

CKM Unitarity Triangle:

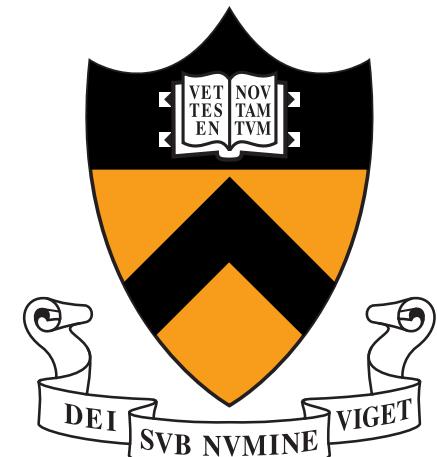
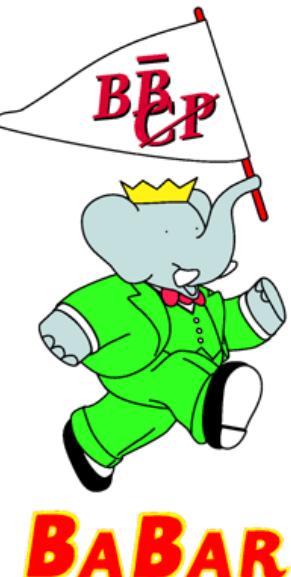
Update on Angles from *BaBar*

*Particle Physics Seminar
Physics Department, Brookhaven National Laboratory*

Thursday, February 28, 2008

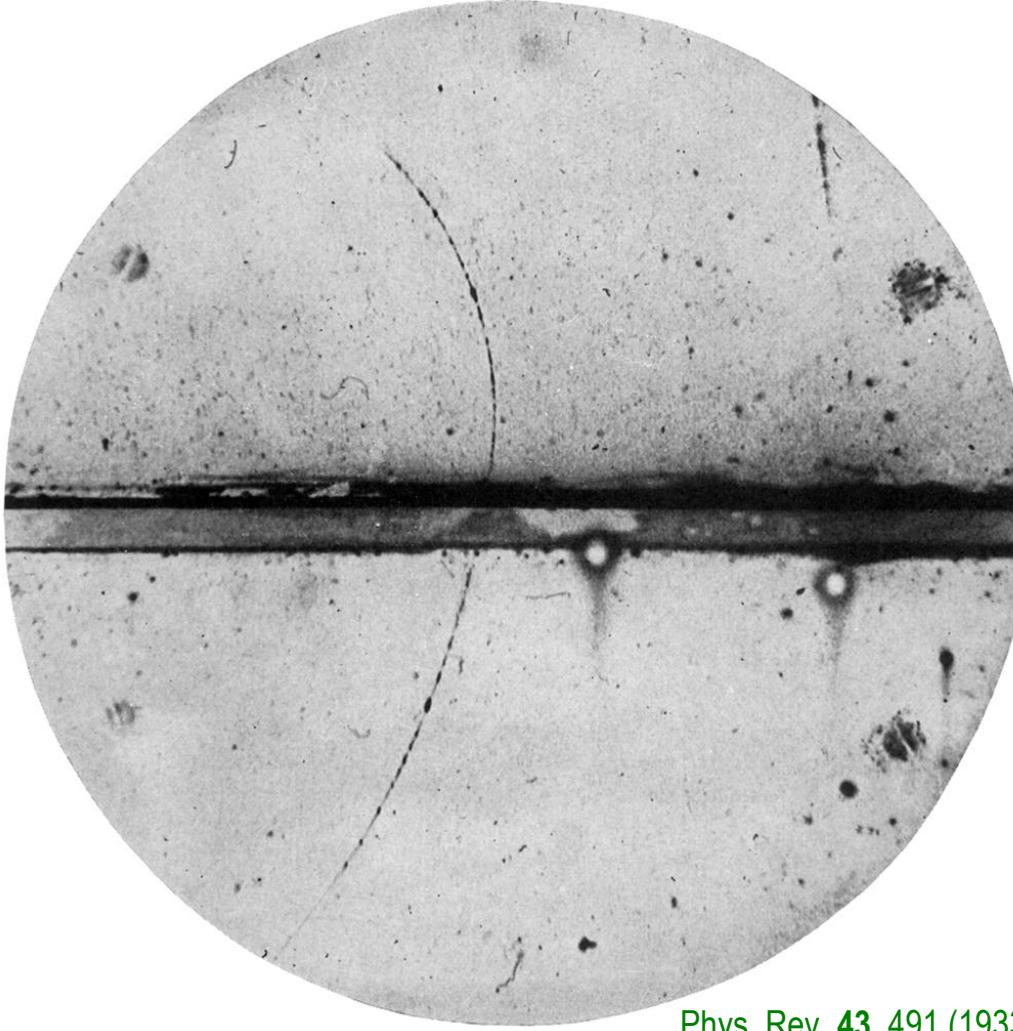
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Discovery of antimatter

Each particle, except the truly neutral ones, has an antiparticle



Phys. Rev. 43, 491 (1933)

FIG. 1. A 63 million volt positron ($H\rho = 2.1 \times 10^5$ gauss-cm) passing through a 6 mm lead plate and emerging as a 23 million volt positron ($H\rho = 7.5 \times 10^4$ gauss-cm). The length of this latter path is at least ten times greater than the possible length of a proton path of this curvature.

1928: Dirac predicts antimatter to explain a seemingly unphysical solution to his equations of relativistic quantum mechanics

1932: Anderson discovers positrons in cosmic rays passing through a Wilson chamber in 1.5 T magnetic field, shares 1936 Nobel Prize



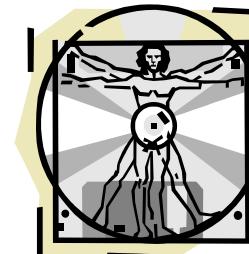
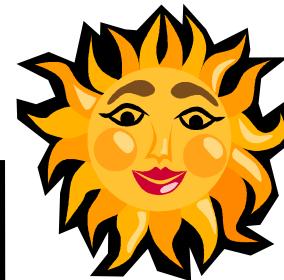
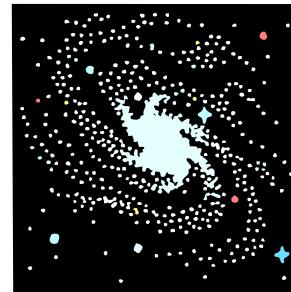
Matter-Antimatter Asymmetry of the Universe



Very early Universe must have had equal amounts of matter and antimatter. Where did all the antimatter go?

Baryonic asymmetry of the Universe:

$$\frac{N_B - N_{\bar{B}}}{N_\gamma} \simeq \frac{N_B}{N_\gamma} \simeq 5 \times 10^{-10}$$





Symmetries in Nature



Symmetries have played a central role in the development of physics:

Translation in space \leftrightarrow conservation of linear momentum

Rotation in space \leftrightarrow conservation of angular momentum

Translation in time \leftrightarrow conservation of energy

Redefinition of relative phase \leftrightarrow conservation of electrical charge

Parity: a discrete symmetry

$$\vec{r} \rightarrow -\vec{r}, \quad \vec{s} \rightarrow +\vec{s}, \quad \vec{L} \rightarrow +\vec{L}$$

$$P |a(E, \vec{p}, \lambda)\rangle = \eta_P |a(E, -\vec{p}, -\lambda)\rangle \quad (\lambda \equiv \vec{s} \cdot \vec{p})$$

Spatial parity P : $P = P^{-1} = P^\dagger, \quad \eta_P = \pm 1$

$$P(Y_{\ell m}(\vartheta, \varphi)) = Y_{\ell m}(\pi - \vartheta, \pi + \varphi) = (-1)^\ell Y_{\ell m}(\vartheta, \varphi)$$

$$P(\text{fermion}) = -P(\text{antifermion}); \quad P(q \bar{q}') = (-1)^{L+1}$$

Charge conjugation

$$C |a(E, \vec{p}, \lambda)\rangle = \eta_C |\bar{a}(E, \vec{p}, \lambda)\rangle$$

C : $C = C^{-1} = C^\dagger, \quad \eta_C = \pm 1$

Fermi statistics

Spin wavefunction

Orbital wavefunction

$$-1 = (-1)^{S+1} \cdot (-1)^L \cdot C(q \bar{q}) \Rightarrow C(q \bar{q}) = (-1)^{L+S}$$

Time reversal T : $T |a(E, \vec{p}, \lambda)\rangle = \eta_T \langle a(E, -\vec{p}, \lambda)| ; \quad \eta_T = \pm 1$



CPT theorem



Lagrangian of any quantum field theory
that obeys the laws of relativity and causality, conforms to the quantum
mechanical interpretation of the positive, conserved probability, and is local,
is invariant under the combined *CPT* transformation.

Consequence: masses and total decay widths of a particle
and its antiparticle **must be equal** to all orders of interactions.

Note: equality of all *partial* decay widths requires, in addition to
CPT, invariance of the Lagrangian under ***CP***.



Discovery of CP violation

Christensen, Cronin, Fitch, Turlay @ AGS (Brookhaven), 1964



$$\begin{cases} K^0 = d \bar{s} \\ \bar{K}^0 = s \bar{d} \end{cases} ; \quad \begin{cases} CP|K^0\rangle = e^{+2i\vartheta} |\bar{K}^0\rangle \\ CP|\bar{K}^0\rangle = e^{-2i\vartheta} |K^0\rangle \end{cases} \quad (\vartheta \text{ is a matter of convention})$$

$$\begin{cases} K_1^0 = |K_{CP=+1}\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle + e^{+2i\vartheta} |\bar{K}^0\rangle) \rightarrow \pi^+ \pi^-, \pi^0 \pi^0 \\ K_2^0 = |K_{CP=-1}\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle - e^{+2i\vartheta} |\bar{K}^0\rangle) \rightarrow \pi^+ \pi^- \pi^0, \pi^0 \pi^0 \pi^0 \end{cases}$$

$$\begin{cases} m_{K^0} = 497.648 \pm 0.022 \text{ MeV} \\ m_{K_L^0} - m_{K_S^0} = (3.483 \pm 0.006) \times 10^{-6} \text{ eV} \end{cases} ; \quad \begin{cases} \tau_{K_S^0} = (0.8953 \pm 0.0005) \times 10^{-10} \text{ sec} \\ \tau_{K_L^0} = (5.116 \pm 0.020) \times 10^{-8} \text{ sec} \end{cases}$$

$$\begin{cases} \text{Br}(K_S^0 \rightarrow \pi^+ \pi^-) = 69.20 \pm 0.05 \% \\ \text{Br}(K_S^0 \rightarrow \pi^0 \pi^0) = 30.69 \pm 0.05 \% \\ \text{Br}(K_S^0 \rightarrow \pi^+ \pi^- \pi^0) = 3.5_{-0.9}^{+1.1} \times 10^{-7} \\ \text{Br}(K_S^0 \rightarrow 3\pi^0) < 1.2 \times 10^{-7} \end{cases} ;$$

PDG 2007 data

$$\begin{cases} \text{Br}(K_L^0 \rightarrow 3\pi^0) = 19.51 \pm 0.12 \% \\ \text{Br}(K_L^0 \rightarrow \pi^+ \pi^- \pi^0) = 12.54 \pm 0.05 \% \\ \text{Br}(K_L^0 \rightarrow \pi^+ \pi^-) = (1.966 \pm 0.010) \times 10^{-3} \\ \text{Br}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.64 \pm 0.06) \times 10^{-4} \end{cases}$$

↑ CP violating decays ↑

Through the CPT Theorem, CP violation implies the existence of T violation



Sakharov's three conditions



The three conditions necessary to produce the baryonic asymmetry of the Universe:



(photo circa 1943)

А. Д. Сахаров, *Письма в ЖЭТФ*, 5, № 1, 32-35, 1 января 1967
A. D. Sakharov, *Soviet Journal of Experimental and Theoretical Physics, Letters to the Editor*, 5, No. 1, 24-27, 1st January 1967

1. Baryon number violation (proton decay)

2. C and CP violation

By far the strongest argument for existence of sources of CP violation in nature is the very fact that we are here today!

3. Departure from thermal equilibrium

The Quark Mixing Matrix

The only Standard-Model source of CP violation in the quark sector



The Cabibbo-Kobayashi-Maskawa matrix relates the electroweak (q') and the mass (q) quark eigenstates:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2 / 2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2 / 2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4) + iO(\lambda^6)$$

$$V^\dagger V = 1 \Rightarrow V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

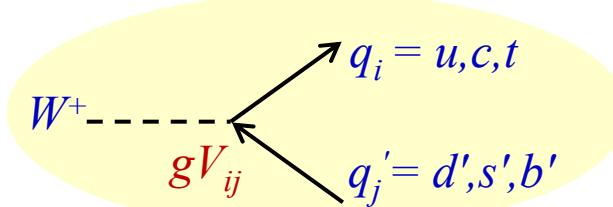
the “unitarity triangle”

$$\alpha \equiv \arg \left[-\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right]$$

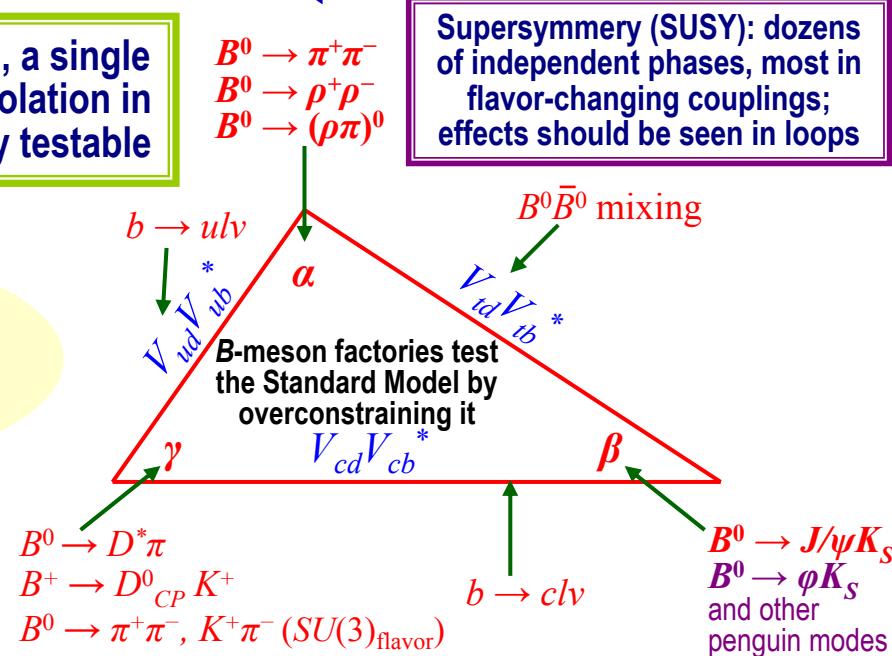
In the Kobayashi-Maskawa model, a single phase is responsible for all CP violation in meson decays, making it uniquely testable

$$\beta \equiv \arg \left[-\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right]$$

$$\gamma \equiv \arg \left[-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right]$$



CKM mechanism alone is far too small to account for the baryon asymmetry of the universe: Gavela et.al, Nucl. Phys. **B 430**, 382 (1994)



Time evolution of the B^0 meson

The time-dependent rate for \bar{B}^0 (f_+) or B^0 (f_-) decays to a final state f (neglecting the lifetime difference between the mass eigenstates B_{Heavy} and B_{Light}):

