho\rho$ , there are 3 such relations (one for each polarization)

6 unknowns, 6 observables in  $\pi\pi$  (there is no vertex to measure  $S_{\pi^0\pi^0}$ )

5 observables in  $\rho\rho$  (or 7, when both  $C_{\rho^0\rho^0}$  and  $S_{\rho^0\rho^0}$  are measured)

4-fold ambiguity in  $2\Delta\alpha$ : either triangle can flip up or down

$$A_{hh} = e^{+i\gamma} T + e^{-i\beta} P$$

Neglecting EW penguins,  $\pm 0$  is a pure tree mode, and so the two triangles share a common side:

$$\tilde{A}_{hh} = e^{-i\gamma} T + e^{+i\beta} P$$

$$A(B^+ \rightarrow h^+ h^0) = \tilde{A}(B^- \rightarrow h^- h^0)$$

$A^{+-} = A(B^0 \rightarrow \pi^+ \pi^-)$
$\tilde{A}^{+-} = A(\bar{B}^0 \rightarrow \pi^+ \pi^-)$
$A^{00} = A(B^0 \rightarrow \pi^0 \pi^0)$
$\tilde{A}^{00} = A(\bar{B}^0 \rightarrow \pi^0 \pi^0)$
$A^{+0} = A(B^+ \rightarrow \pi^+ \pi^0)$
$\tilde{A}^{-0} = A(B^- \rightarrow \pi^- \pi^0)$

$$A^{+0} = \frac{1}{\sqrt{2}} A^{+-} + A^{00}$$

$$\tilde{A}^{-0} = \frac{1}{\sqrt{2}} \tilde{A}^{+-} + \tilde{A}^{00}$$

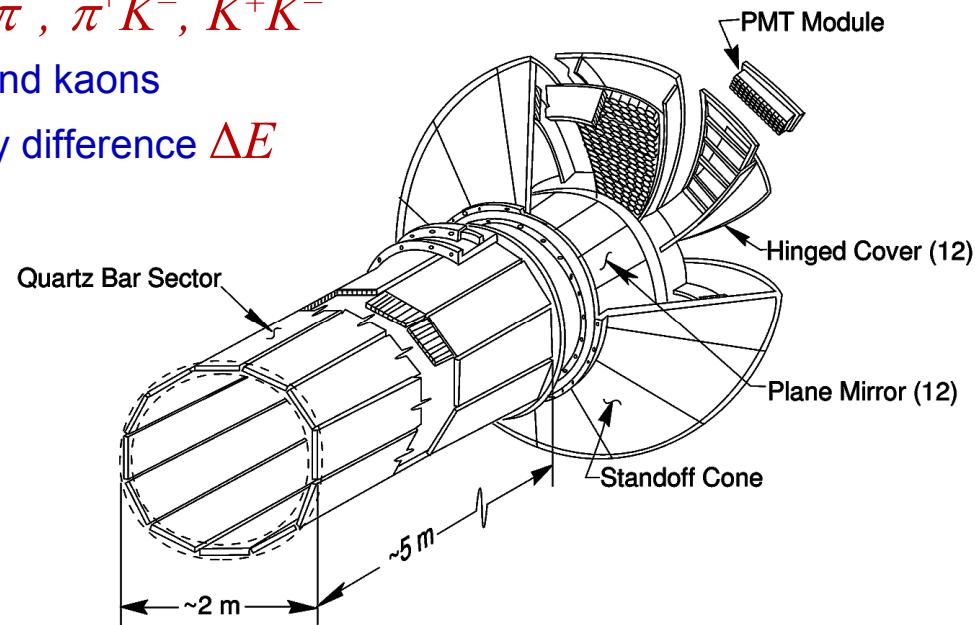
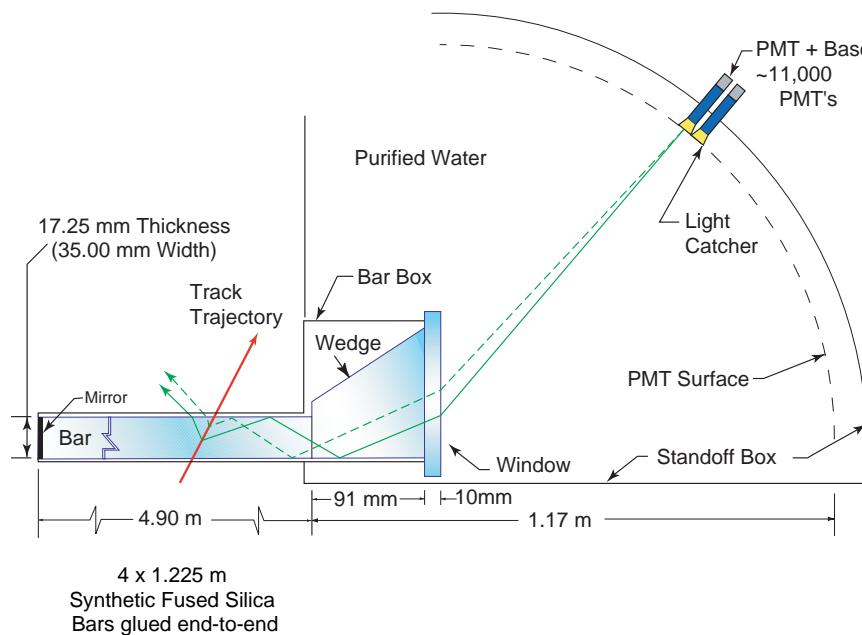
Knowledge of  $A^{00}$  is the primary limiting factor in the isospin analysis

# The “classic” $B^0 \rightarrow h^+h^-$ analysis

**Simultaneous ML fit to  $B^0 \rightarrow \pi^+\pi^-, K^+\pi^-, \pi^+K^-, K^+K^-$**

Using DIRC Cherenkov angle to identify pions and kaons

Additional  $\pi\pi/K\pi/KK$  separation from energy difference  $\Delta E$



**DIRC:** 144 quartz bars  
 $0.84 \times 4\pi$  coverage; 91% eff. with  $n_\gamma > 5$   
 $13\sigma$   $\pi/K$  separation at 1.5 GeV/c, 2.5 $\sigma$  at 4.5 GeV/c  
 Calibration sample:  $B^- \rightarrow \pi^- D^0$ ,  $D^0 \rightarrow \pi^+ K^-$



# $\pi/K$ separation with DCH $dE/dx$ :

Catching up with Belle's  $B^0 \rightarrow h^+h^-$  reconstruction efficiency



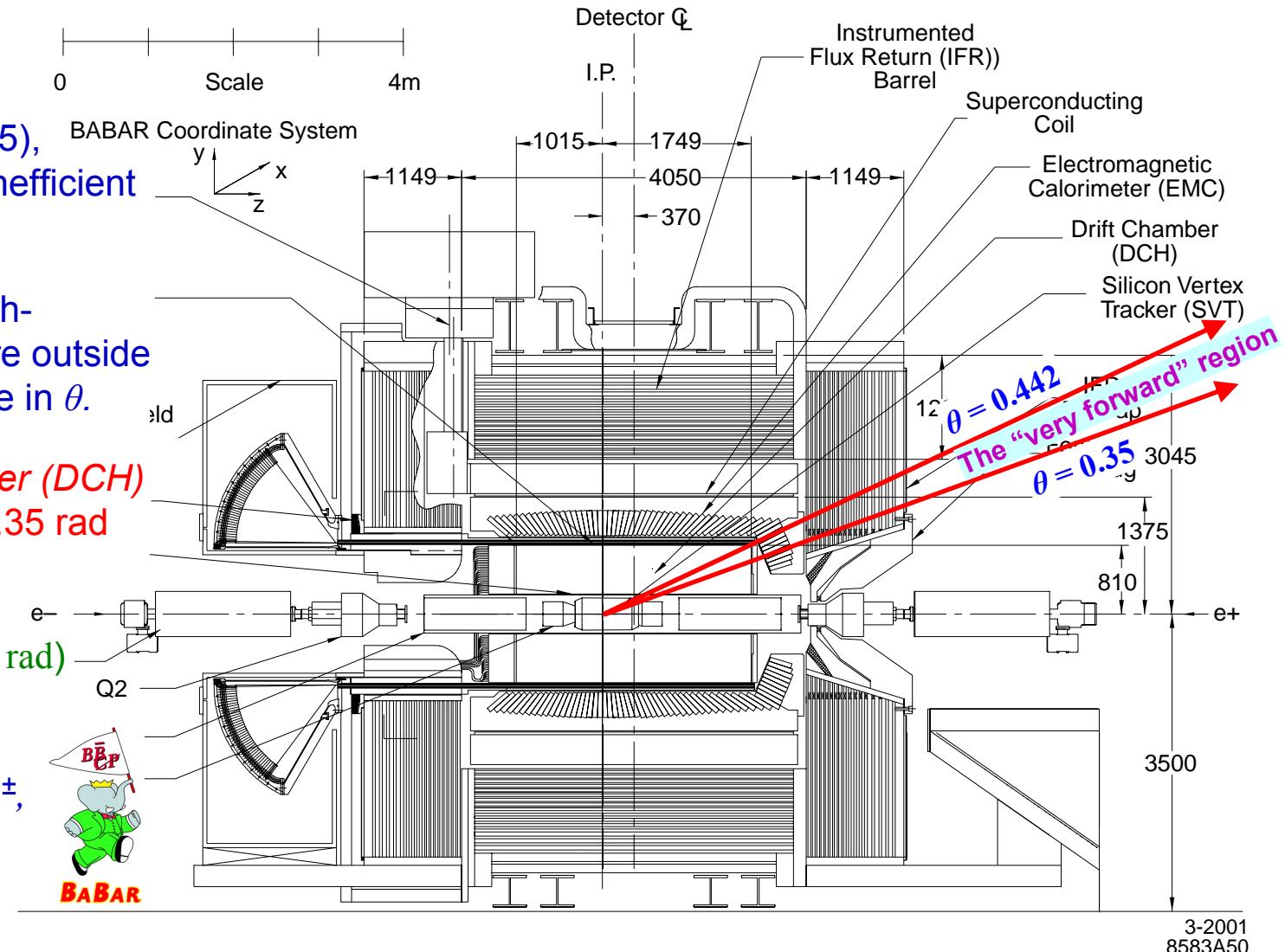
In the barrel ( $\theta > 0.445$ ),  
the DIRC is  $\sim 9.3\%$  inefficient  
( $\phi$  cracks, etc.)

Another  $\sim 12\%$  of high-momentum tracks are outside  
the DIRC acceptance in  $\theta$ .