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} [1 \mp C_f \cos(\Delta m \Delta t) \mp S_f \sin(\Delta m \Delta t)]$$

where

S and C is what we measure

$$|B_{L/H}\rangle = p |B^0\rangle \pm q |\bar{B}^0\rangle, \quad \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f},$$

from mixing, $\approx e^{-2i\beta}$

$$S_f = \frac{-2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2}, \quad C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

a_f is the time-evolution asymmetry:

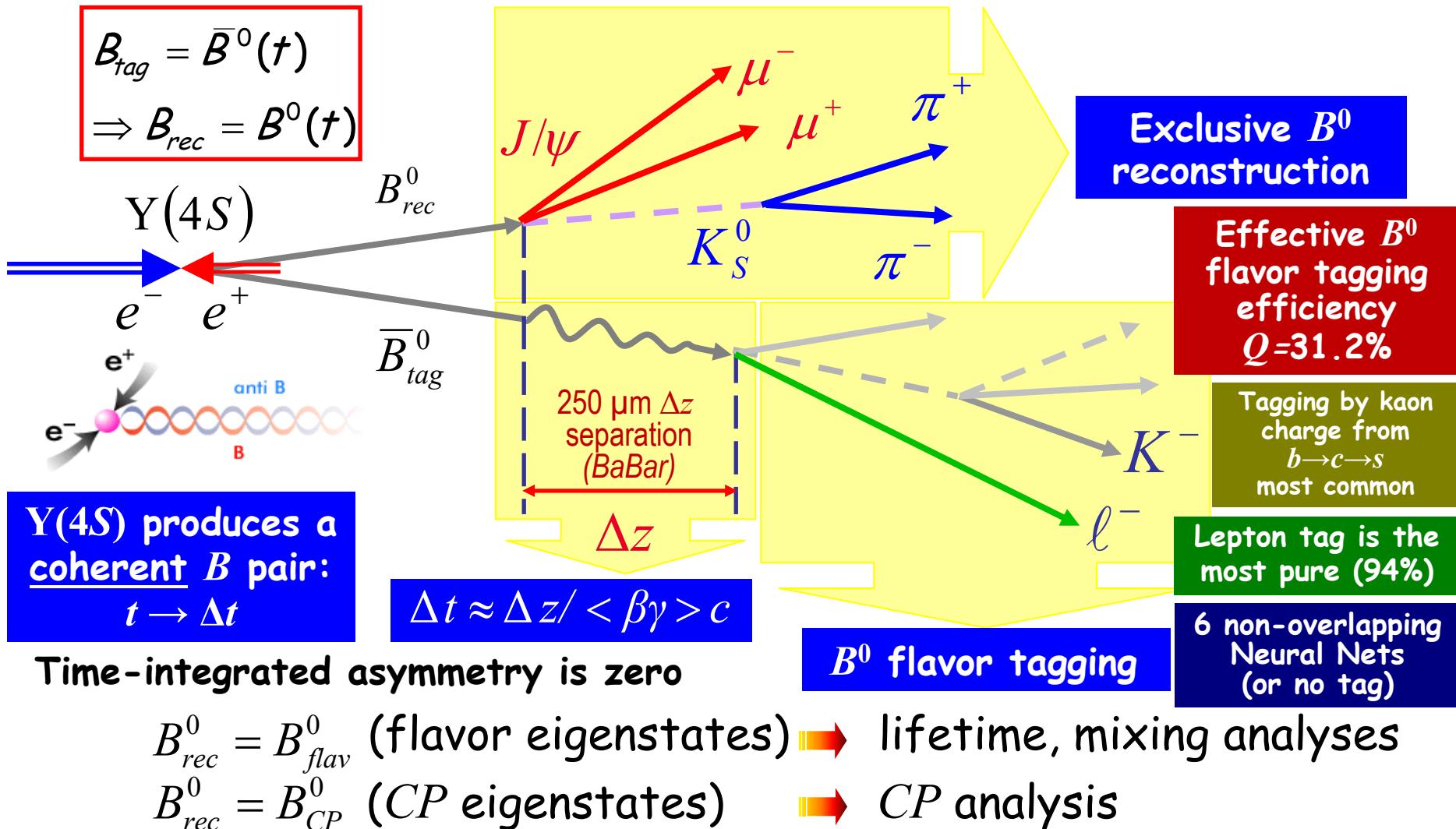
$$a_f(\Delta t) = \frac{f_+(\Delta t) - f_-(\Delta t)}{f_+(\Delta t) + f_-(\Delta t)}$$

If f is a CP eigenstate, f_{CP} , we have CP violation if $\lambda_f \neq \pm 1$:

- $|q/p| \neq 1$ (CP violation in mixing, very small)
- $|\bar{A}_f/A_f| \neq 1$ (direct CP violation, small in $b \rightarrow c\bar{c}s\bar{s}$)
- $\operatorname{Im}(\lambda_f) \neq 0$ (interference between mixing and decay)

*B. Aubert et al. (BaBar Collaboration)
Phys. Rev. Lett. 96, 251802 (2006)*

Time-dependent CP analysis at a B -meson factory



PEP-II performance

Y(4S) CM energy: 10.580 GeV

Beam energies:

electrons: 9.0 GeV

positrons: 3.1 GeV

Beam currents:

electrons: 2.05 A

positrons: 3.03 A

Number of bunches: 1722

Beam size at IP: 125 μm x 4 μm

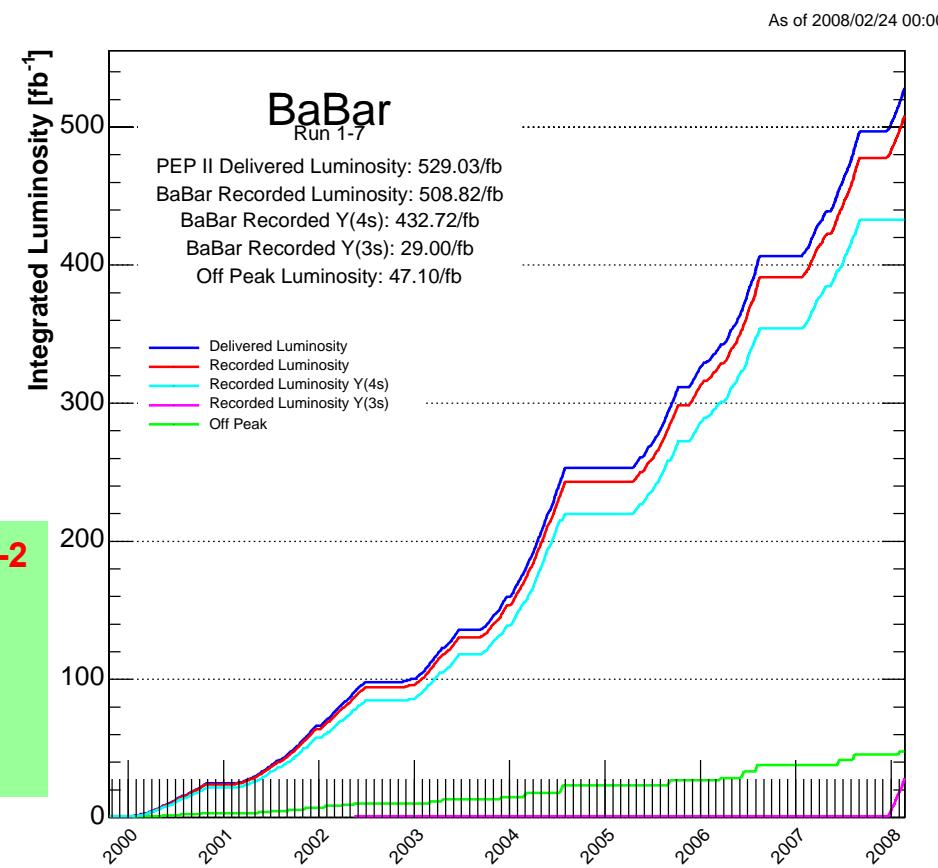
Peak luminosity: $12.1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

(design: $3 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$)

Best 24 hours: 911 pb^{-1} delivered

(design: $135 \text{ pb}^{-1}/\text{day}$)

Y(4S) operation concluded on December 21, 2007
 Y(3S): 30 fb^{-1} (done)
 Y(2S): 20 fb^{-1} (in progress)

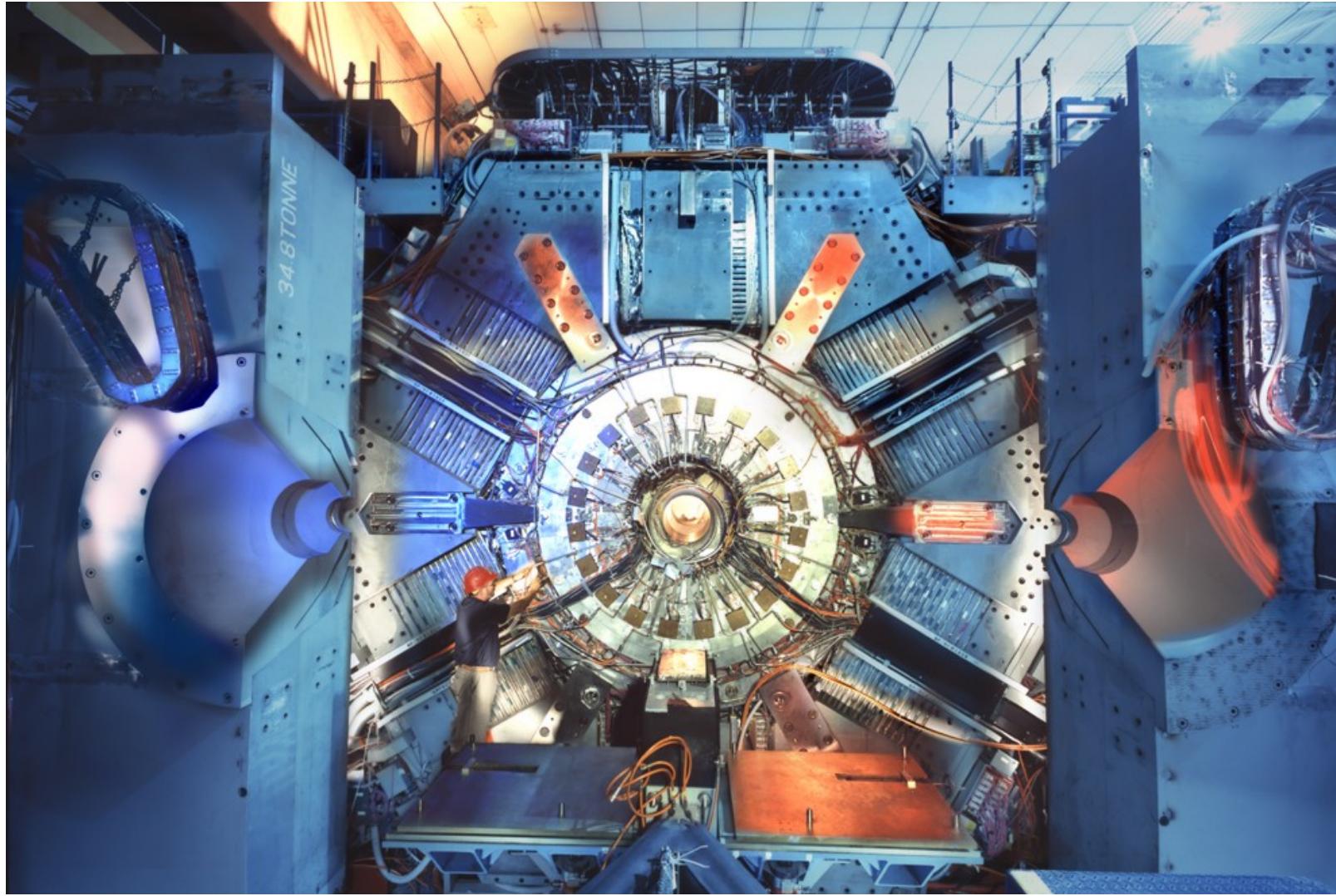




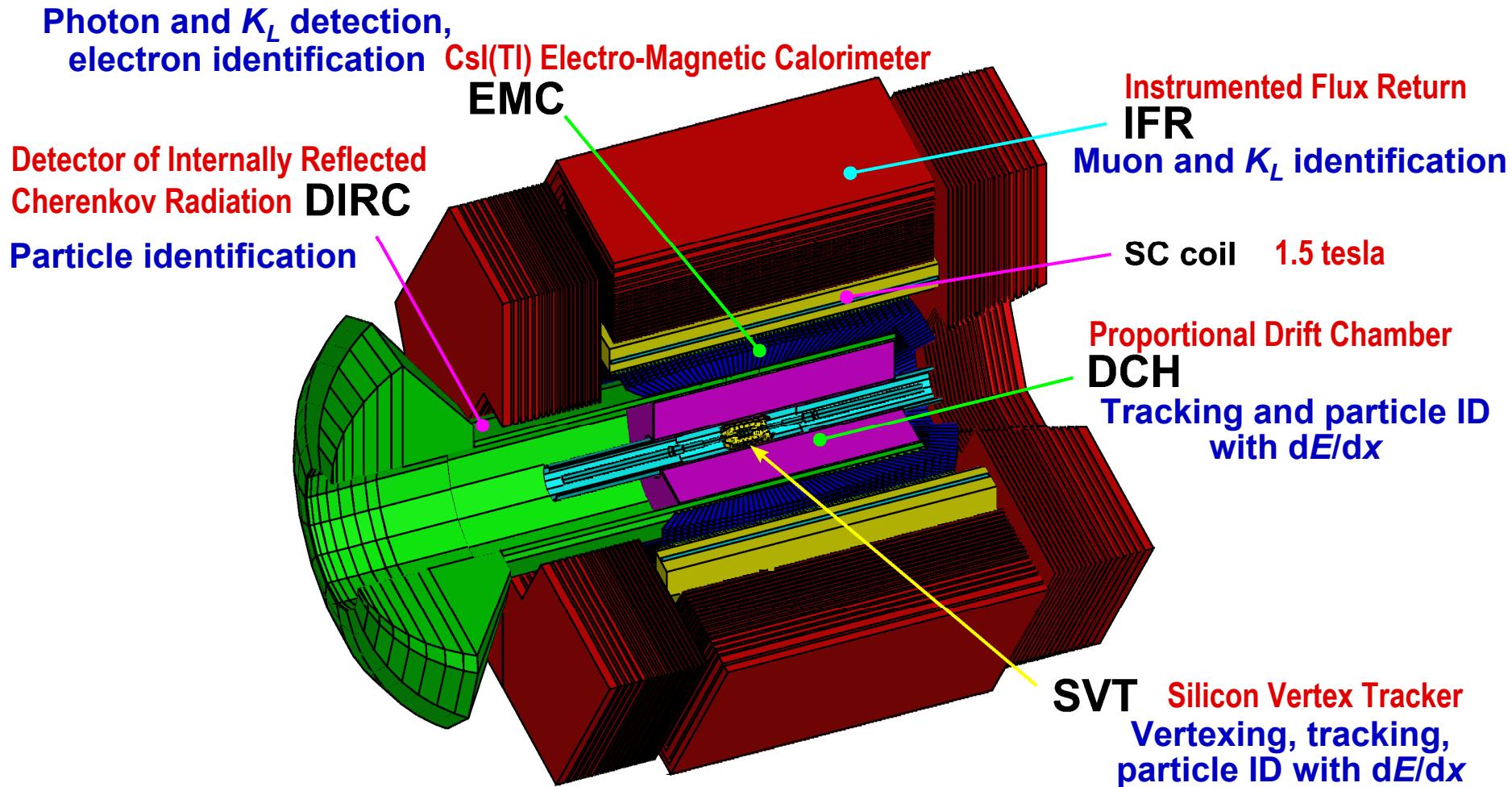
BABAR



The BaBar detector



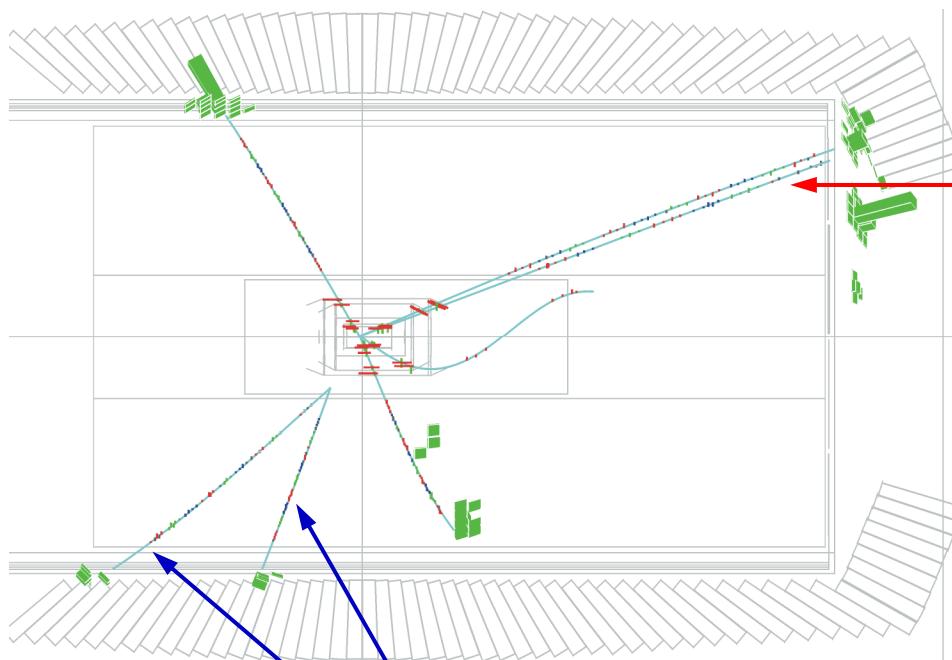
The BaBar detector



Note that electron ID and muon ID are largely orthogonal to pion/kaon/proton separation with DIRC+DCH+SVT

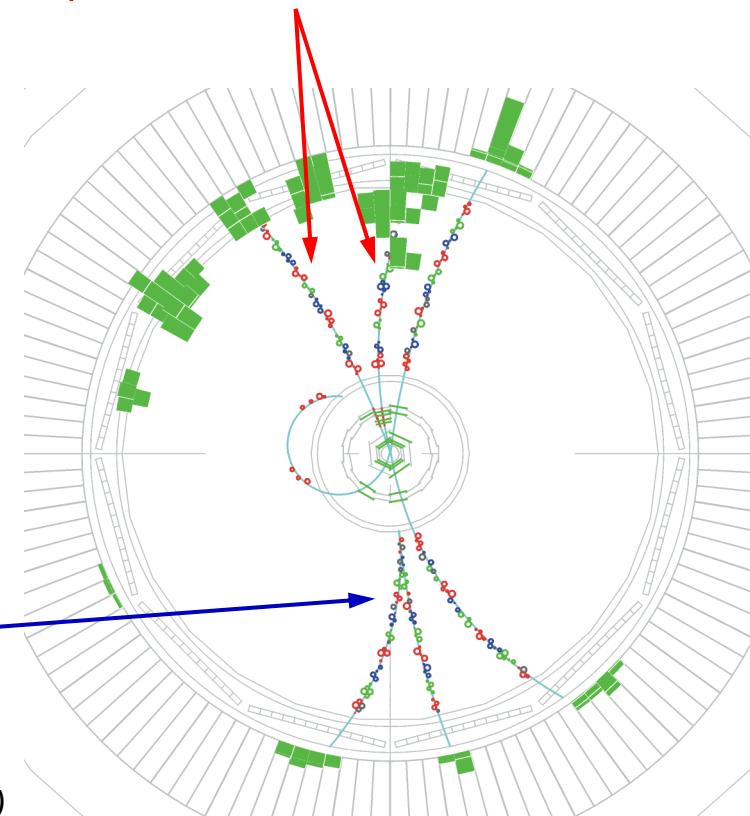
Example of a B -decay event in BaBar

$$B^0 \rightarrow \phi K_S$$



only the hits that correspond to reconstructed tracks and neutral candidates are shown
(noise hits are removed)

$$\phi \rightarrow K^+ K^-$$



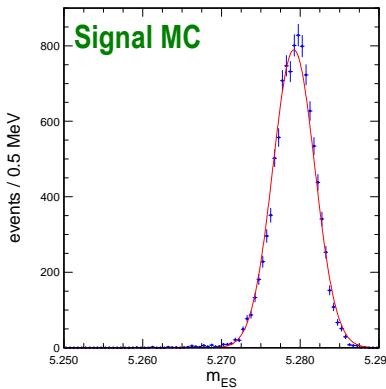
$$K_S \rightarrow \pi^+ \pi^-$$

Run 29368, event hexID 249a4b/d610dd73 (June 27, 2002)
From the dataset used in [Phys.Rev.D 69:011102, 2004](#)

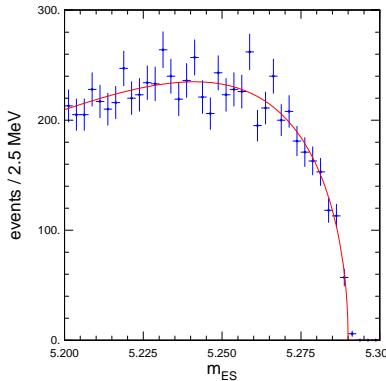
Common discriminating variables: kinematics

A pair of weakly correlated variables that reflect energy and momentum conservation:
peaking for fully reconstructed B decays, smooth for combinatorial background

$$m_{\text{ES}} \equiv \sqrt{E_{\text{CM beam}}^2 - p_{\text{CM } B}^2} = m_B$$

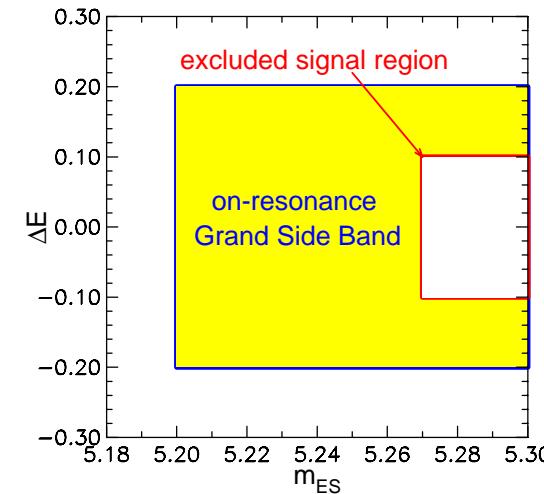


resolution $\sim 2.6 \text{ MeV}/c^2$
determined by the beam energy spread

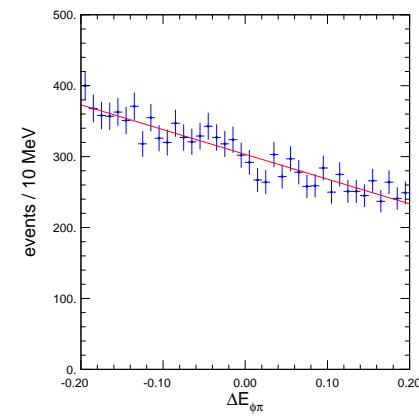
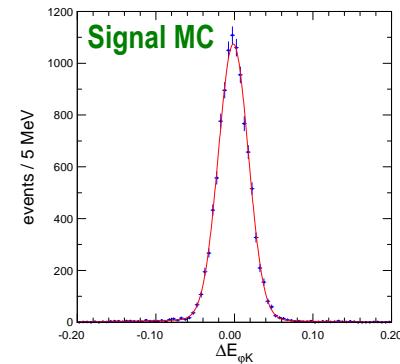


$$\Delta E \equiv E_{\text{CM } B} - E_{\text{CM beam}} = 0$$

resolution $\sim 15\text{--}80 \text{ MeV}$
depending on the number of tracks and presence of neutrals in the final state

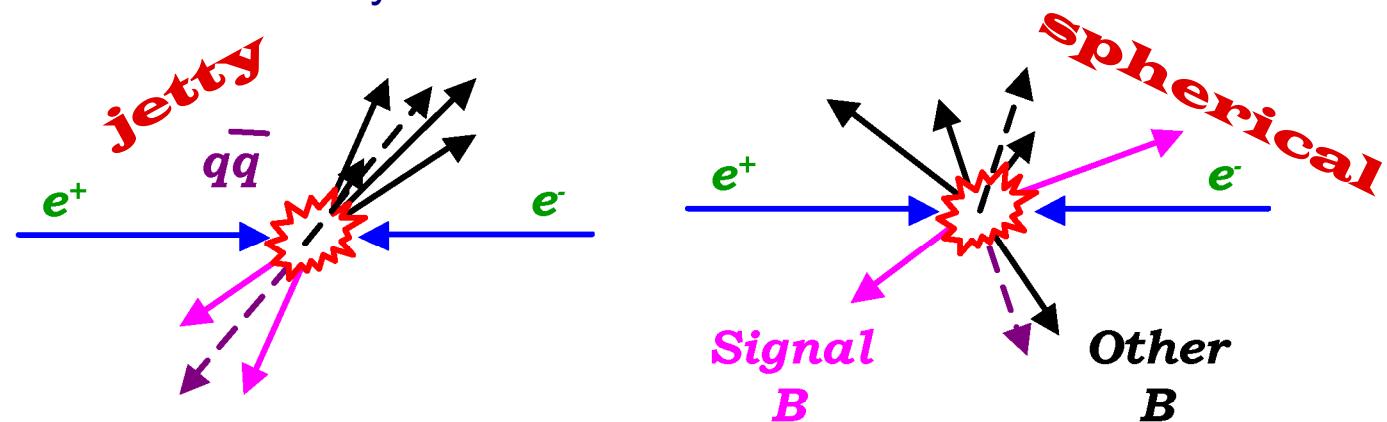


continuum background in the Grand Side Band



Common discriminating variables: event shape

- The principal source of background to rare B decays: random track/neutral combinations from quark-pair ($udsc$) production in the continuum:
 - total $udsc$ cross section ~ 3.4 nb, compared to ~ 1.1 nb for $\Upsilon(4S)$
 - $udsc$ events have jet-like topology, while B decays are nearly spherical in CM
 - several topological variables are employed to suppress this background
- Backgrounds from $\tau^+\tau^-$ production and two-photon physics are usually negligible
- Backgrounds from other B decays tend to be small



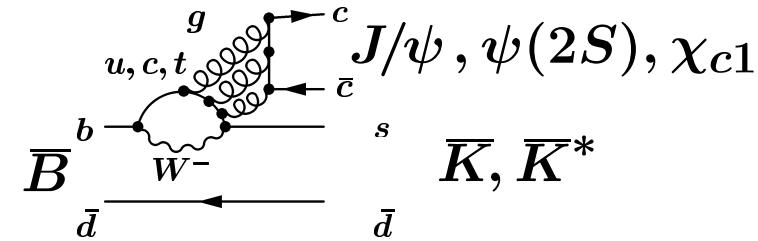
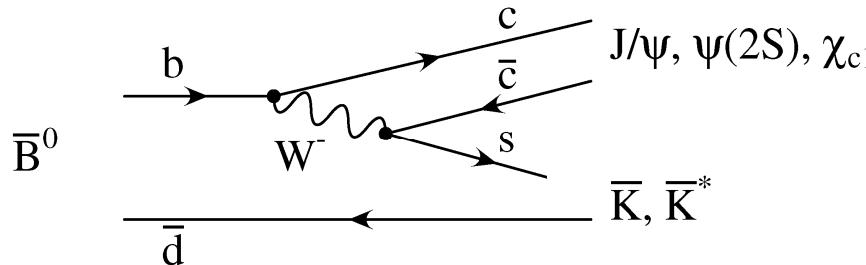
Analyses are blind until the methodology has been finalized and frozen

$\sin 2\beta$ in “golden” $b \rightarrow c\bar{c}s$ modes:



The highest-precision test of the KM mechanism of CP violation in meson decays

Golden-mode branching fractions are $O(10^{-3})$



“Golden” modes: color-suppressed tree dominates; the t -quark penguin has the same weak phase as the tree (none). In Standard Model, therefore,

$$S_{\text{golden}} = \eta_{CP} \times \sin 2\beta, \quad C_{\text{golden}} = 0 \quad (\eta_{CP} = \pm 1)$$

Theoretical uncertainties:

- an example of a model-independent, data-driven calculation:
assuming $SU(3)_{\text{flavor}}$ invariance, use $B^0 \rightarrow J/\psi \pi^0$ data to constrain penguin pollution in $J/\psi K^0 \Rightarrow \Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta = 0.000 \pm 0.012$

M. Ciuchini, M. Pierini, L. Silvestrini,
Phys. Rev. Lett. **95**, 221804 (2005)

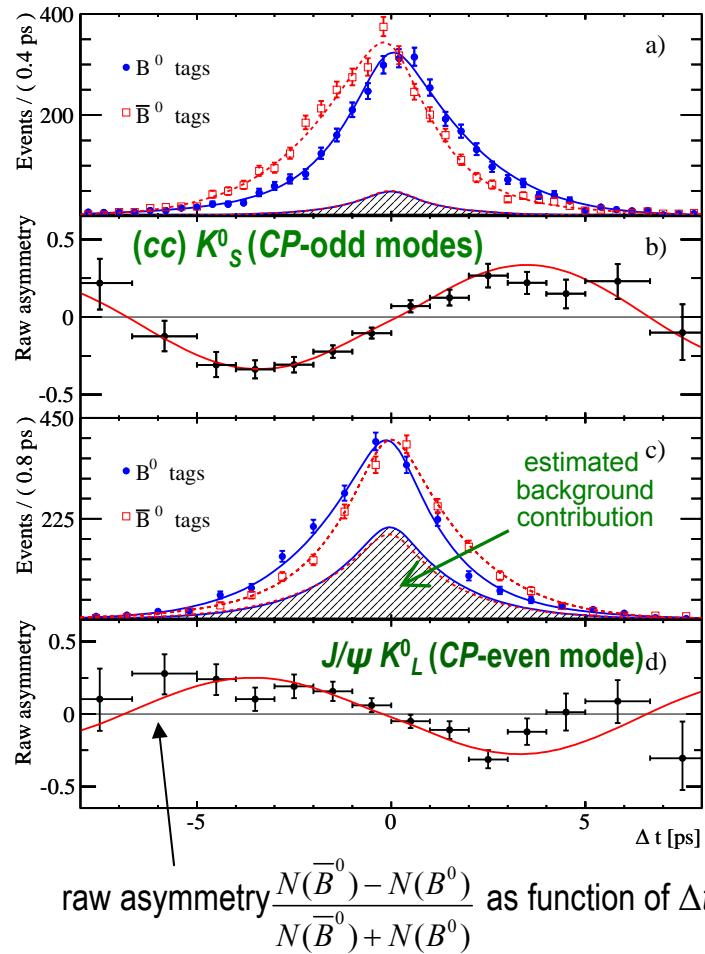
- theoretical estimates of the biases due to u - and c -quark penguins, etc.:
 - $\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-3})$
 - $\Delta S_{J/\psi K^0} = S_{J/\psi K^0} - \sin 2\beta \sim O(10^{-4})$

H. Li, S. Mishima, JHEP 0703:009 (2007) [hep-ph/0610120]

H. Boos et al., Phys. Rev. D **73**, 036006 (2006)

Latest on $\sin 2\beta$ in “golden” modes

CP Violation in B mesons first observed here, in 2001



| | |
|----------------------------|-----------------------------|
| $J/\psi K_s (\pi^+ \pi^-)$ | $0.702 \pm 0.042 \pm 0.020$ |
| $J/\psi K_s (\pi^0 \pi^0)$ | $0.617 \pm 0.103 \pm 0.036$ |
| $\psi(2S) K_s$ | $0.947 \pm 0.112 \pm 0.062$ |
| $\chi_{c1} K_s$ | $0.759 \pm 0.170 \pm 0.037$ |
| $\eta_c K_s$ | $0.778 \pm 0.195 \pm 0.093$ |
| $J/\psi K^*$ | $0.477 \pm 0.271 \pm 0.155$ |
| $J/\psi K_s$ | $0.686 \pm 0.039 \pm 0.015$ |
| $J/\psi K_L$ | $0.735 \pm 0.074 \pm 0.067$ |
| $J/\psi K^0$ | $0.697 \pm 0.035 \pm 0.016$ |
| All | $0.714 \pm 0.032 \pm 0.018$ |

CP violation in Standard Model is not small, it is $O(1)$.
 Smallness of CPV in kaon decays is due to flavor suppression.
 CP-violating phases in New Physics can also be $O(1)$.