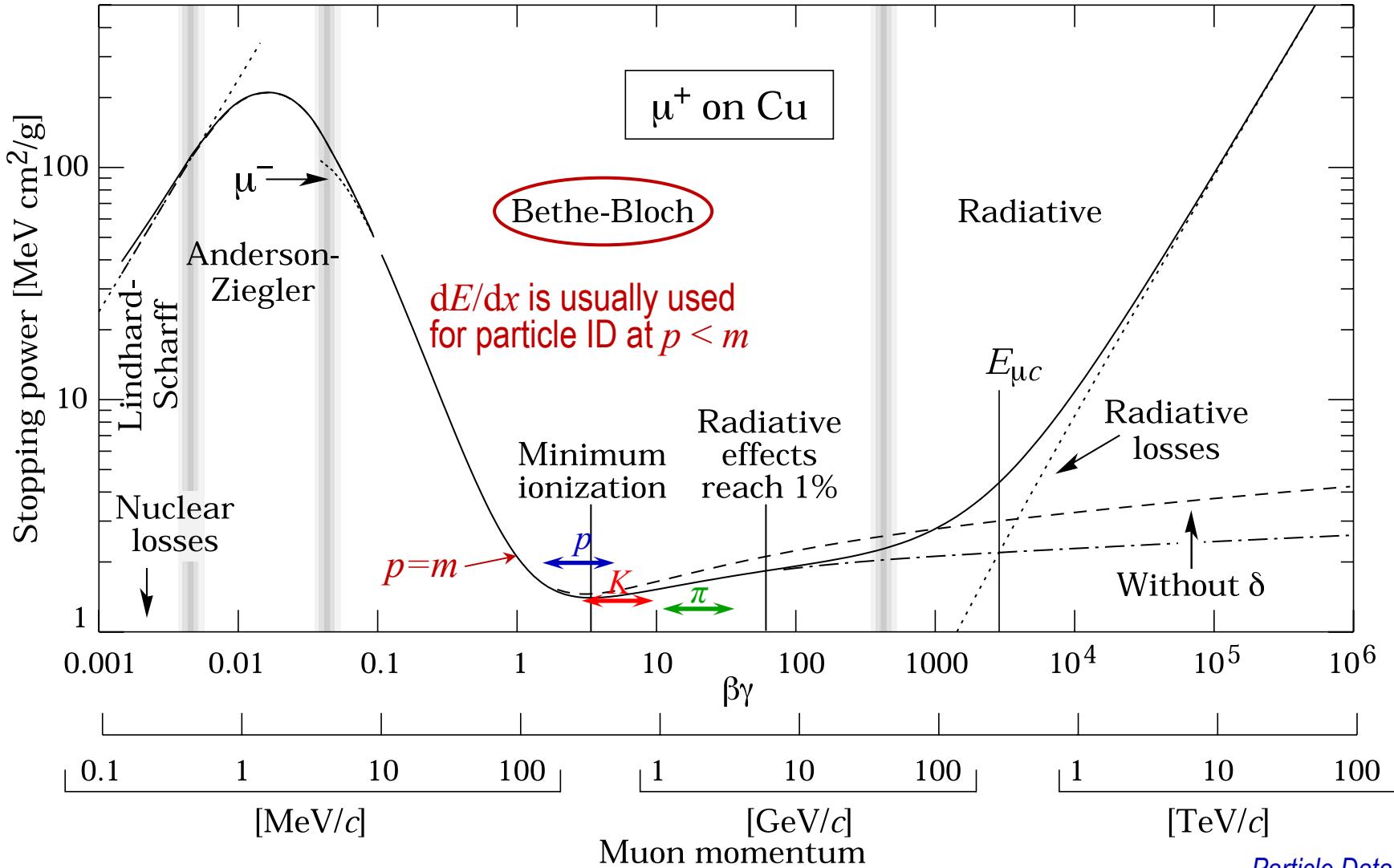
We use Drift Chamber (DCH)  
tracks down to  $\theta = 0.35$  rad

$(J/\psi \rightarrow \mu^+\mu^-)$  in  $\sin 2\beta$   
analysis: down to 0.30 rad)

→ 16% event-yield  
increase for  $B \rightarrow Xh^\pm$ ,  
35% for  $B^0 \rightarrow h^+h^-$



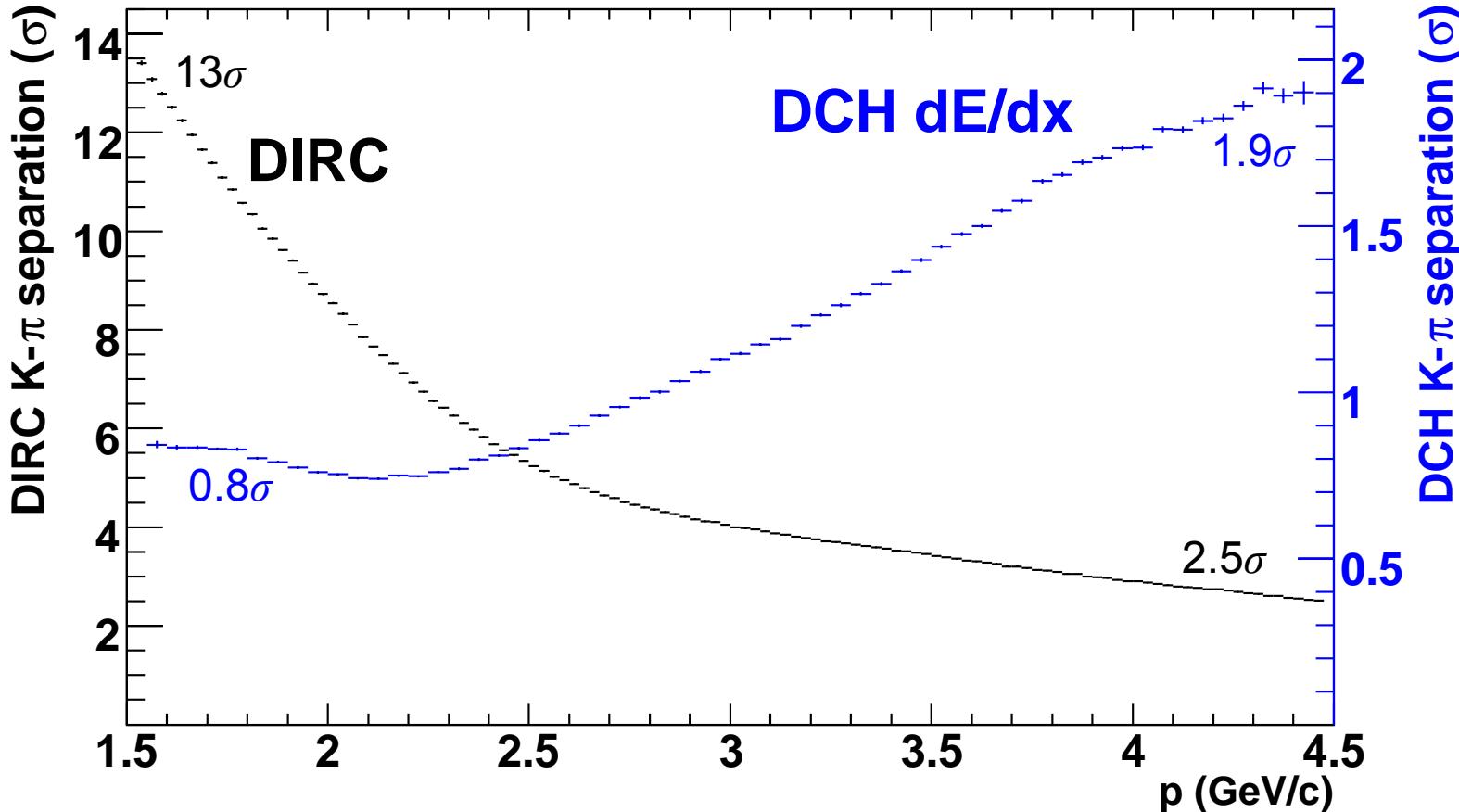
# Ionization energy loss for $B \rightarrow X h^\pm$ momenta



Particle Data Group

# DCH $dE/dx$ $K\text{-}\pi$ separation in $B \rightarrow X h^\pm$

complementary to DIRC



(for tracks that have good DIRC information, we use both DIRC and  $dE/dx$ )

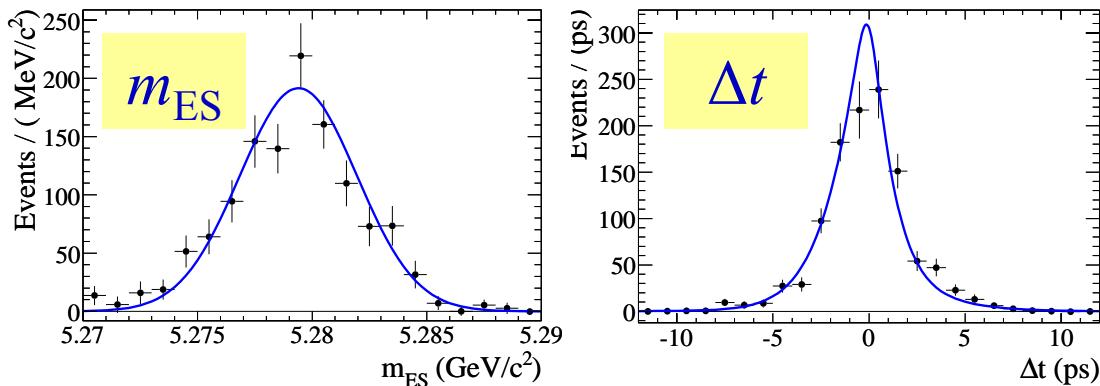
# Our new result: $B^0 \rightarrow \pi^+ \pi^-$



$$N_{\pi^+ \pi^-} = 1139 \pm 49$$

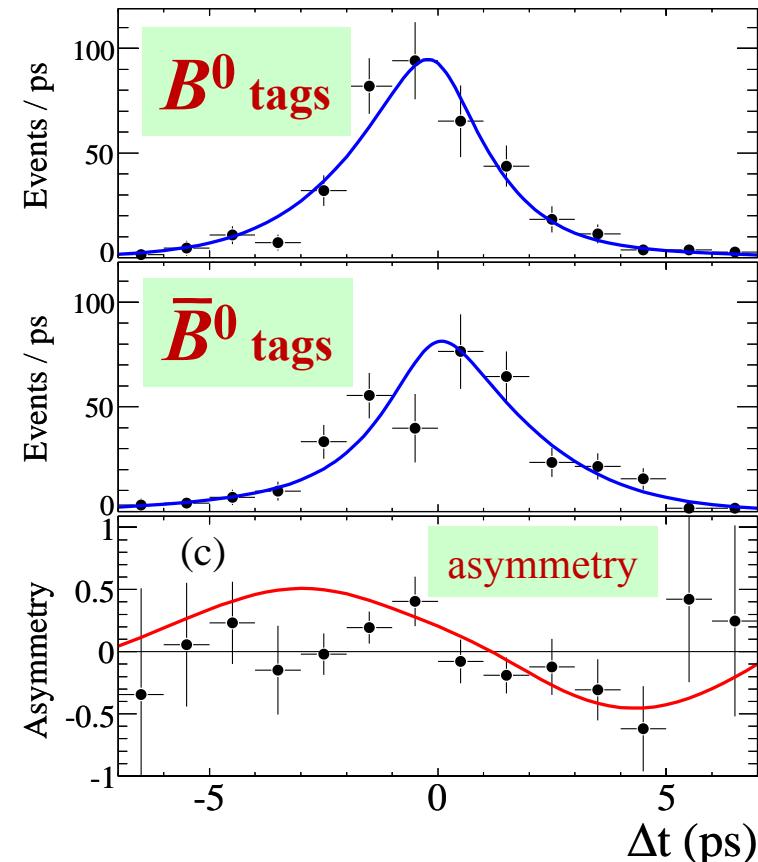
**52% overall increase  
in signal reconstruction efficiency:**

35% from DCH  $dE/dx$ ,  
13% mainly from reoptimizing the event-shape  $|\cos\theta_{\text{spher}}|$  cut



Builds a histogram of  $x$  excluding it from the Maximum-Likelihood fit, assigning a weight to each event, keeping all signal events, getting rid of all background events, and keeping track of the statistical errors in each  $x$  bin

*sPlot:*



M. Pivk and F. R. Le Diberder,  
*"sPlot: a statistical tool to unfold data distributions,"*  
*Nucl. Instrum. Meth. A 555, 356 (2005)*  
*[arXiv:physics/0402083]*

Observation of  $CP$  Violation in  $B^0 \rightarrow K^+ \pi^-$  and  $B^0 \rightarrow \pi^+ \pi^-$ 

**BaBar has made a  $5.4\sigma$  observation of  $CP$  violation in  $B^0 \rightarrow \pi^+ \pi^-$**

$$S_{\pi\pi} = -0.60 \pm 0.11 \pm 0.03 \quad (5.1\sigma)$$

$$C_{\pi\pi} = -0.21 \pm 0.09 \pm 0.02 \quad (2.3\sigma)$$

BaBar: 383 million  $B\bar{B}$  pairs,  $1139 \pm 49 \pi^+ \pi^-$

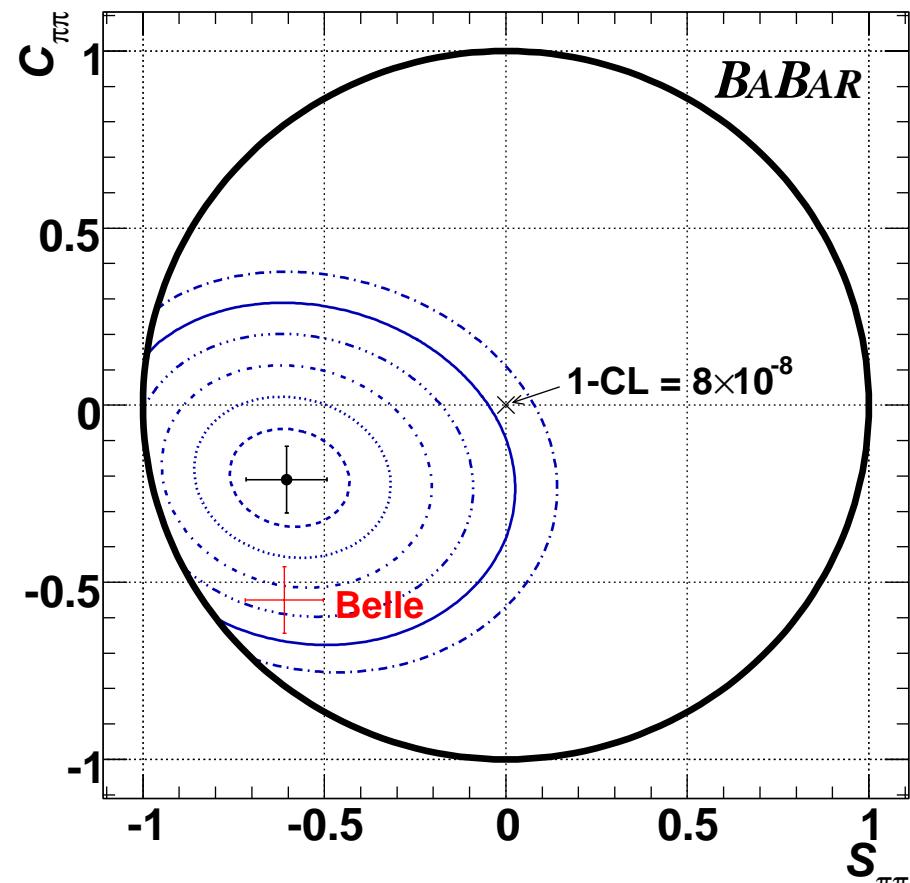
Belle: 535 million  $B\bar{B}$  pairs,  $1464 \pm 65 \pi^+ \pi^-$

Belle

PRL 98, 211801 (2007)

$$S_{\pi\pi} = -0.61 \pm 0.10 \pm 0.04 \quad (5.3\sigma)$$

$$C_{\pi\pi} = -0.55 \pm 0.08 \pm 0.05 \quad (5.5\sigma)$$



also:

$$\mathcal{A}_{K^+ \pi^-} = -0.107 \pm 0.018 {}^{+0.007}_{-0.004} \quad (5.5\sigma)$$

# The $B \rightarrow \pi^\pm \pi^0, \pi^0 \pi^0$ analysis

Simultaneous fit to  $B^0 \rightarrow \pi^+ \pi^0, K^+ \pi^0$  (using DIRC Cherenkov angle to separate pions and kaons)  
 $B^0 \rightarrow \pi^0 \pi^0$ : branching fraction and time-integrated direct  $CP$  asymmetry

**new:** in addition to  $\pi^0 \rightarrow \gamma\gamma$ , we use merged  $\pi^0$  and  $\gamma \rightarrow e^+e^-$  conversions  
 $\Rightarrow 10\% \text{ efficiency increase per } \pi^0$  (4% from merged  $\pi^0$ , 6% from  $\gamma$  conversions)

At a Super  $B$ -meson factory,  $\gamma \rightarrow e^+e^-$  conversions would make  $S_{\pi^0 \pi^0}$  determination possible!

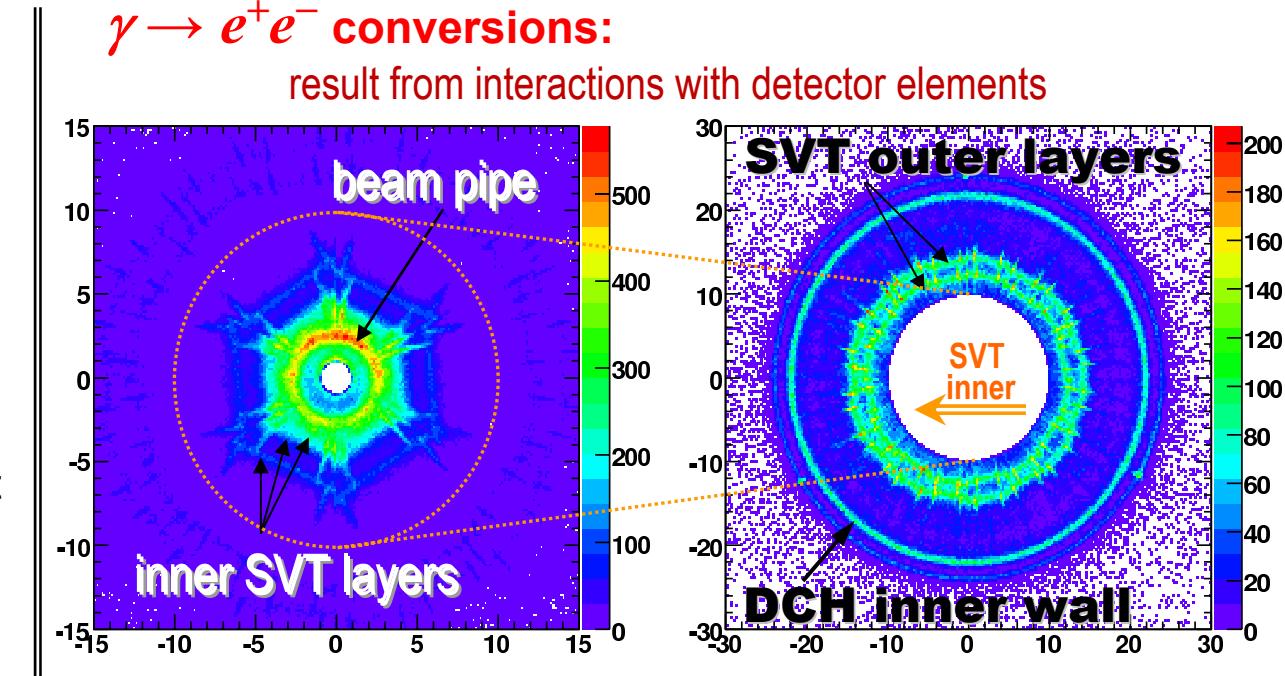
## merged $\pi^0$ :

the two photons are too close to one another in the calorimeter to be reconstructed individually; can be recovered using

$$M_{\pi^0}^2 \approx E_{\pi^0}^2 (S_{\pi^0} - S_\gamma),$$

where  $S$  is the second EMC moment of the merged  $\pi^0 \rightarrow \gamma\gamma$

The control sample:  $\tau \rightarrow \rho\nu$



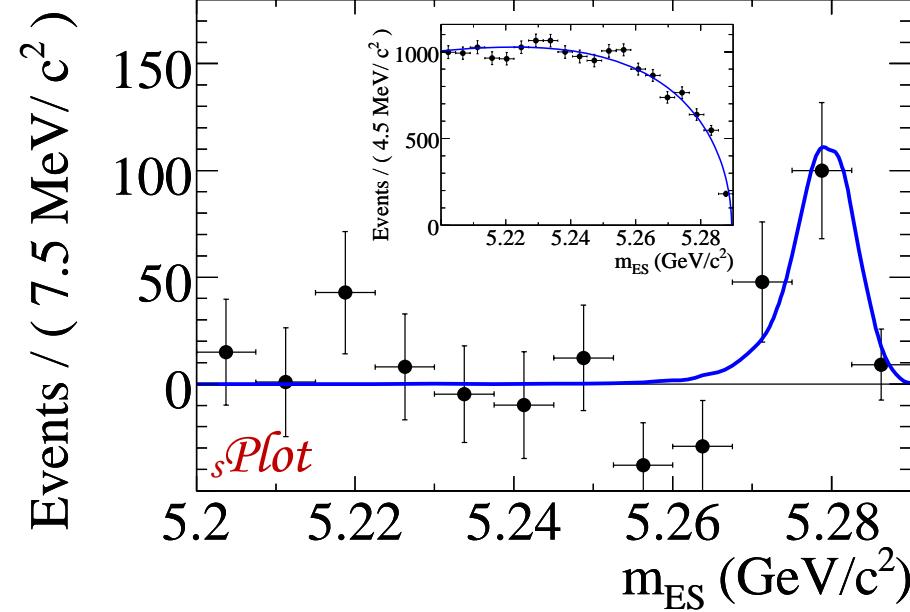
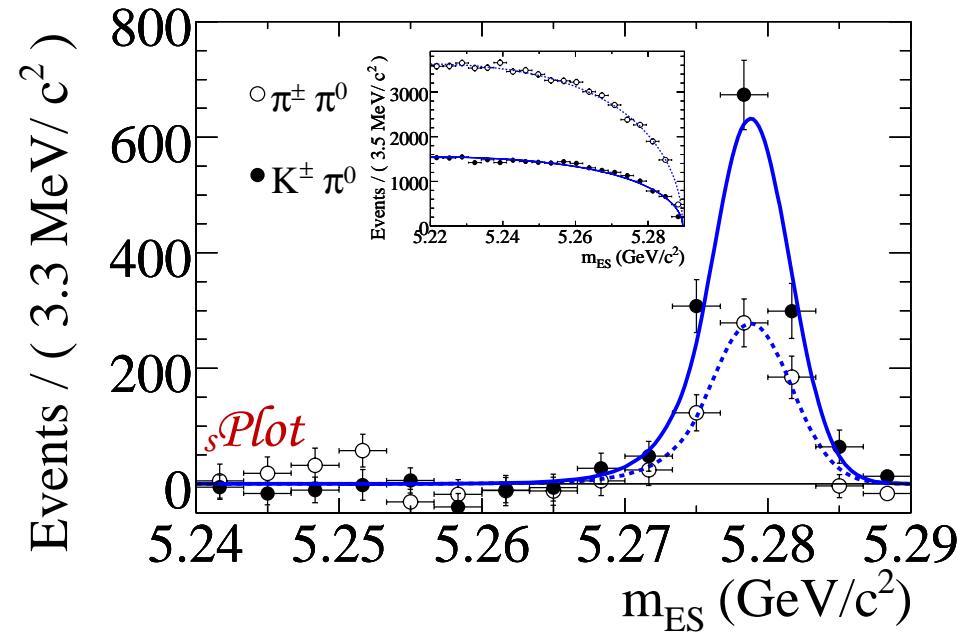
# New BaBar results: $B \rightarrow \pi^\pm \pi^0, \pi^0 \pi^0$