BaBar with 384×10^6 BB pairs: PRL 99, 171803 (2007)

$$\sin 2\beta = 0.714 \pm 0.032 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

Belle with 535×10^6 BB pairs: PRL 98, 031802 (2007)

$$\sin 2\beta = 0.642 \pm 0.031 \text{ (stat)} \pm 0.017 \text{ (syst)}$$

Decays dominated by gluonic penguins:

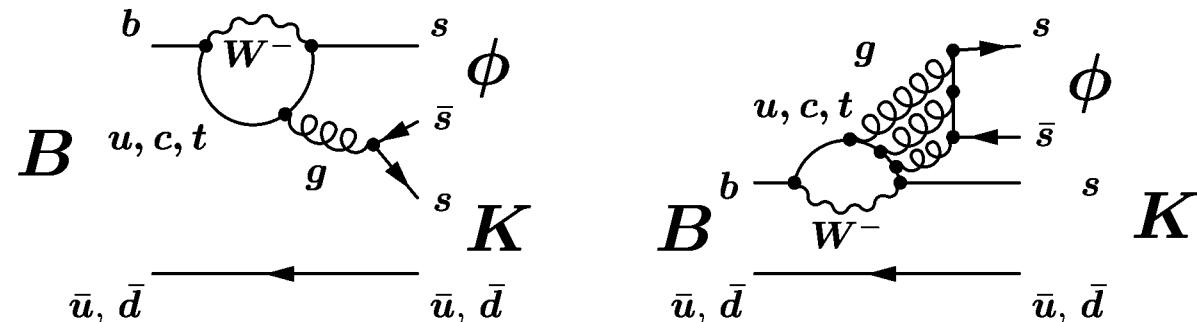
$B^0 \rightarrow \eta' K^0, \varphi K^0, K^+ K^- K_S, K_S \pi^0, K_S K_S K_S, \omega K_S, f_0 K_S, \text{etc.}$



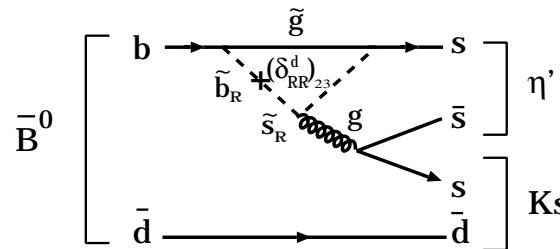
For example, consider

$B^0 \rightarrow \varphi K^0$ or $K_S K_S K_S$

$$b \rightarrow S\bar{S}S$$



- Tree-level SM contributions are absent
- All other SM contributions are strongly suppressed
- SM penguins dominated by top-quark loops
 - ⇒ in SM, direct CP violation is small, ~1%
 - ⇒ and time-dependent CP violation is the same as in the “golden” charmonium- K^0 modes
- Great sensitivity to non-SM physics in the loops!



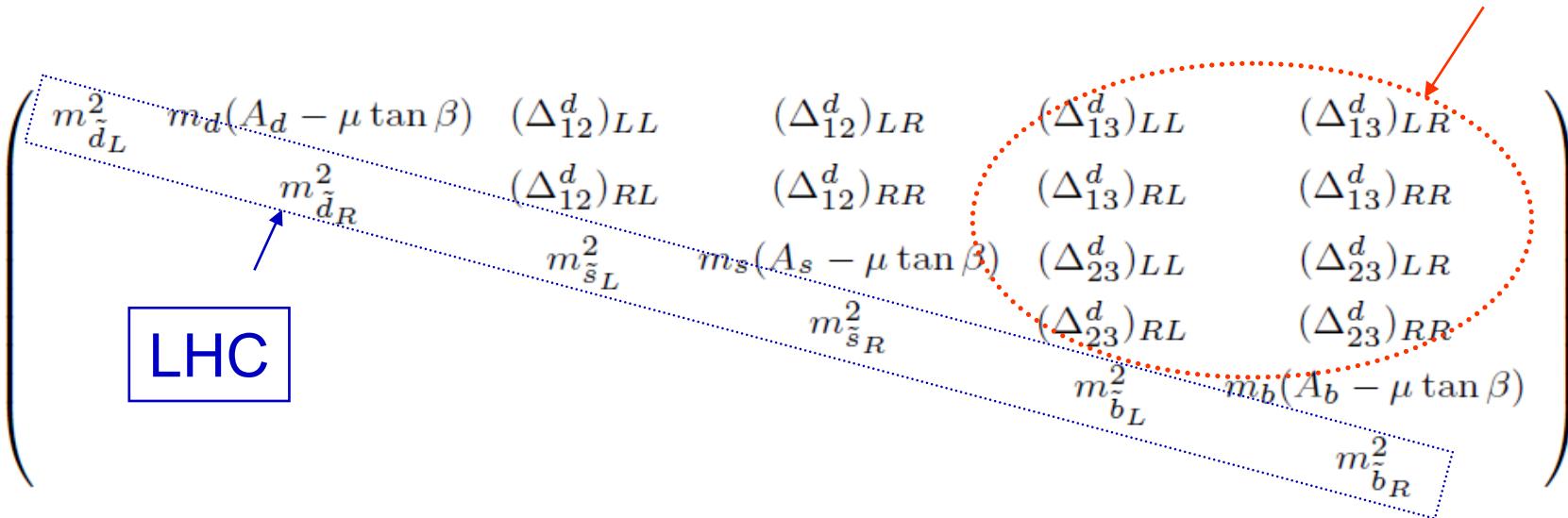
It is not easy for New Physics to hide in penguin-dominated decays unless its flavor and/or mass structure is very special



Decays dominated by gluonic penguins: Indirect limits on squark mixing



B-meson factories



Complementarity with the LHC is part of the physics case for a “Super B Factory”

New Physics near the electroweak scale (i.e., accessible at the LHC) that has a generic flavor-violation structure is ruled out by K^0-K^0 , B^0-B^0 , $B_s^0-B_s^0$ mixing and $b \rightarrow s\gamma$, $b \rightarrow sg$ measurements (“*the New Physics flavor problem*”). Flavor-blind New Physics is unnatural because Standard Model contains flavor violation in the Yukawa couplings. For supersymmetry, a solution is Minimal Flavor Violation, possibly with SM-like loop suppression

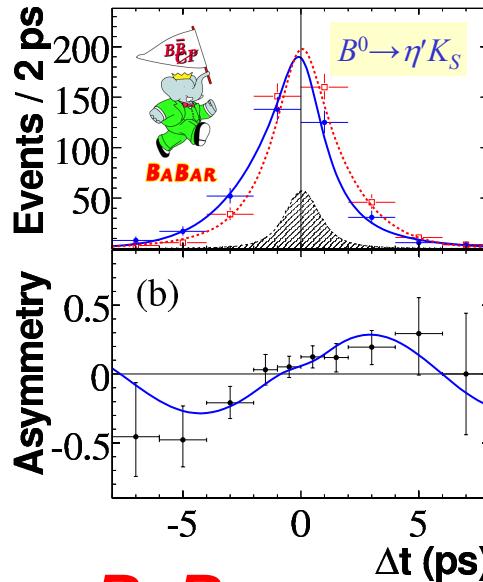


The highest-statistics penguin-dominated mode:

$$B^0 \rightarrow \eta' K_S$$



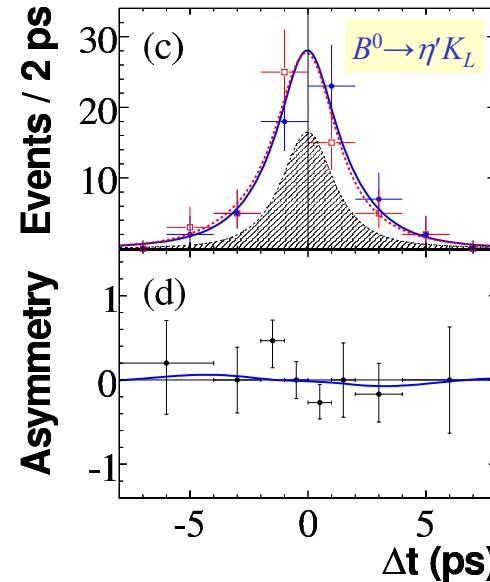
Back-to-back:
 BaBar: Phys.Rev.Lett. **98** (2007) 031801
 Belle: Phys.Rev.Lett. **98** (2007) 031802



BaBar

$$S_{\eta' K^0} = +0.58 \pm 0.10 \pm 0.03 \quad (5.5\sigma)$$

$$C_{\eta' K^0} = -0.16 \pm 0.07 \pm 0.03$$



Belle

$$S_{\eta' K^0} = +0.64 \pm 0.10 \pm 0.04 \quad (5.6\sigma)$$

$$C_{\eta' K^0} = +0.01 \pm 0.07 \pm 0.05$$

Measurements of S in $B^0 \rightarrow \eta' K^0$ by *BaBar* and then *Belle* are the **second** observations of CP violation in B mesons (Fall 2006)

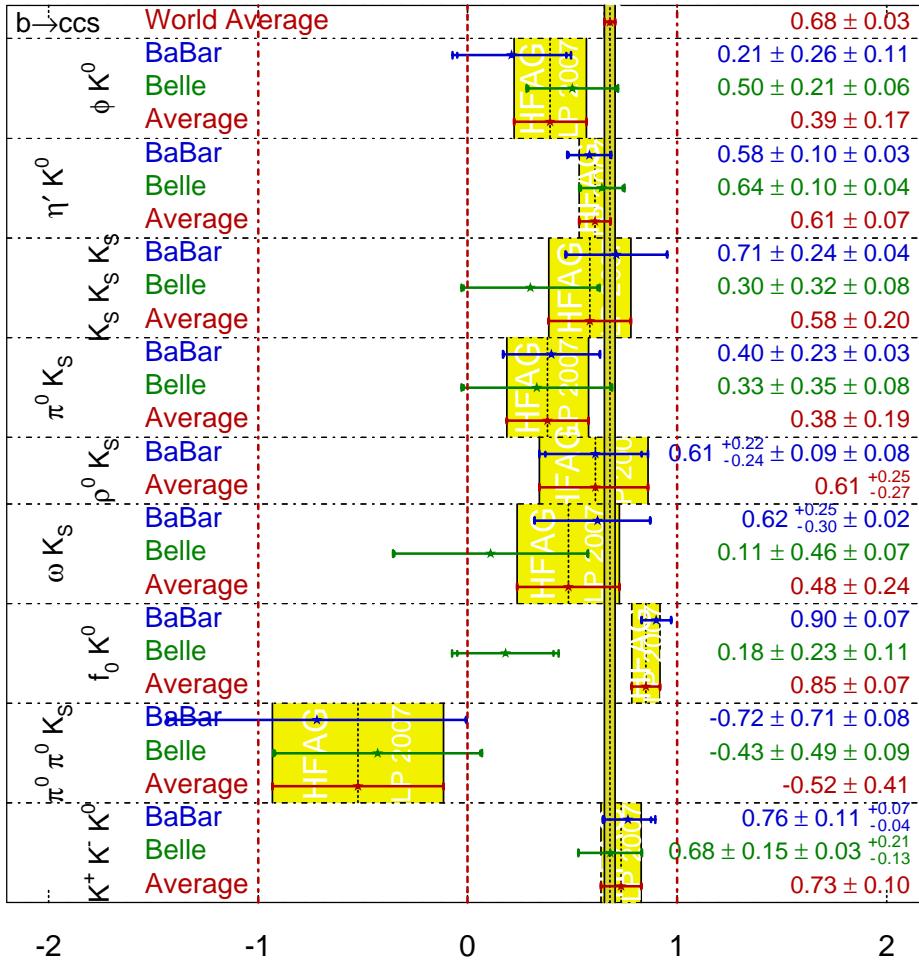
The world-average $\sin 2\beta$ in penguin modes is 2.2σ less than in the “golden” modes

In 2004, the difference was 3.7σ ...