$383 \times 10^6 BB$  pairs

PRD 76, 091102 (2007)

$$N_{\pi^\pm \pi^0} = 627 \pm 58$$



$$\mathcal{Br}_{\pi^\pm \pi^0} = (5.02 \pm 0.46 \pm 0.29) \times 10^{-6}$$

$$\mathcal{Br}_{\pi^0 \pi^0} = (1.47 \pm 0.25 \pm 0.12) \times 10^{-6}$$

$$\mathcal{A}_{\pi^\pm \pi^0} = 0.03 \pm 0.08 \pm 0.01$$

$$C_{\pi^0 \pi^0} = -0.49 \pm 0.35 \pm 0.05$$



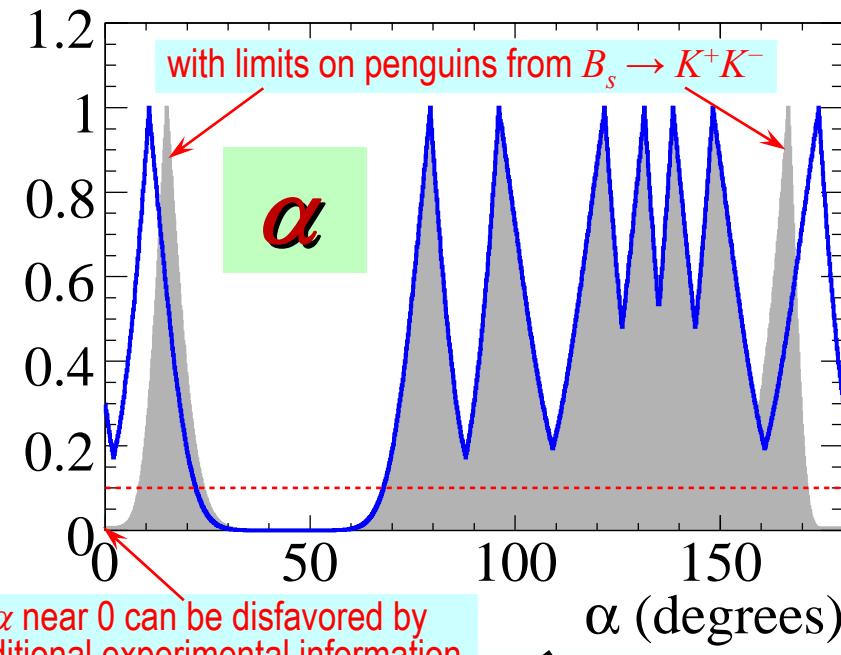
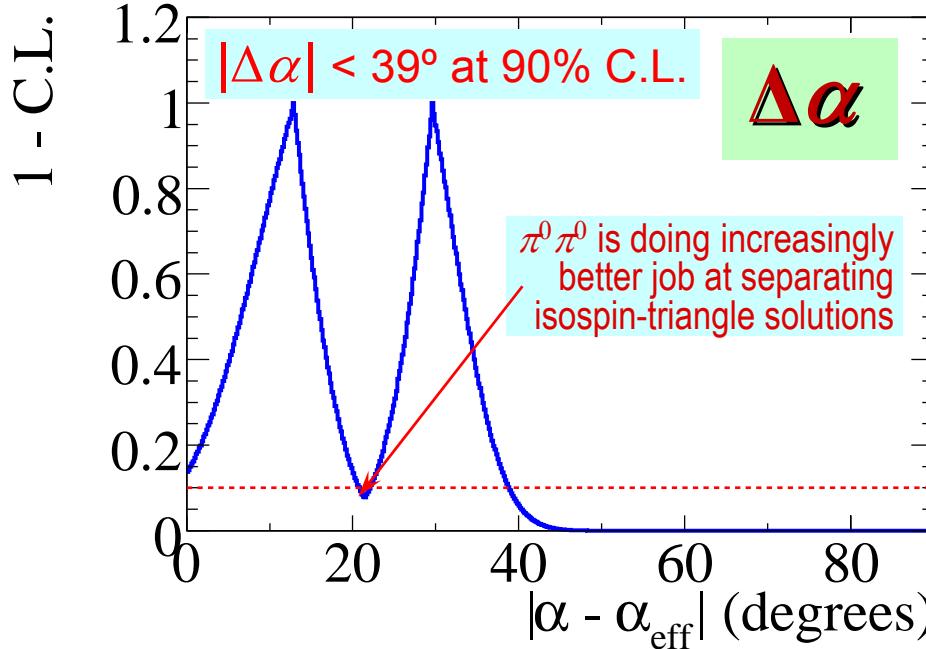
# An interpretation of our new $B \rightarrow \pi\pi$ results



**BABAR**

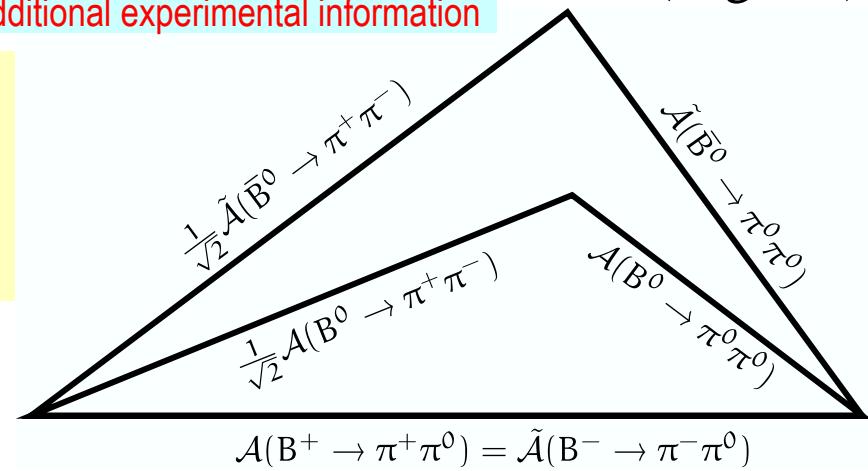
383x10<sup>6</sup> BB pairs

PRD 76, 091102 (2007)



This is a frequentist interpretation: we use only the  $B \rightarrow \pi\pi$  isospin-triangle relations in arriving at these constraints on  $\Delta\alpha = \alpha - \alpha_{\text{eff}}$  and on  $\alpha$  itself

Here is one of the possible solutions to the Gronau-London isospin triangle in  $B \rightarrow \pi\pi$  according to the central values of the Summer 2006 BaBar results:



# $B \rightarrow \rho\rho$ angular analysis

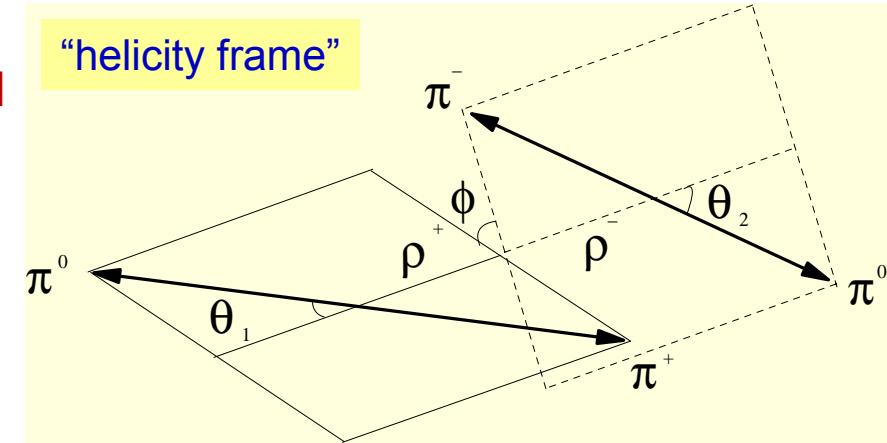
$B \rightarrow \rho\rho$  is a vector-vector state; angular analysis is required to determine  $CP$  content:

Longitudinal:  $A_0 = -\frac{1}{\sqrt{3}}S + \sqrt{\frac{2}{3}}D$  pure  $CP = +1$

Transverse  $A_{+1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D + \frac{1}{\sqrt{2}}P$

Transverse  $A_{-1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D - \frac{1}{\sqrt{2}}P$

transverse  
is not a  $CP$   
eigenstate



Fortunately, the fraction  $f_L$  of the helicity-zero state in  $B \rightarrow \rho\rho$  decays is very close to 1:

$$f_L(B^0 \rightarrow \rho^+ \rho^-)_{\text{WA}} = 0.978^{+0.025}_{-0.022}$$

$$f_L(B^\pm \rightarrow \rho^\pm \rho^0)_{\text{WA}} = 0.912^{+0.044}_{-0.045}$$

# New BaBar result:

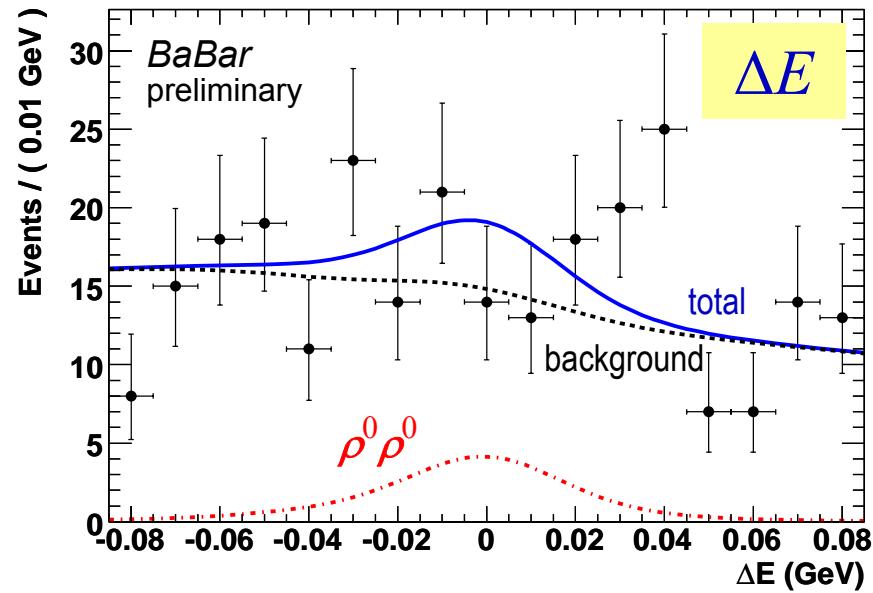
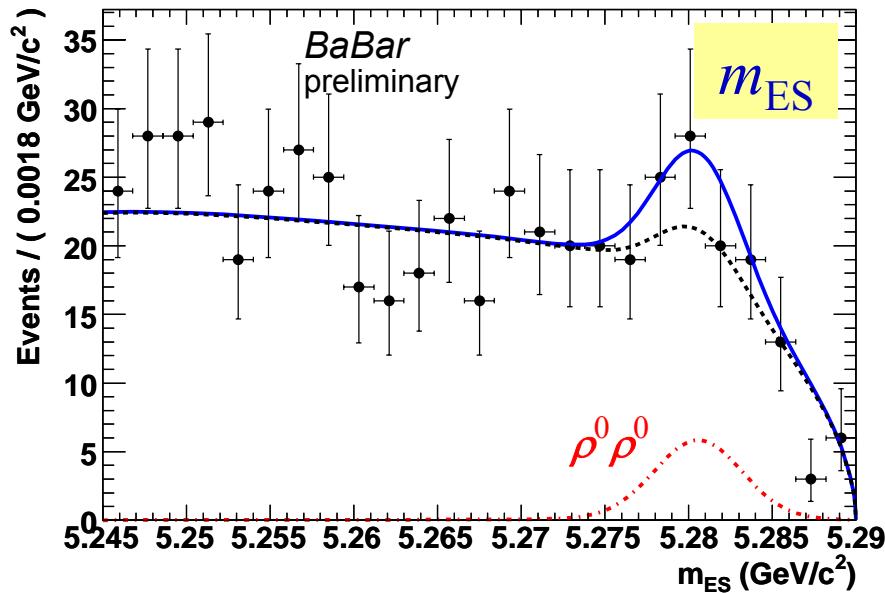
**3.6 $\sigma$  evidence for  $B^0 \rightarrow \rho^0 \rho^0$**