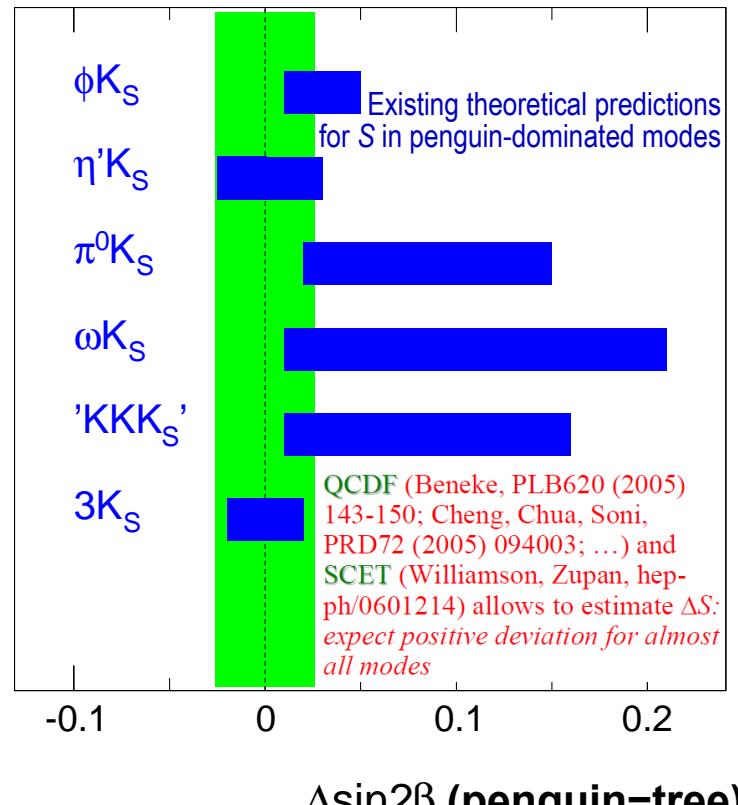
$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFAG
LP 2007
PRELIMINARY



This is a very naive average

$$\langle \sin 2\beta_{\text{golden}} \rangle = 0.680 \pm 0.025$$

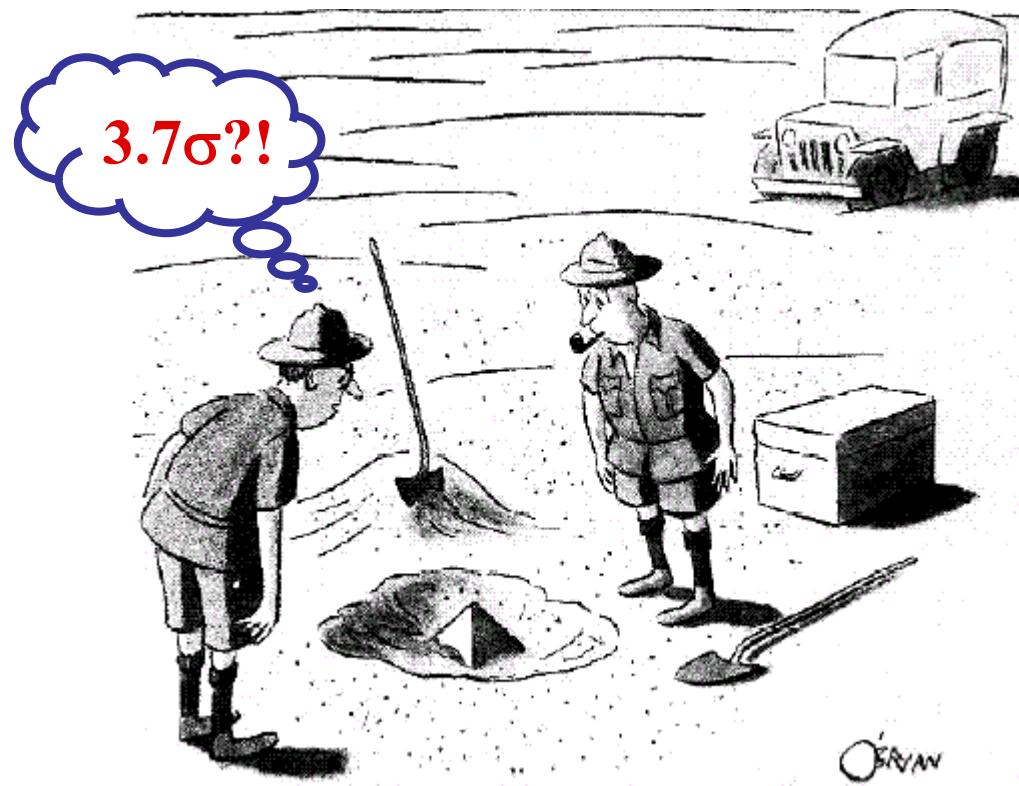


$$\langle \sin 2\beta_{\text{peng}} \rangle_{\text{naive}} = 0.56 \pm 0.05 (\chi^2 = 19/16 \text{ dof})$$

<http://www.slac.stanford.edu/xorg/hfag/triangle/summer2007/index.shtml>



What do we make of this discrepancy?



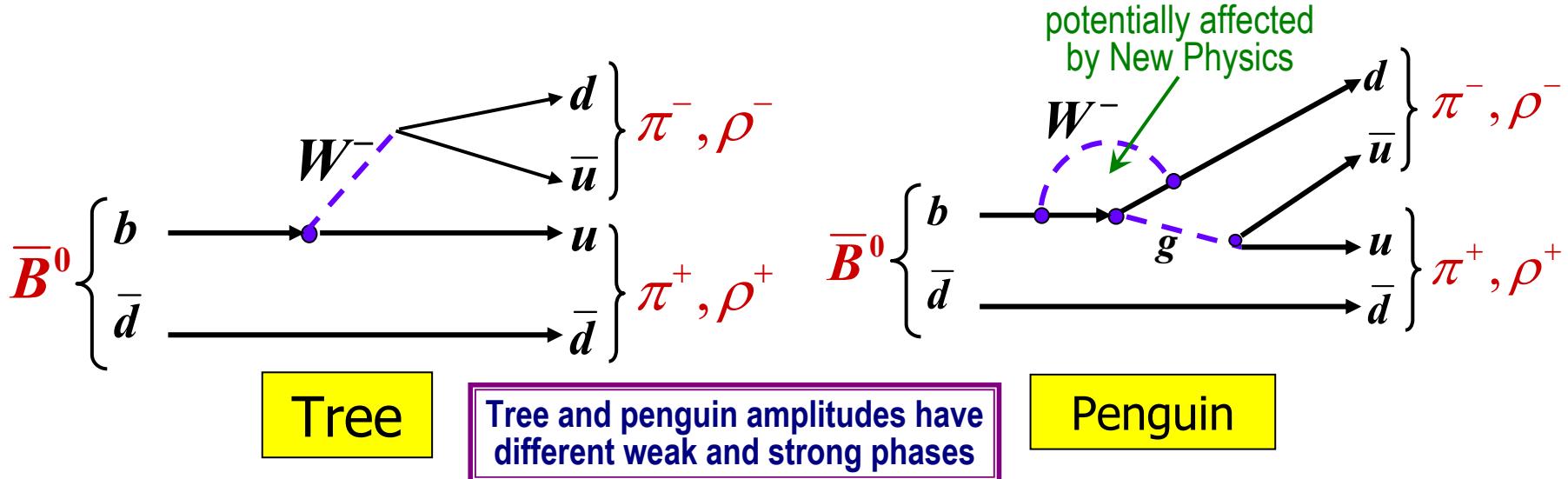
*"This could be the greatest discovery of the century.
Depending, of course, on how far down it goes..."*

Measuring α

$\mathcal{A}_{CP}(t)$ in $b \rightarrow u\bar{u}d$ decay to a CP eigenstate at the tree level:

Measure $180^\circ - \beta - \gamma = \alpha \equiv \arg \left[\frac{-V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right]$ (in SM)

Penguins: $\mathcal{A}_{CP}(t) \Rightarrow \sin(2\alpha_{\text{eff}})$; $\alpha_{\text{eff}} = \alpha - \Delta\alpha$; direct $\mathcal{A}_{CP} \neq 0$



SU(2) isospin analysis in $B \rightarrow \pi\pi, \rho\rho$

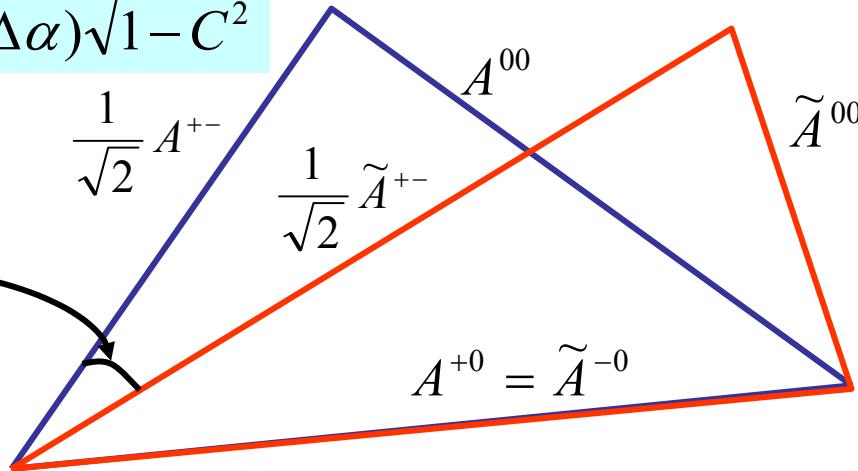


Determines relative phase between B^0 mixing and the tree, independent of the EW model

M. Gronau, D. London, Phys. Rev. Lett. **65**, 3381 (1990)

$$S = \sin(2\alpha + 2\Delta\alpha)\sqrt{1 - C^2}$$

$2\Delta\alpha$



In $B \rightarrow \rho\rho$, there are 3 such relations (one for each polarization)

6 unknowns, 6 observables in $\pi\pi$ (there is no vertex to measure $S_{\pi^0\pi^0}$)

5 observables in $\rho\rho$ (or 7, when both $C_{\rho^0\rho^0}$ and $S_{\rho^0\rho^0}$ are measured)

4-fold ambiguity in $2\Delta\alpha$: either triangle can flip up or down

$$A_{hh} = e^{+i\gamma} T + e^{-i\beta} P$$

Neglecting EW penguins, ± 0 is a pure tree mode, and so the two triangles share a common side:

$$\tilde{A}_{hh} = e^{-i\gamma} T + e^{+i\beta} P$$

$$A(B^+ \rightarrow h^+ h^0) = \tilde{A}(B^- \rightarrow h^- h^0)$$

| |
|---|
| $A^{+-} = A(B^0 \rightarrow \pi^+ \pi^-)$ |
| $\tilde{A}^{+-} = A(\bar{B}^0 \rightarrow \pi^+ \pi^-)$ |
| $A^{00} = A(B^0 \rightarrow \pi^0 \pi^0)$ |
| $\tilde{A}^{00} = A(\bar{B}^0 \rightarrow \pi^0 \pi^0)$ |
| $A^{+0} = A(B^+ \rightarrow \pi^+ \pi^0)$ |
| $\tilde{A}^{-0} = A(B^- \rightarrow \pi^- \pi^0)$ |

| |
|---|
| $A^{+0} = \frac{1}{\sqrt{2}} A^{+-} + A^{00}$ |
| $\tilde{A}^{-0} = \frac{1}{\sqrt{2}} \tilde{A}^{+-} + \tilde{A}^{00}$ |

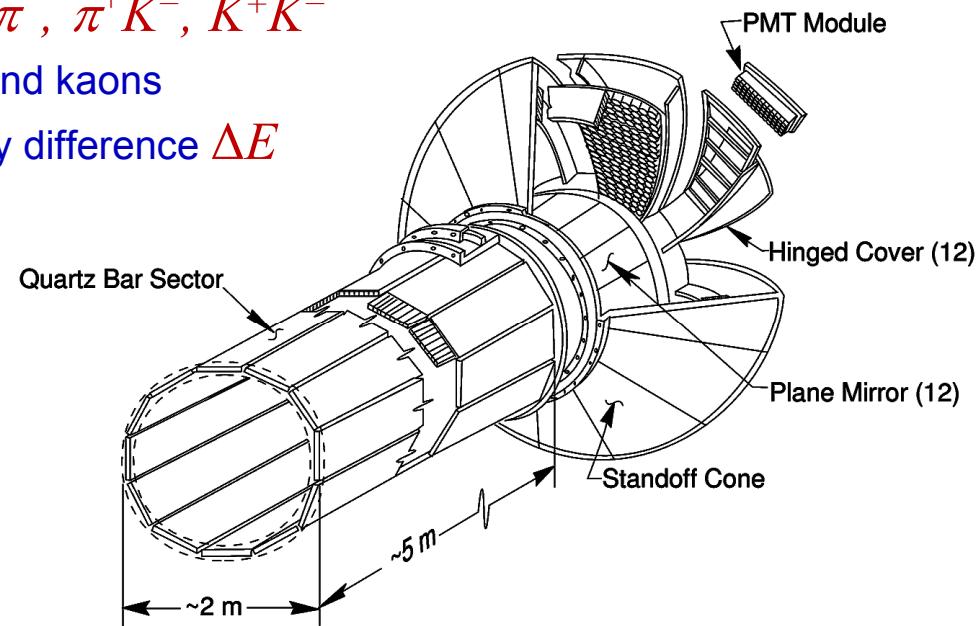
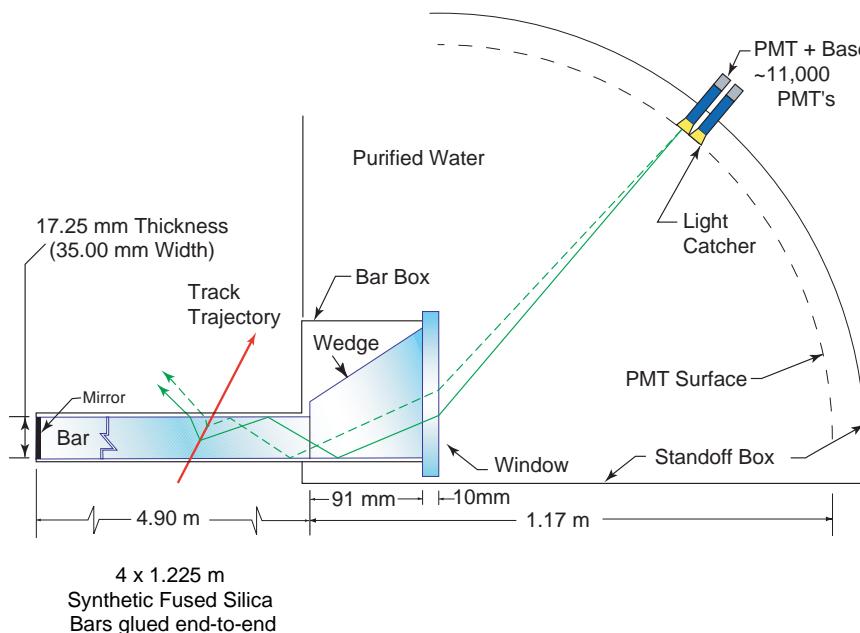
Knowledge of A^{00} is the primary limiting factor in the isospin analysis

The “classic” $B^0 \rightarrow h^+h^-$ analysis

Simultaneous ML fit to $B^0 \rightarrow \pi^+\pi^-, K^+\pi^-, \pi^+K^-, K^+K^-$

Using DIRC Cherenkov angle to identify pions and kaons

Additional $\pi\pi/K\pi/KK$ separation from energy difference ΔE



DIRC: 144 quartz bars
 $0.84 \times 4\pi$ coverage; 91% eff. with $n_\gamma > 5$
 13σ π/K separation at 1.5 GeV/c, 2.5 σ at 4.5 GeV/c
 Calibration sample: $B^- \rightarrow \pi^- D^0$, $D^0 \rightarrow \pi^+ K^-$



π/K separation with DCH dE/dx :