427x10<sup>6</sup> BB pairs  
BaBar-CONF-07/012



$$N_{\rho^0 \rho^0} = 85 \pm 28 \pm 17$$

A time-dependent analysis was successfully performed, despite the limited statistics

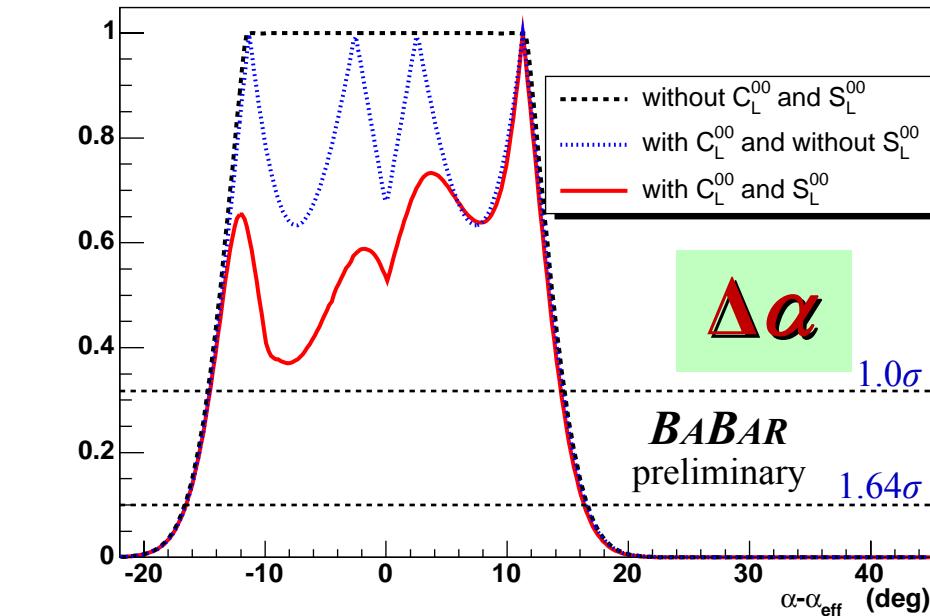
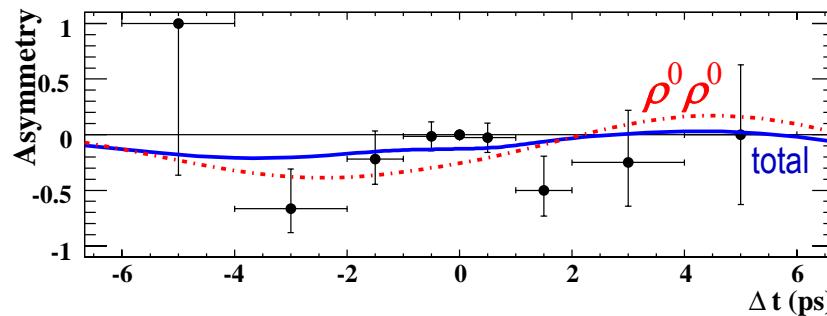
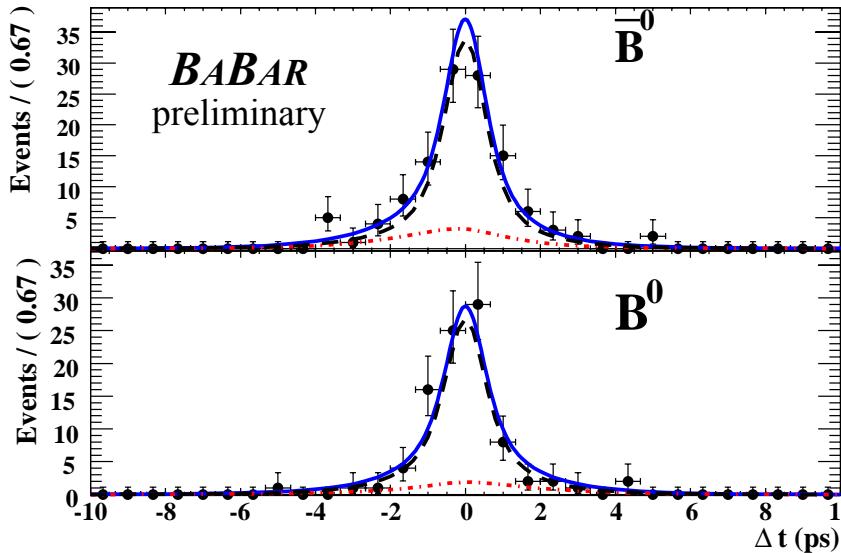


$$\mathcal{Br}_{\rho^0 \rho^0} = (0.84 \pm 0.29 \pm 0.17) \times 10^{-6}$$

$$f_L(B^0 \rightarrow \rho^0 \rho^0) = 0.70 \pm 0.14 \pm 0.05$$

# An interpretation of the new $B \rightarrow \rho\rho$ results

$427 \times 10^6$   $BB$  pairs  
BaBar-CONF-07/012



$$S_{\text{Long}}^{00} = 0.5 \pm 0.9 \pm 0.2$$

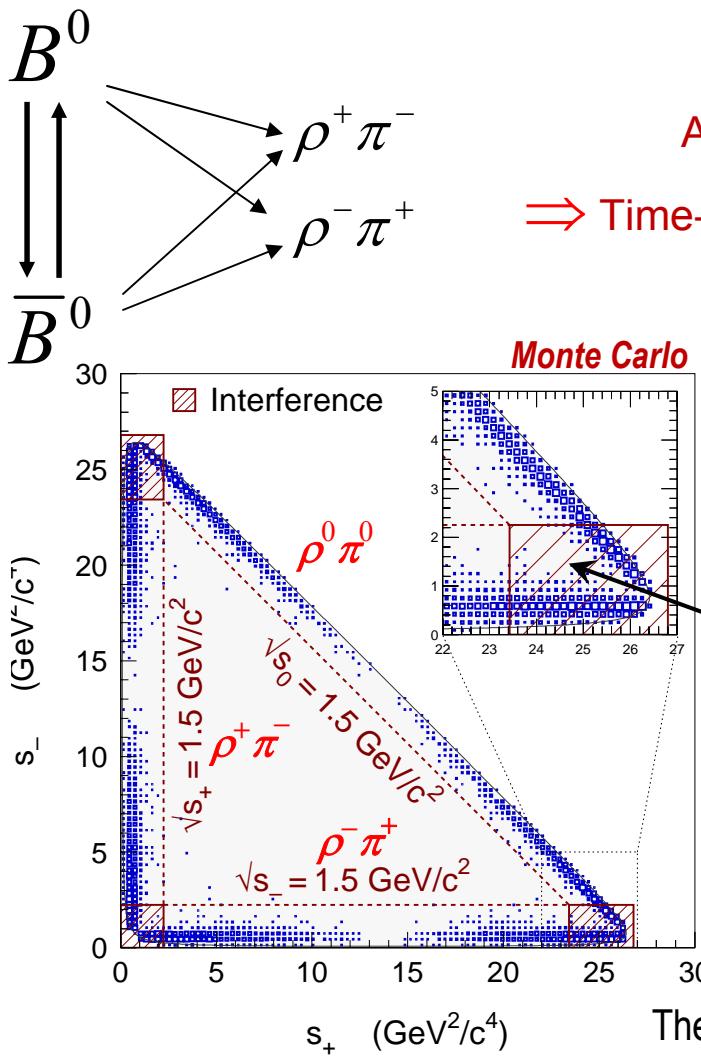
$$C_{\text{Long}}^{00} = 0.4 \pm 0.9 \pm 0.2$$

$|\Delta\alpha| < 14.5^\circ$  at 68% C.L.

$|\Delta\alpha| < 16.5^\circ$  at 90% C.L.

This is a frequentist interpretation: we use only the  $B \rightarrow \rho\rho$  branching fractions, polarization fractions and isospin-triangle relations in arriving at these constraints on  $\Delta\alpha = \alpha - \alpha_{\text{eff}}$

# $B^0 \rightarrow (\rho\pi)^0$ : Dalitz-plot analysis



The  $\rho(1450)$  and  $\rho(1700)$  resonances are also included in this analysis

$\rho\pi$  is not a  $CP$  eigenstate

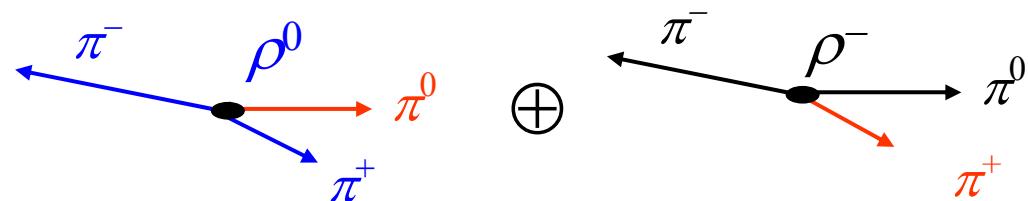
An isospin-pentagon analysis method exists but is not fruitful

⇒ Time-dependent Dalitz-plot analysis assuming isospin symmetry,  
measuring 26 coefficients of the bilinear form factors  
 $A.~Snyder~and~H.~Quinn,~Phys.~Rev.~D,~48,~2139~(1993)$

$$A(B^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ A(\rho^+ \pi^-) + f_- A(\rho^- \pi^+) + f_0 A(\rho^0 \pi^0)$$

$$\tilde{A}(\bar{B}^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ \tilde{A}(\rho^+ \pi^-) + f_- \tilde{A}(\rho^- \pi^+) + f_0 \tilde{A}(\rho^0 \pi^0)$$

Interference in the corners of the Dalitz plot provides information on **strong phases** between resonances



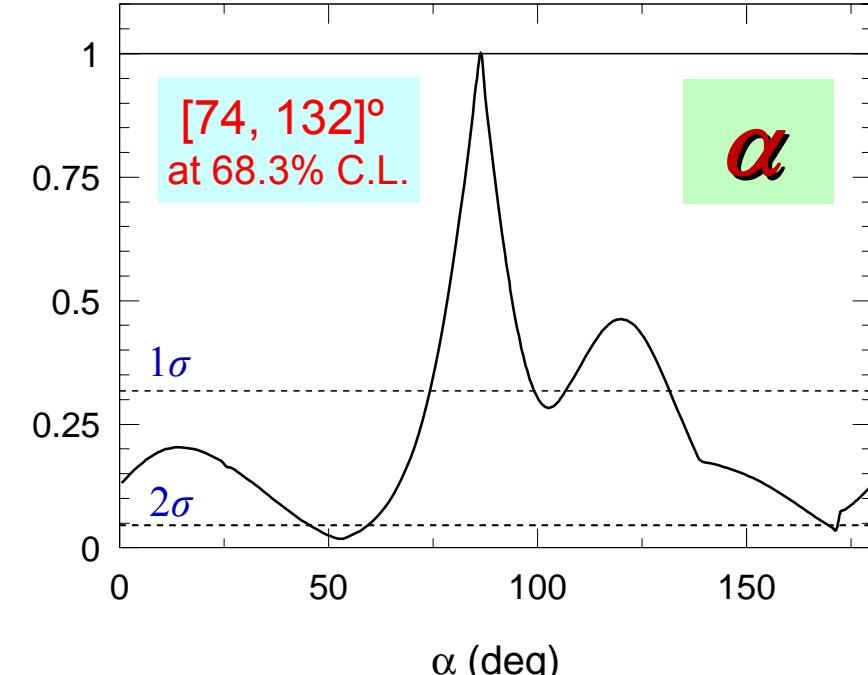
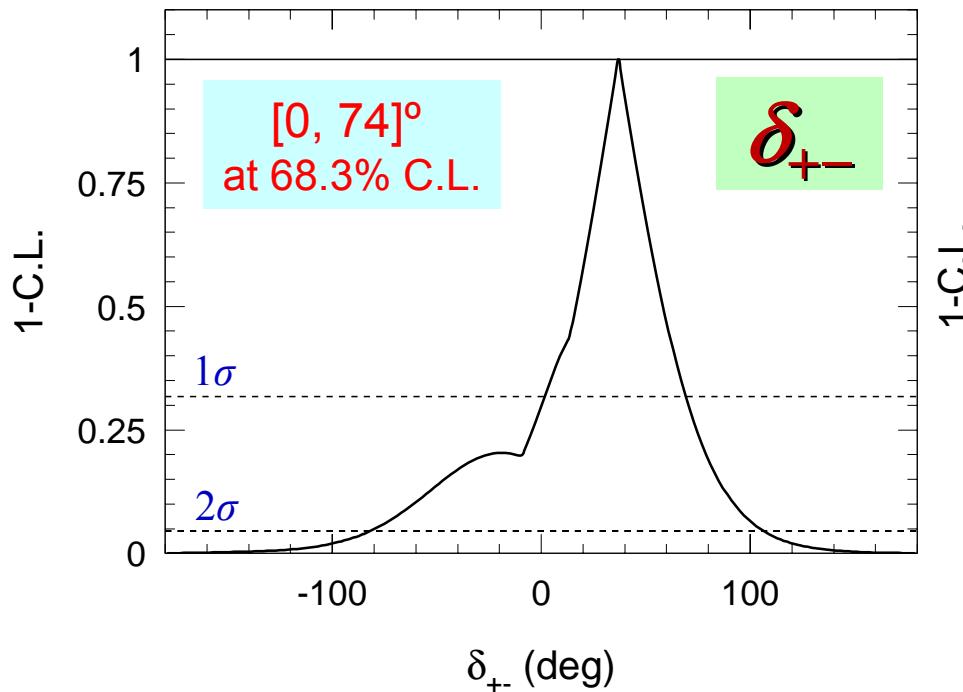
# An interpretation of the new $B^0 \rightarrow (\rho\pi)^0$ results

$375 \times 10^6$  BB pairs  
PRD 76, 012004 (2007)



DEI SVB NVMINE VIGET

$\delta_{+-} = \arg(A^{+*}A^-)$  : the relative phase between the amplitudes of  $B^0 \rightarrow \rho^-\pi^+$  and  $B^0 \rightarrow \rho^+\pi^-$



The constraint on  $\alpha$  from  $B^0 \rightarrow (\rho\pi)^0$  is relatively weak – but free from ambiguities!

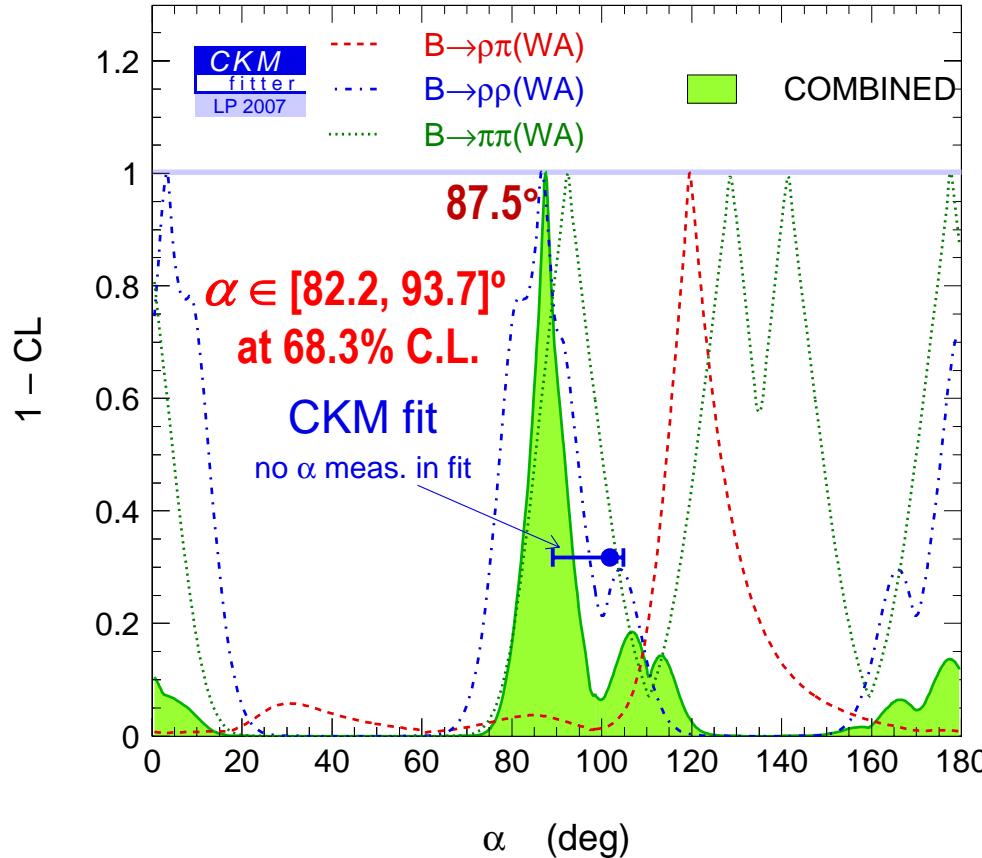
# Global fits for the value of $\alpha$



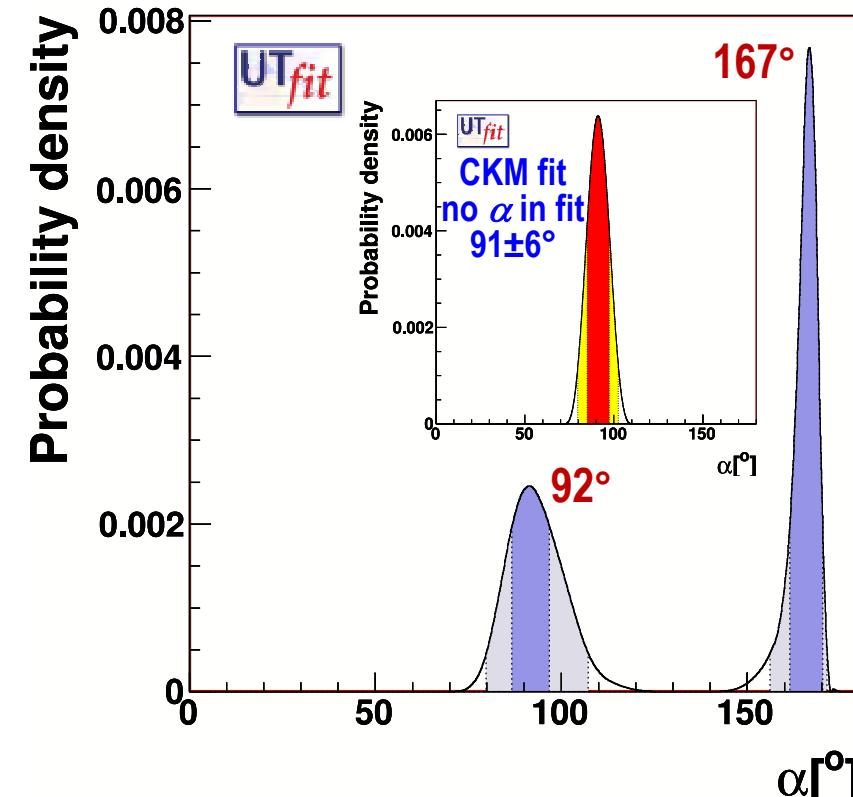
The second-highest-precision test of the KM mechanism of  $CP$  violation in meson decays

Two interpretations currently exist that convert the  $B \rightarrow \pi\pi, \rho\pi, \rho\rho$  measurements to constraints on  $\alpha$ :

A frequentist interpretation



A Bayesian interpretation, with model-dependent choices of priors



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C**41**, 1-131 (2005) [hep-ph/0406184],  
updated results and plots available at <http://ckmfitter.in2p3.fr>

M. Ciuchini, G. D'Agostini, E. Franco, V. Lubicz, G. Martinelli, F. Parodi, P. Roudeau, A. Stocchi, JHEP **0107** (2001) 013 [hep-ph/0012308],  
updated results and plots available at <http://www.utfit.org>



# $\gamma$ : the hardest to measure directly

Several techniques are combined, but the constraint is still rather weak



**Time-dependent:**  $\sin(2\beta + \gamma)$  from  $b \rightarrow c$ ,  $b \rightarrow u$  interference +  $B^0$  mixing

- $B^0 \rightarrow D^\mp \pi^\pm, D^{*\mp} \pi^\pm, D^\mp \rho^\pm$  : limited sensitivity due to smallness of  $r = |A(b \rightarrow u)/A(b \rightarrow c)|$
- $B^0 \rightarrow D^\mp K^0 \pi^\pm$  Dalitz plot (mostly through  $B^0 \rightarrow \bar{D}^{**0} K_S^0$  and  $B^0 \rightarrow D^- K^{*+}$ )