Catching up with Belle's $B^0 \rightarrow h^+h^-$ reconstruction efficiency



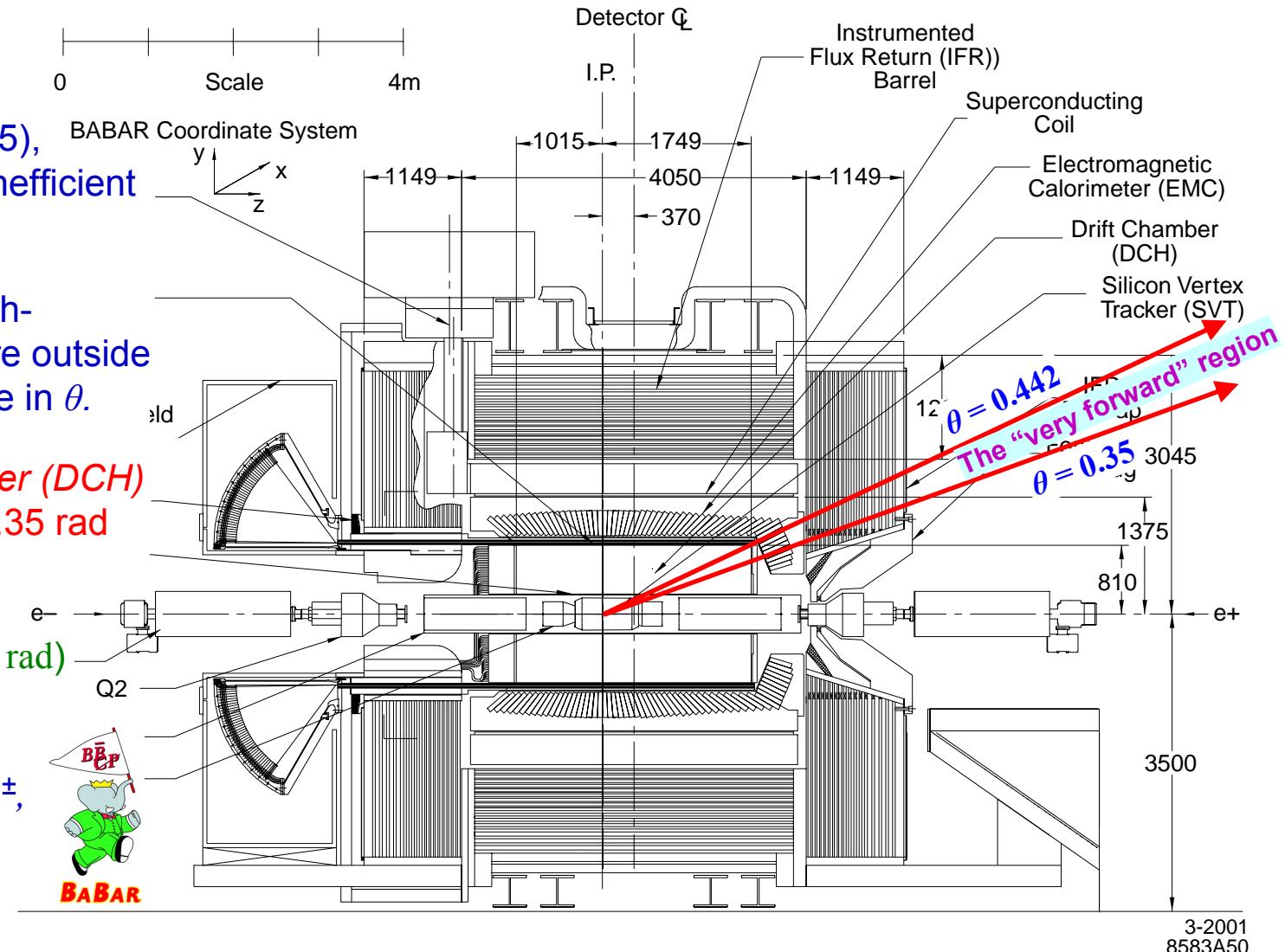
In the barrel ($\theta > 0.445$),
the DIRC is $\sim 9.3\%$ inefficient
(ϕ cracks, etc.)

Another $\sim 12\%$ of high-momentum tracks are outside
the DIRC acceptance in θ .

We use Drift Chamber (DCH)
tracks down to $\theta = 0.35$ rad

$(J/\psi \rightarrow \mu^+\mu^-)$ in $\sin 2\beta$
analysis: down to 0.30 rad)

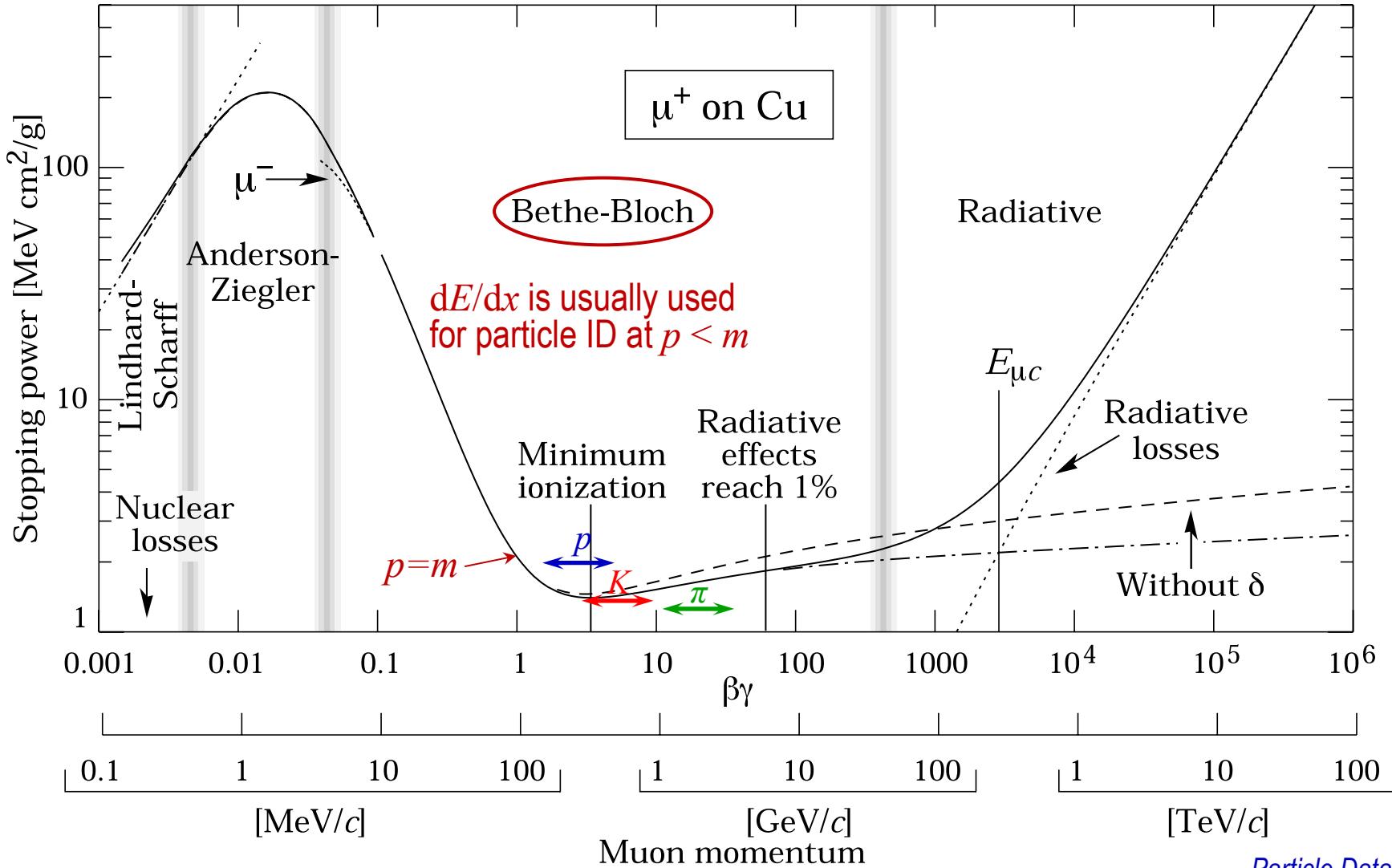
→ 16% event-yield
increase for $B \rightarrow Xh^\pm$,
35% for $B^0 \rightarrow h^+h^-$



BABAR

3-2001
8583A50

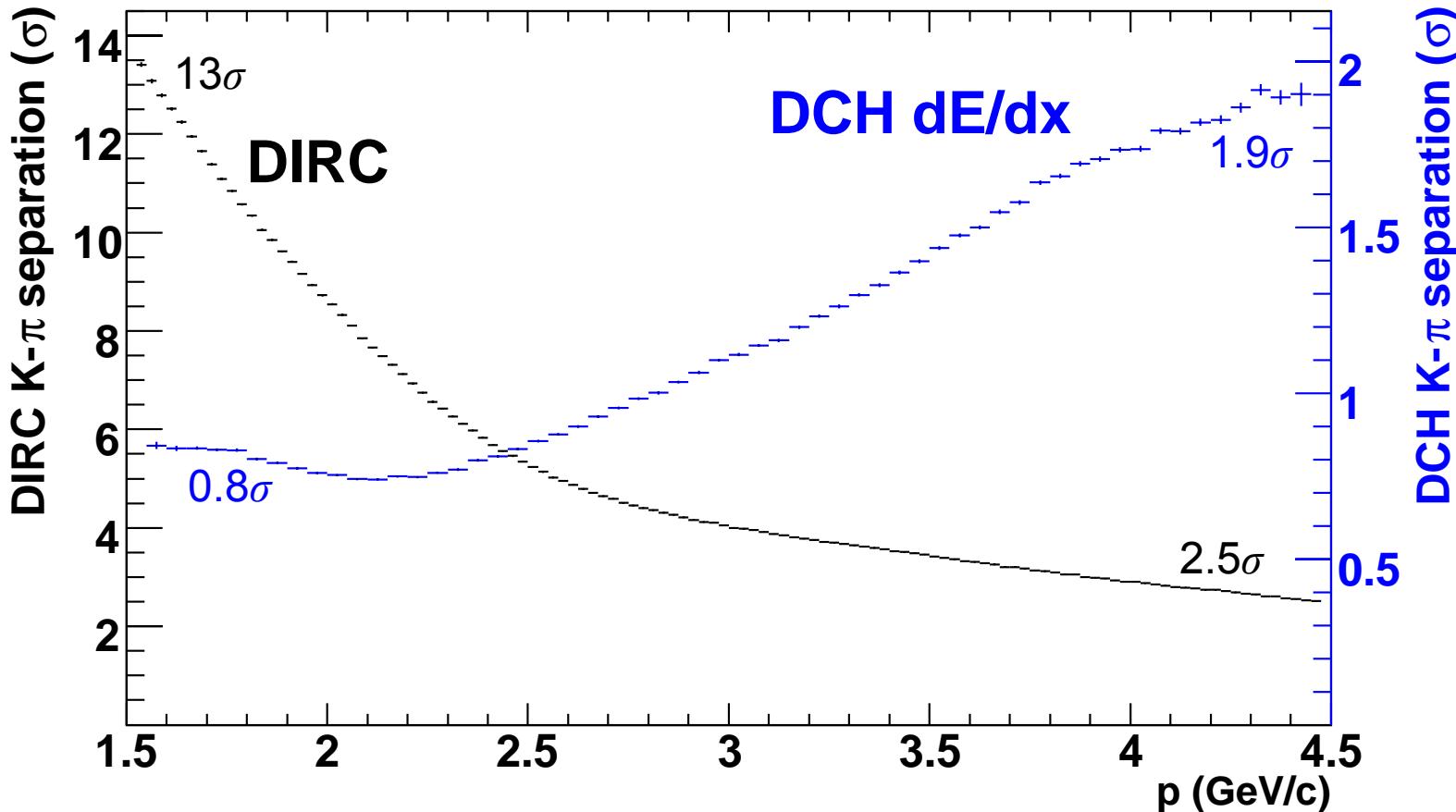
Ionization energy loss for $B \rightarrow X h^\pm$ momenta



Particle Data Group

DCH dE/dx $K\text{-}\pi$ separation in $B \rightarrow X h^\pm$

complementary to DIRC



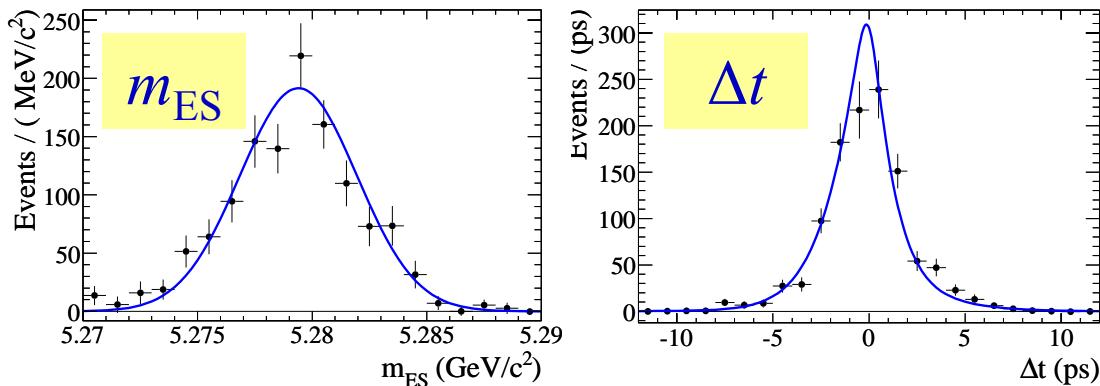
(for tracks that have good DIRC information, we use both DIRC and dE/dx)

Our new result: $B^0 \rightarrow \pi^+ \pi^-$

$$N_{\pi^+ \pi^-} = 1139 \pm 49$$

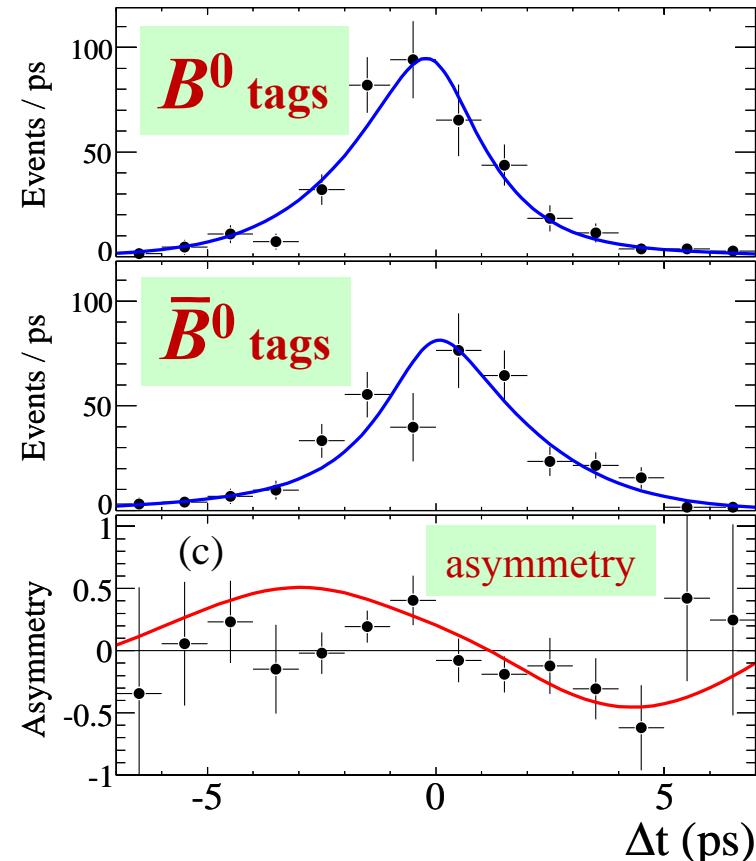
**52% overall increase
in signal reconstruction efficiency:**

35% from DCH dE/dx ,
13% mainly from reoptimizing the event-shape $|\cos\theta_{\text{spher}}|$ cut



sPlot:

Builds a histogram of x excluding it from the Maximum-Likelihood fit, assigning a weight to each event, keeping all signal events, getting rid of all background events, and keeping track of the statistical errors in each x bin



M. Pivk and F. R. Le Diberder,
“sPlot: a statistical tool to unfold data distributions,”
Nucl. Instrum. Meth. A **555**, 356 (2005)
[arXiv:physics/0402083]

Observation of CP Violation in $B^0 \rightarrow K^+ \pi^-$ and $B^0 \rightarrow \pi^+ \pi^-$