**Not time-dependent:**  $\gamma$  from  $b \rightarrow c$ ,  $b \rightarrow u$  interference

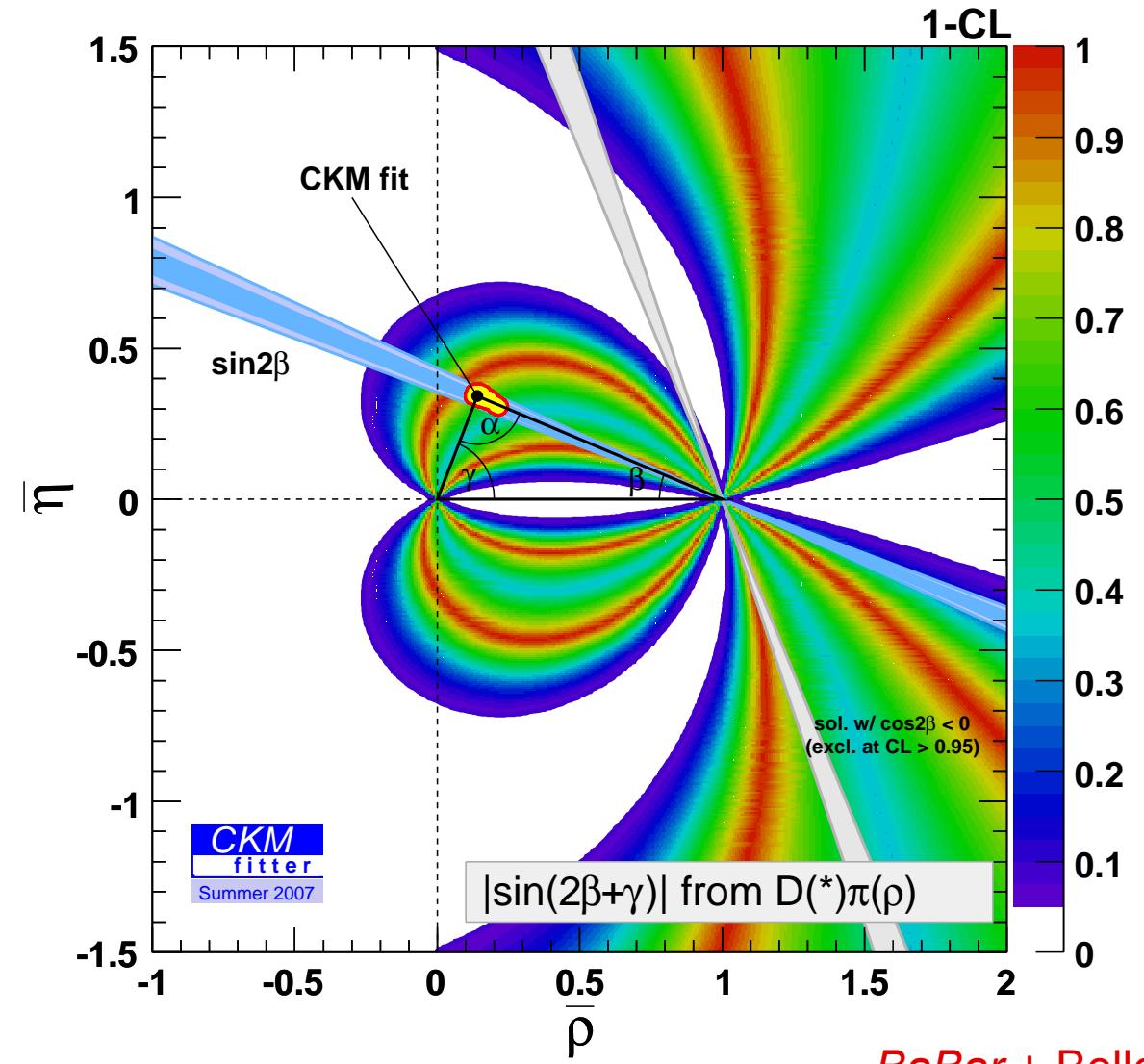
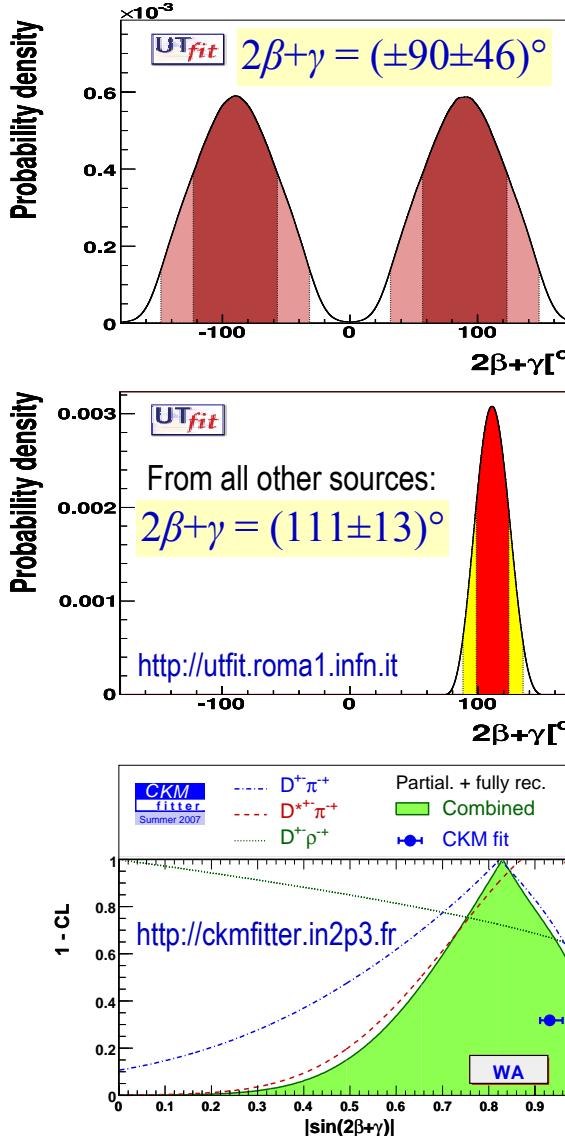
- $B^+ \rightarrow D^0_{CP} K^+$  (GLW = Gronau, London, Wyler): the first idea on the market
- $B^+ \rightarrow \bar{D}^0 K^+, D^0 \rightarrow K^+ \pi^-$  (ADS = Atwood, Dunietz, Soni): limited sensitivity
- $B^0 \rightarrow \bar{D}^0 K^{*0}$  Dalitz plot (also “ADS”) “wrong sign”  $D^0$  decay – doubly Cabibbo-suppressed
- $B^+ \rightarrow \bar{D}^{(*)0} K^+, D^0 \rightarrow K_S^0 \pi^+ \pi^-$  Dalitz plot (GGSZ = Giri, Grossman, Soffer, Zupan)

**Indirect:** (model-dependent and beyond the scope of this talk)

- $SU(3)$  analysis of amplitudes in  $B \rightarrow K\pi, \pi\pi$  (e.g., Gronau and Rosner, arXiv:0704.3459v3 [hep-ph])

# $\sin(2\beta+\gamma)$ status as of Summer 2007

Interpretations of  $B^0 \rightarrow D^\mp \pi^\pm, D^{*\mp} \pi^\pm, D^\mp \rho^\pm$  by UTfit and CKMfitter



*BaBar + Belle*

# $\sin(2\beta+\gamma)$ in $B^0 \rightarrow D^\mp K^0 \pi^\pm$ Dalitz plot



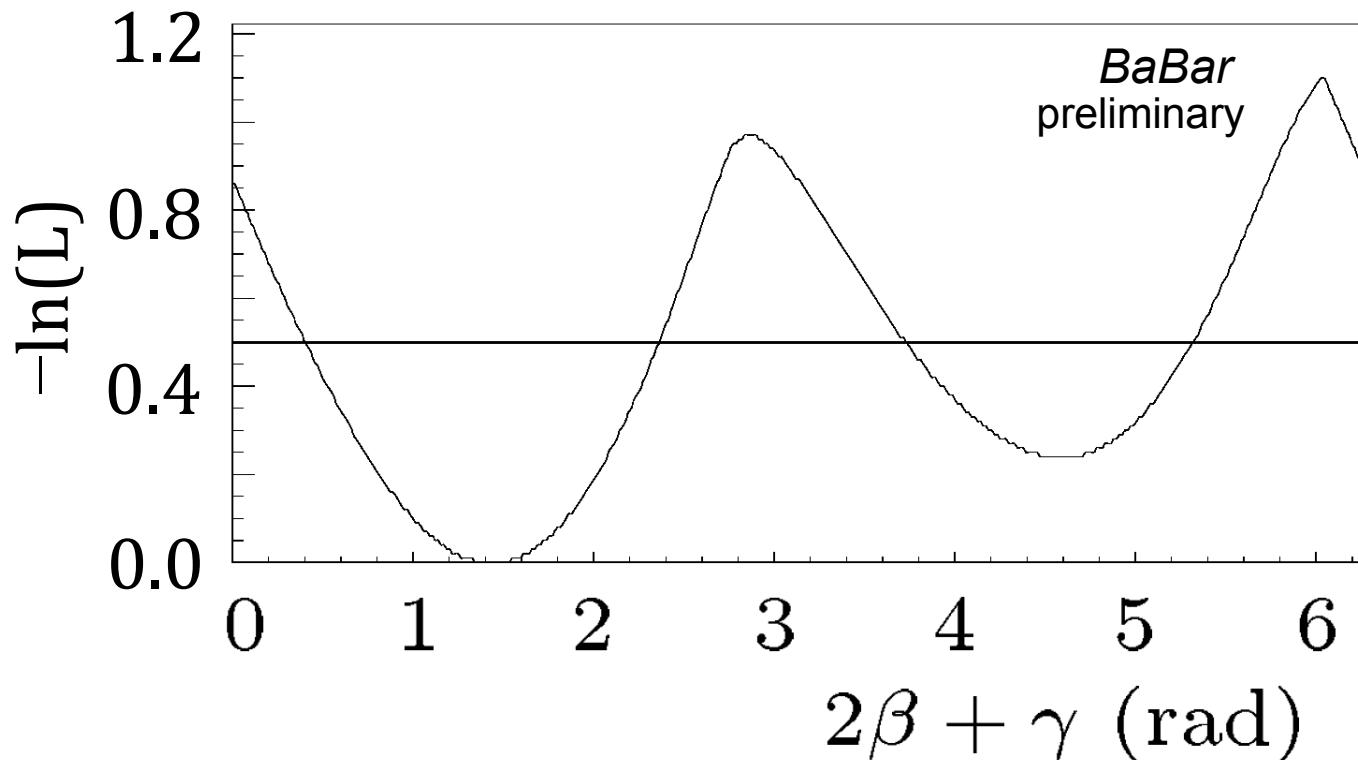
arXiv:0712.3469, accepted to Phys. Rev. D

$$N_{BB} = 347M$$

Assumes  $r = |A(b \rightarrow u)/A(b \rightarrow c)| = 0.3 \pm 0.1$

$$N_{\text{sig}} = 558 \pm 34$$

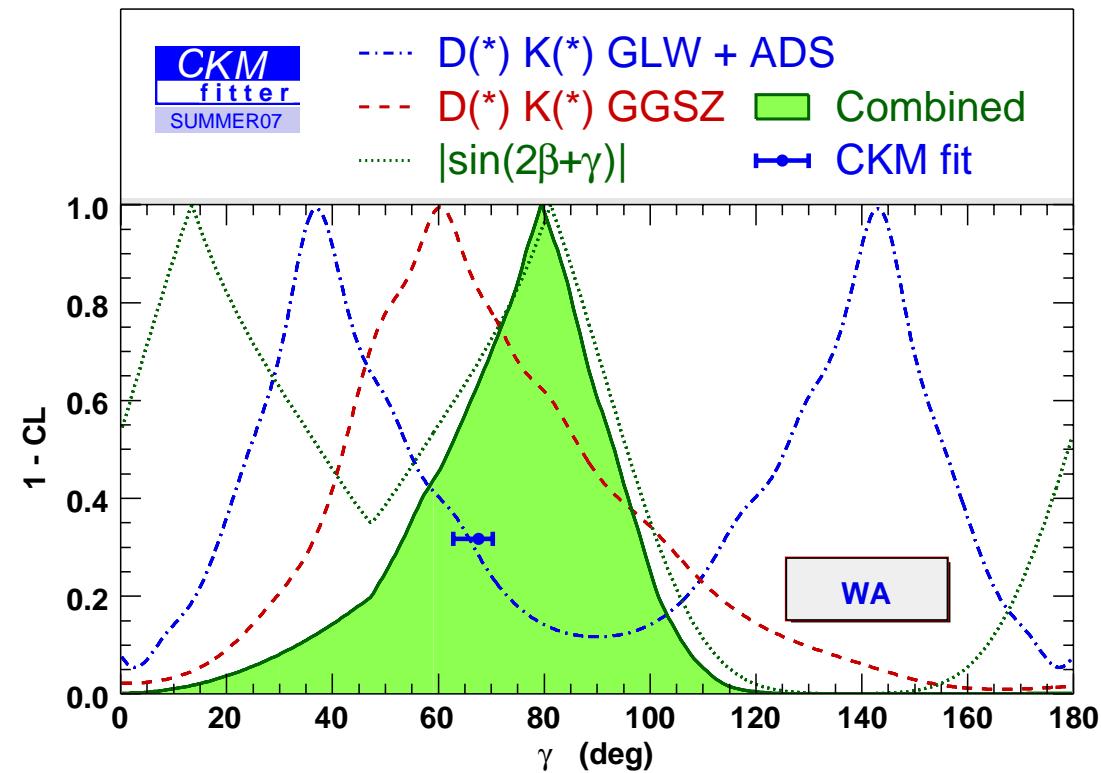
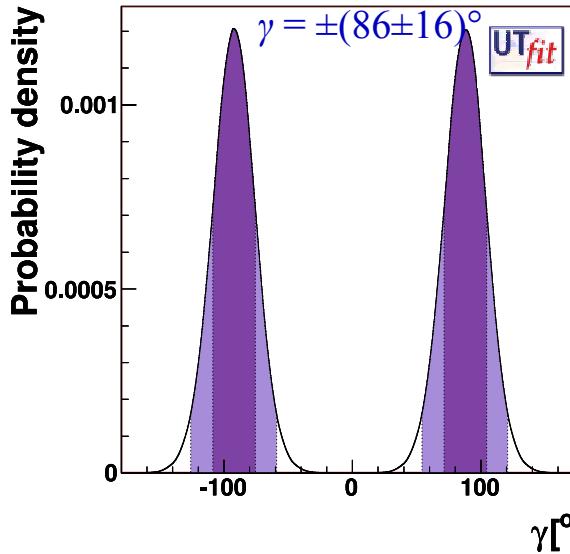
$$2\beta + \gamma = (83 \pm 53 \pm 20)^\circ \text{ or } (263 \pm 53 \pm 20)^\circ$$