BaBar has made a 5.4σ observation of CP violation in $B^0 \rightarrow \pi^+ \pi^-$

$$S_{\pi\pi} = -0.60 \pm 0.11 \pm 0.03 \quad (5.1\sigma)$$

$$C_{\pi\pi} = -0.21 \pm 0.09 \pm 0.02 \quad (2.3\sigma)$$

BaBar: 383 million $B\bar{B}$ pairs, $1139 \pm 49 \pi^+ \pi^-$

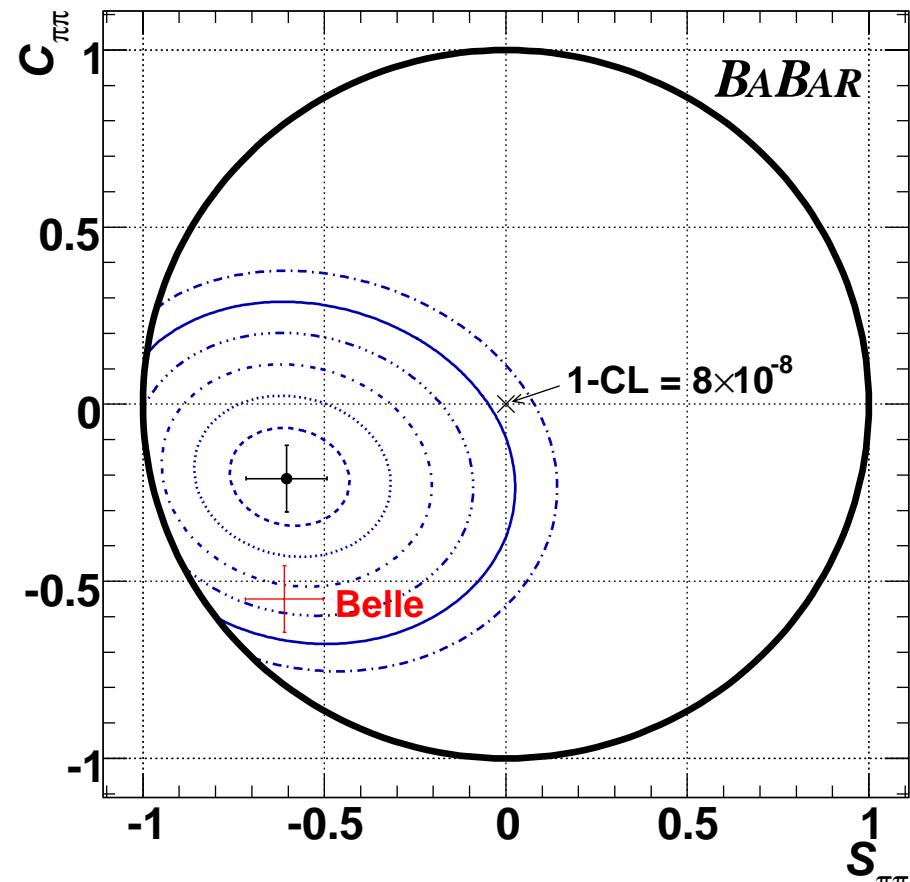
Belle: 535 million $B\bar{B}$ pairs, $1464 \pm 65 \pi^+ \pi^-$

Belle

PRL 98, 211801 (2007)

$$S_{\pi\pi} = -0.61 \pm 0.10 \pm 0.04 \quad (5.3\sigma)$$

$$C_{\pi\pi} = -0.55 \pm 0.08 \pm 0.05 \quad (5.5\sigma)$$



also:

$$\mathcal{A}_{K^+ \pi^-} = -0.107 \pm 0.018 {}^{+0.007}_{-0.004} \quad (5.5\sigma)$$

The $B \rightarrow \pi^\pm \pi^0, \pi^0 \pi^0$ analysis

Simultaneous fit to $B^0 \rightarrow \pi^+ \pi^0, K^+ \pi^0$ (using DIRC Cherenkov angle to separate pions and kaons)
 $B^0 \rightarrow \pi^0 \pi^0$: branching fraction and time-integrated direct CP asymmetry

new: in addition to $\pi^0 \rightarrow \gamma\gamma$, we use *merged* π^0 and $\gamma \rightarrow e^+e^-$ conversions
 $\Rightarrow 10\%$ efficiency increase per π^0 (4% from merged π^0 , 6% from γ conversions)

At a Super B -meson factory, $\gamma \rightarrow e^+e^-$ conversions would make $S_{\pi^0 \pi^0}$ determination possible!

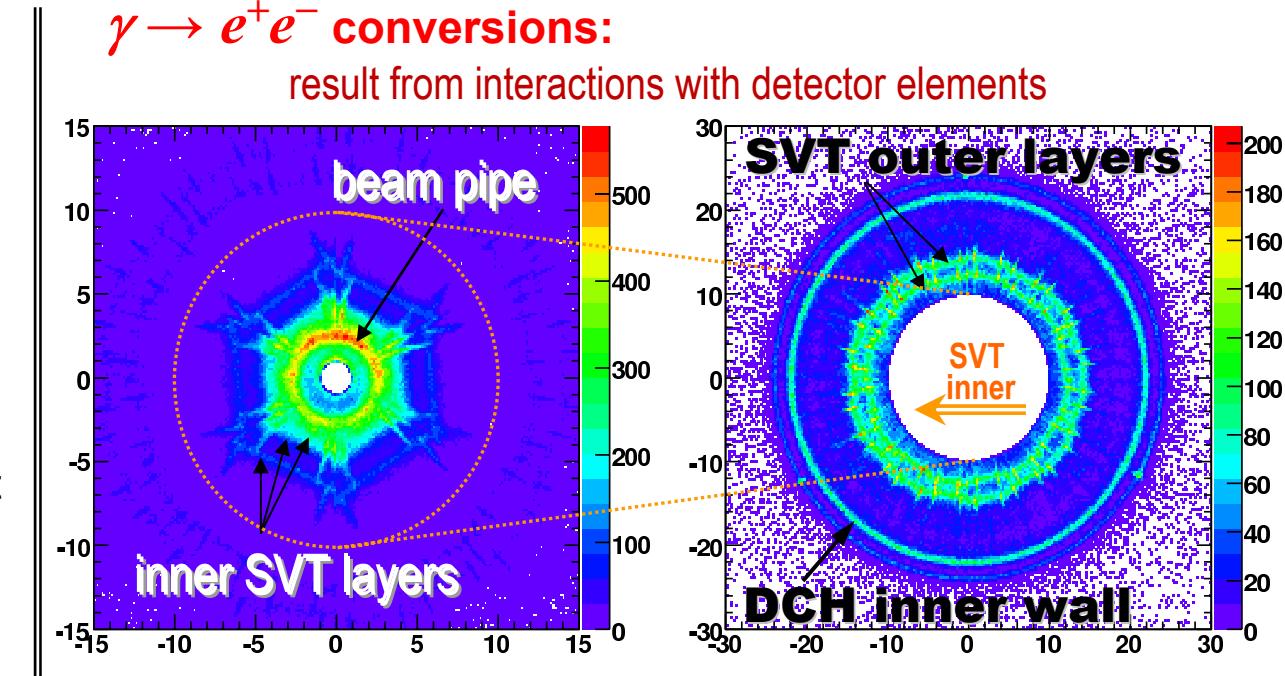
merged π^0 :

the two photons are too close to one another in the calorimeter to be reconstructed individually; can be recovered using

$$M_{\pi^0}^2 \approx E_{\pi^0}^2 (S_{\pi^0} - S_\gamma),$$

where S is the second EMC moment of the merged $\pi^0 \rightarrow \gamma\gamma$

The control sample: $\tau \rightarrow \rho\nu$



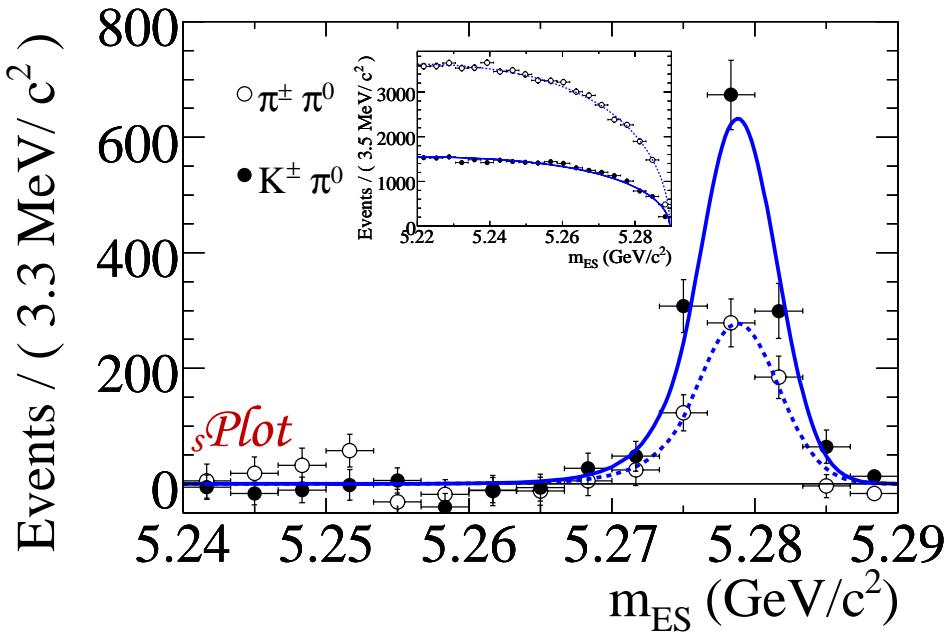
New BaBar results: $B \rightarrow \pi^\pm \pi^0, \pi^0 \pi^0$



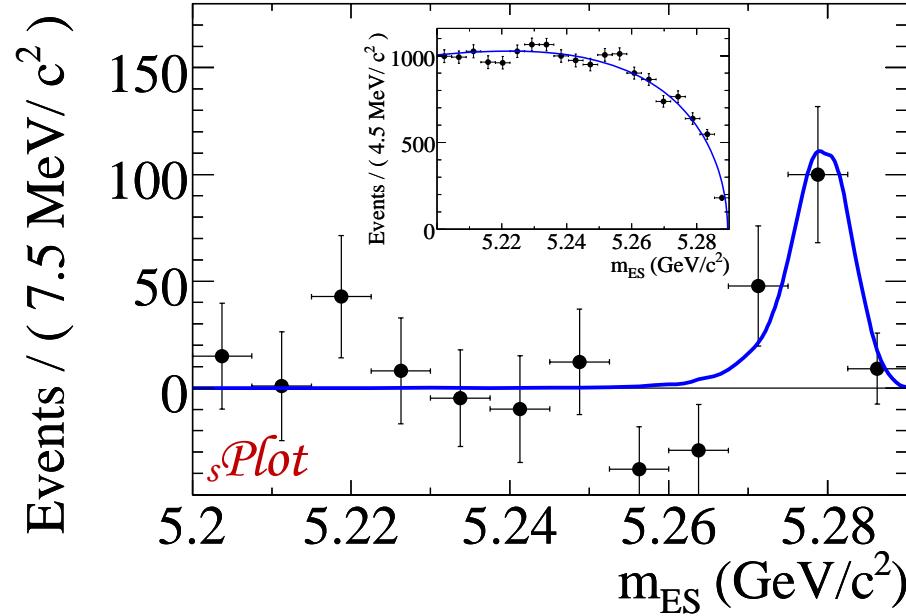
$383 \times 10^6 BB$ pairs

PRD 76, 091102 (2007)

$$N_{\pi^\pm \pi^0} = 627 \pm 58$$



$$N_{\pi^0 \pi^0} = 154 \pm 27$$



$$\mathcal{Br}_{\pi^\pm \pi^0} = (5.02 \pm 0.46 \pm 0.29) \times 10^{-6}$$

$$\mathcal{Br}_{\pi^0 \pi^0} = (1.47 \pm 0.25 \pm 0.12) \times 10^{-6}$$

$$\mathcal{A}_{\pi^\pm \pi^0} = 0.03 \pm 0.08 \pm 0.01$$

$$C_{\pi^0 \pi^0} = -0.49 \pm 0.35 \pm 0.05$$



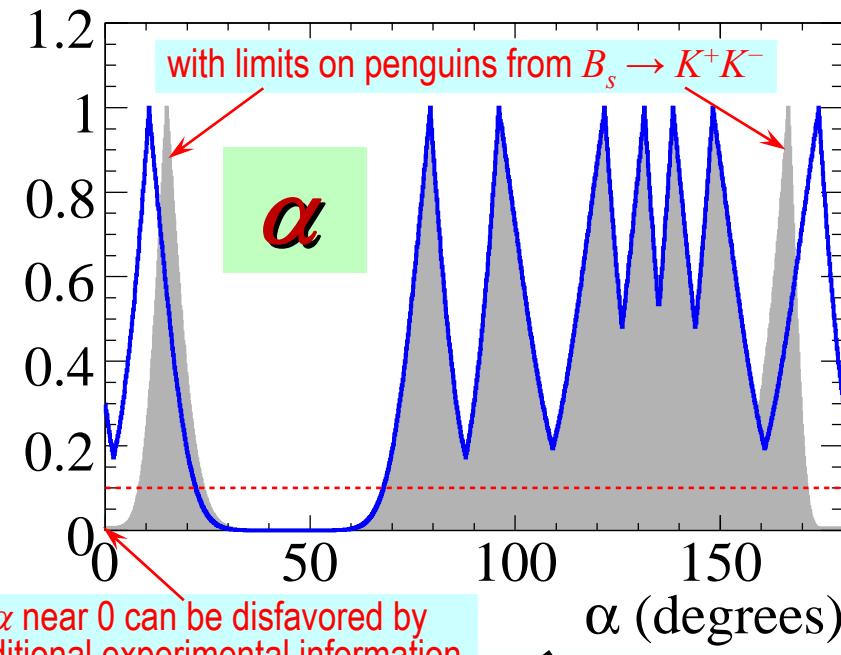
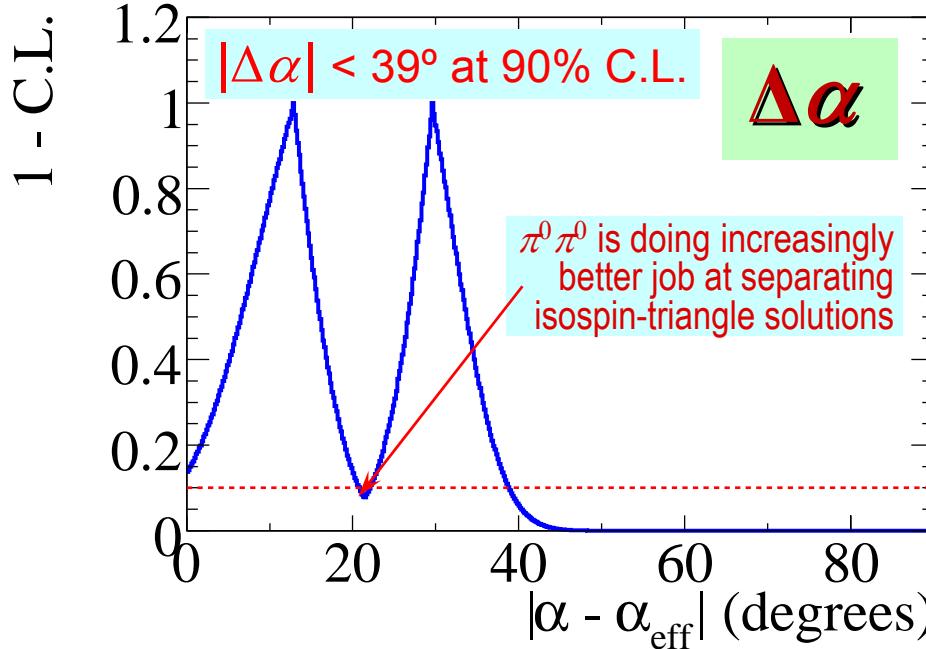
An interpretation of our new $B \rightarrow \pi\pi$ results