# $\gamma$ status as of Summer 2007

Interpretations by UTfit and CKMfitter



CKMfitter:  $\gamma = (80^{+18}_{-26})^\circ$

BaBar + Belle

# $\gamma$ in $B^0 \rightarrow \bar{D}^0 K^{*0}$ GGSZ Dalitz plot

BaBar-PUB-07/072, to be submitted to Phys. Rev. D

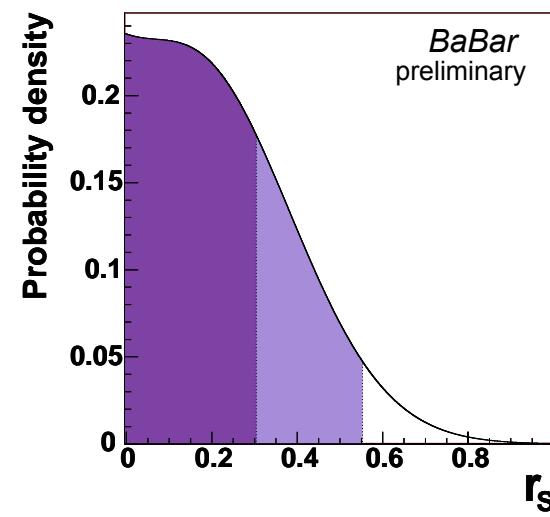
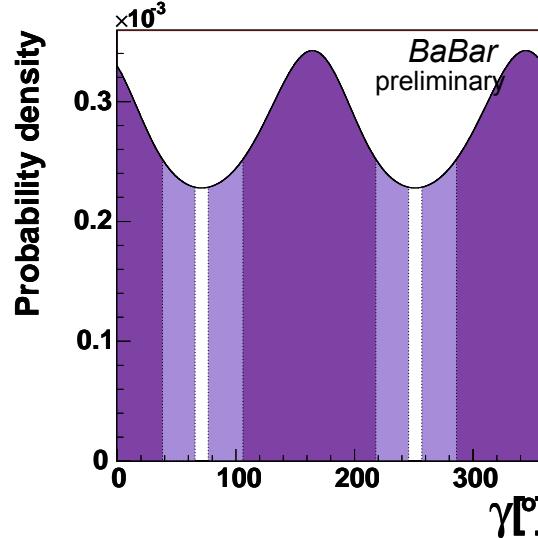
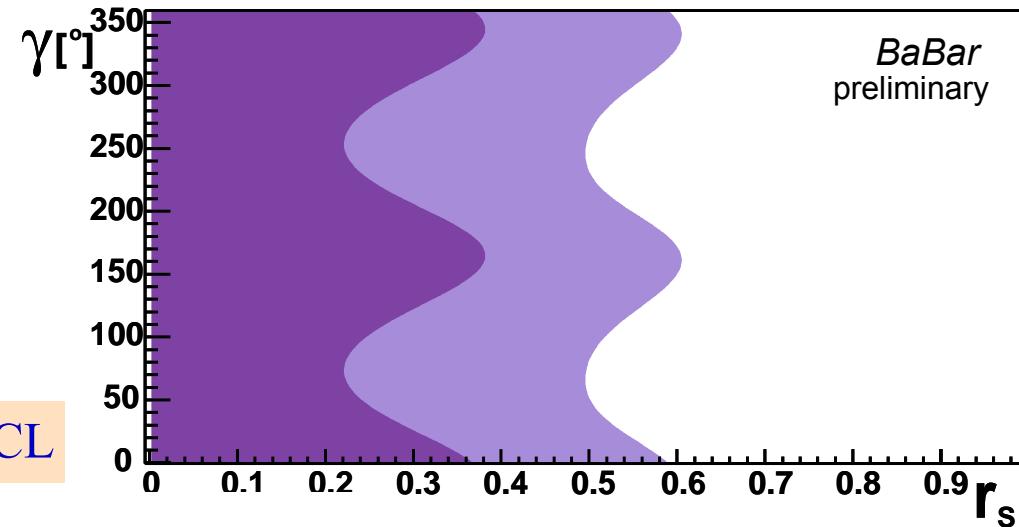


$N_{BB} = 371M$

$N_{\text{sig}} = 39 \pm 9$

$\gamma = (162 \pm 56)^\circ \text{ or } (342 \pm 56)^\circ$

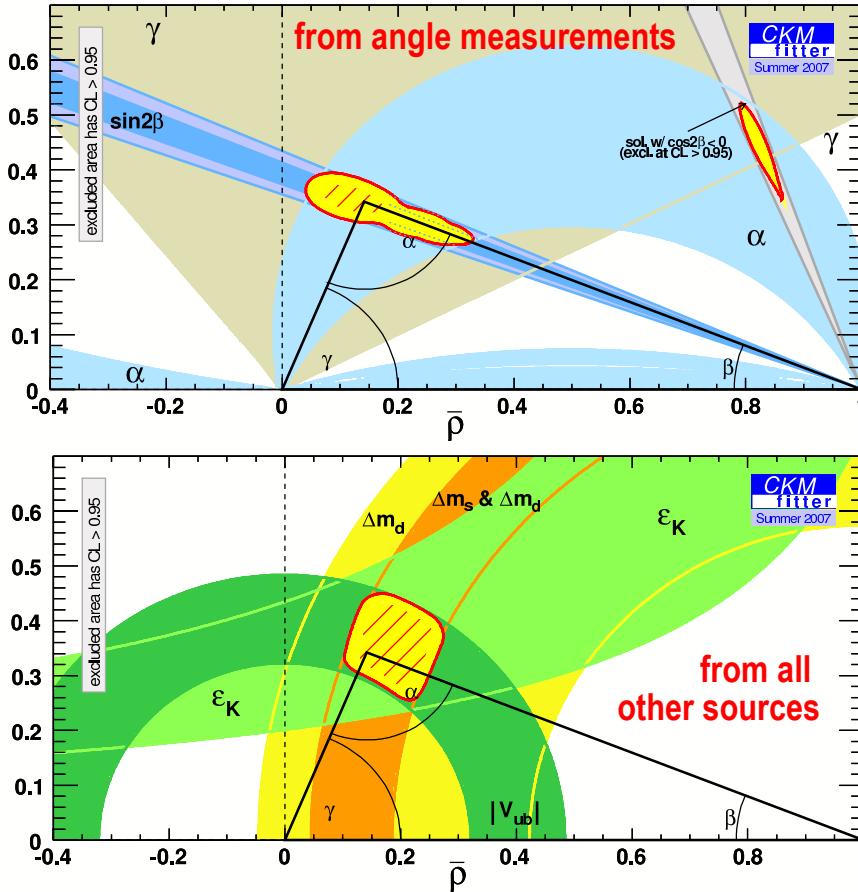
$r_s = |A(b \rightarrow u)/A(b \rightarrow c)| < 0.55 @ 95\% \text{ CL}$



# Current knowledge of the Unitarity Triangle

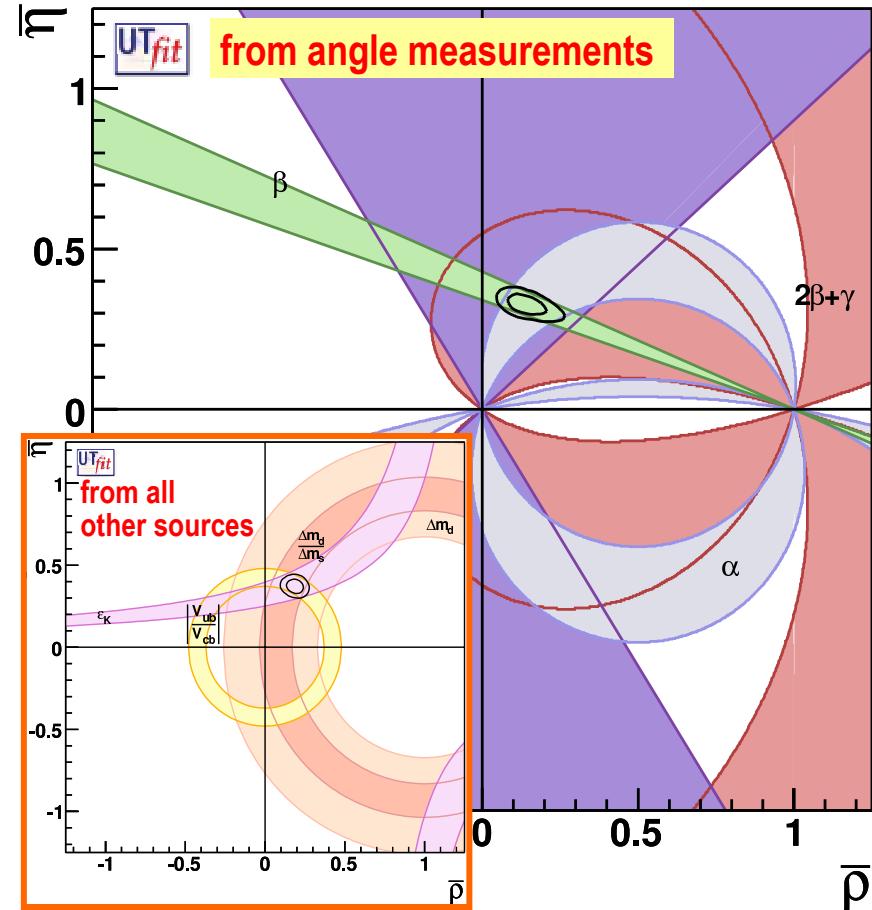
Important: nearly all measurements are still statistics-limited

A frequentist interpretation



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005), [hep-ph/0406184],  
 updated results and plots available at <http://ckmfitter.in2p3.fr>

A Bayesian interpretation, with model-dependent choices of priors



M. Ciuchini, G. D'Agostini, E. Franco, V. Lubicz, G. Martinelli, F. Parodi, P. Roudeau, A. Stocchi, JHEP 0107 (2001) 013 [hep-ph/0012308],  
 updated results and plots available at <http://utfit.roma1.infn.it>

# Summary and outlook

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The Kobayashi-Maskawa phase has been demonstrated to be the dominant source of  $CP$  violation in meson decays.

Constraints on the CKM Unitarity Triangle from angle measurements are statistics-limited, comparable with constraints from all other sources – and mutually consistent.

The absence of statistically significant inconsistencies contains a wealth of information about the flavor structure New Physics that can be expected at the TeV scale. In particular, it pushes up the scale of new  $CP$ -violating physics in many NP models.