BABAR

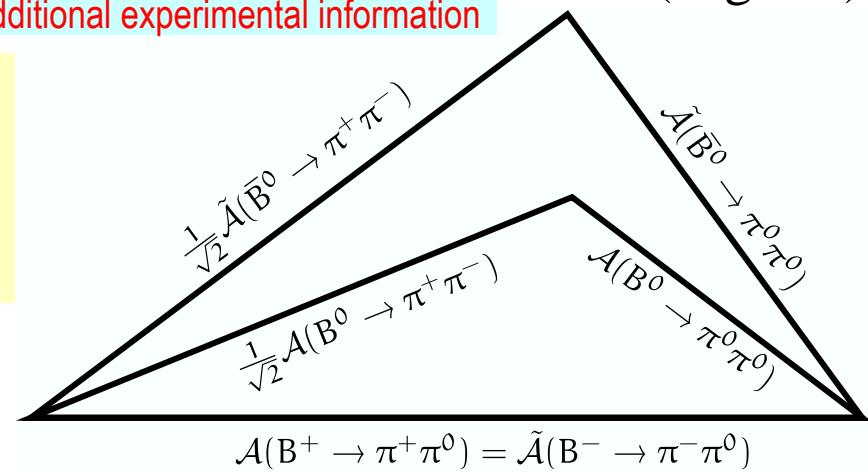
383x10⁶ BB pairs

PRD 76, 091102 (2007)



This is a frequentist interpretation: we use only the $B \rightarrow \pi\pi$ isospin-triangle relations in arriving at these constraints on $\Delta\alpha = \alpha - \alpha_{\text{eff}}$ and on α itself

Here is one of the possible solutions to the Gronau-London isospin triangle in $B \rightarrow \pi\pi$ according to the central values of the Summer 2006 BaBar results:



$B \rightarrow \rho\rho$ angular analysis

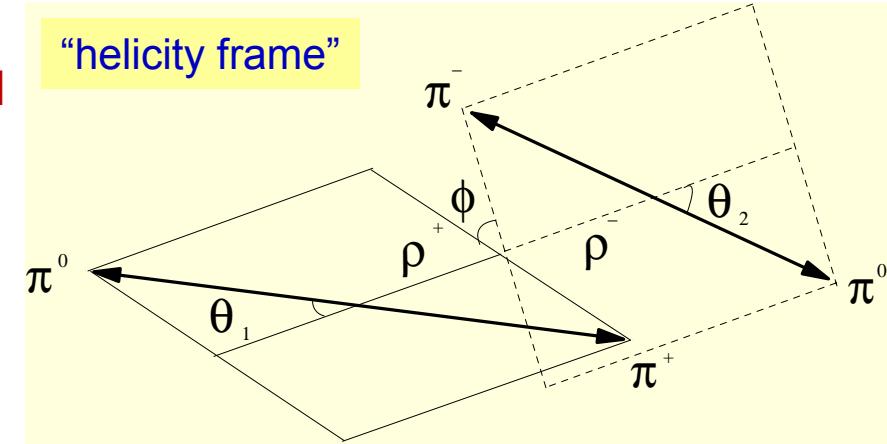
$B \rightarrow \rho\rho$ is a vector-vector state; angular analysis is required to determine CP content:

Longitudinal: $A_0 = -\frac{1}{\sqrt{3}}S + \sqrt{\frac{2}{3}}D$ pure $CP = +1$

Transverse $A_{+1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D + \frac{1}{\sqrt{2}}P$

Transverse $A_{-1} = \frac{1}{\sqrt{3}}S + \frac{1}{\sqrt{6}}D - \frac{1}{\sqrt{2}}P$

transverse
is not a CP
eigenstate



Fortunately, the fraction f_L of the helicity-zero state in $B \rightarrow \rho\rho$ decays is very close to 1:

$$f_L(B^0 \rightarrow \rho^+ \rho^-)_{\text{WA}} = 0.978^{+0.025}_{-0.022}$$

$$f_L(B^\pm \rightarrow \rho^\pm \rho^0)_{\text{WA}} = 0.912^{+0.044}_{-0.045}$$

New BaBar result:

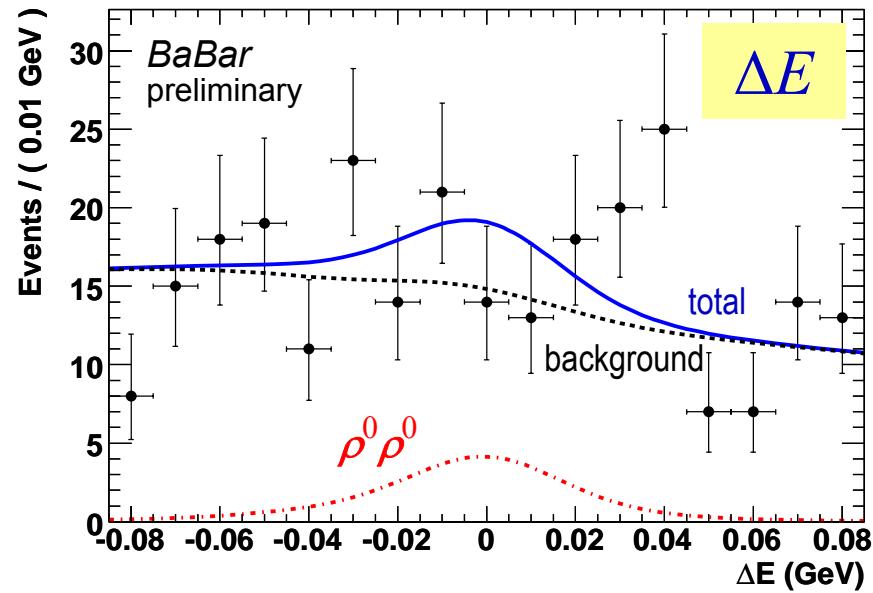
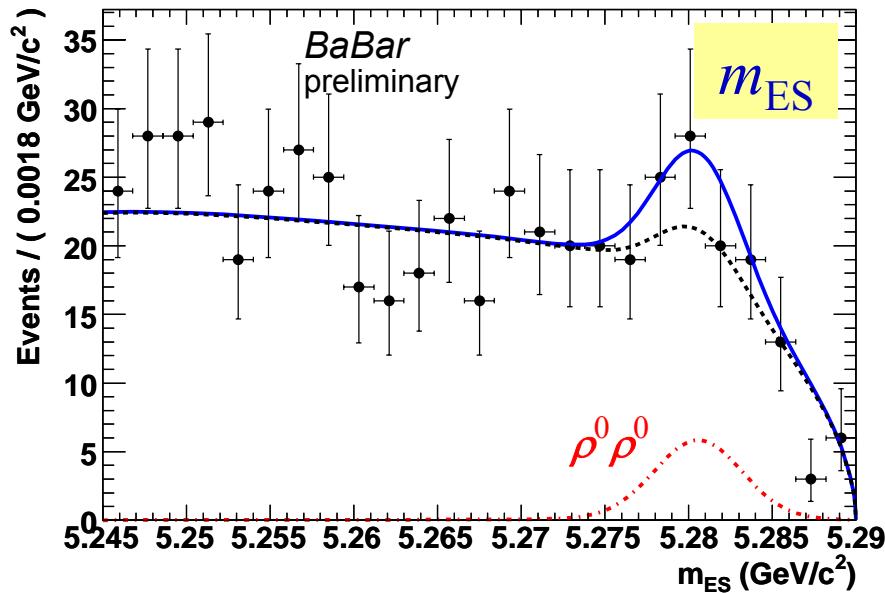
3.6 σ evidence for $B^0 \rightarrow \rho^0 \rho^0$

427x10⁶ BB pairs
BaBar-CONF-07/012



$$N_{\rho^0 \rho^0} = 85 \pm 28 \pm 17$$

A time-dependent analysis was successfully performed, despite the limited statistics

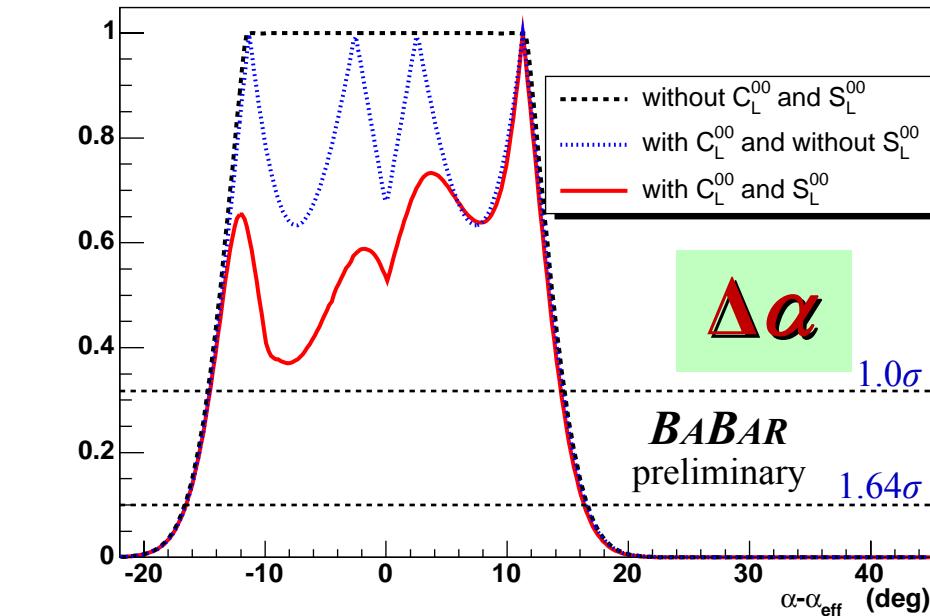
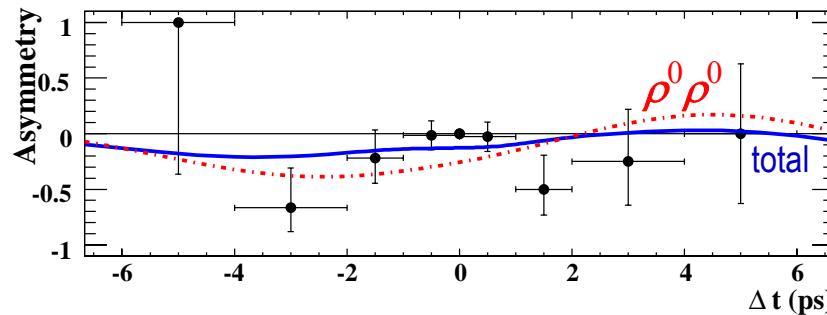
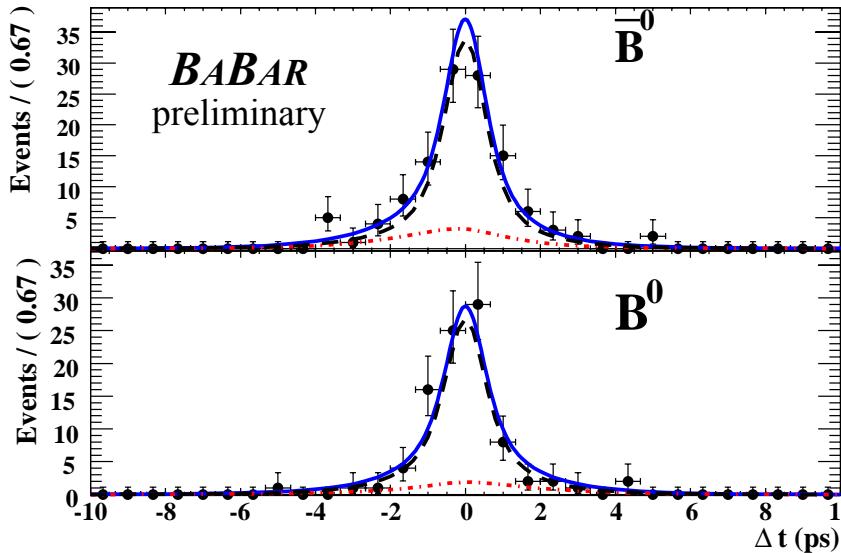


$$\mathcal{Br}_{\rho^0 \rho^0} = (0.84 \pm 0.29 \pm 0.17) \times 10^{-6}$$

$$f_L(B^0 \rightarrow \rho^0 \rho^0) = 0.70 \pm 0.14 \pm 0.05$$

An interpretation of the new $B \rightarrow \rho\rho$ results

427×10^6 BB pairs
BaBar-CONF-07/012



$$S_{\text{Long}}^{00} = 0.5 \pm 0.9 \pm 0.2$$

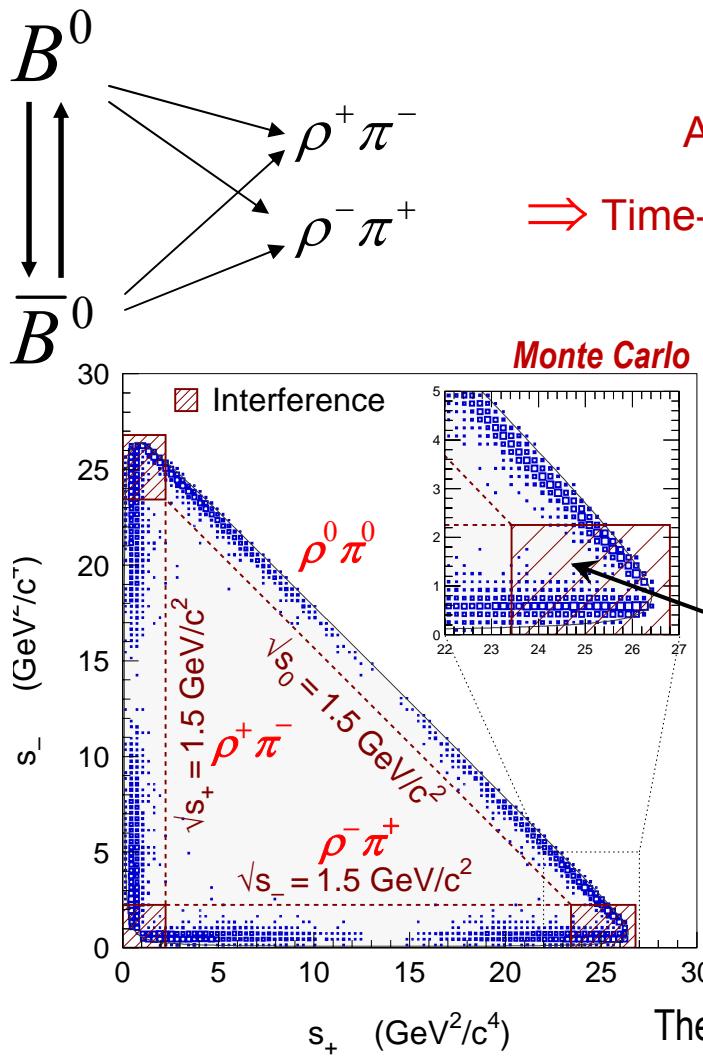
$$C_{\text{Long}}^{00} = 0.4 \pm 0.9 \pm 0.2$$

$|\Delta\alpha| < 14.5^\circ$ at 68% C.L.

$|\Delta\alpha| < 16.5^\circ$ at 90% C.L.

This is a frequentist interpretation: we use only the $B \rightarrow \rho\rho$ branching fractions, polarization fractions and isospin-triangle relations in arriving at these constraints on $\Delta\alpha = \alpha - \alpha_{\text{eff}}$

$B^0 \rightarrow (\rho\pi)^0$: Dalitz-plot analysis



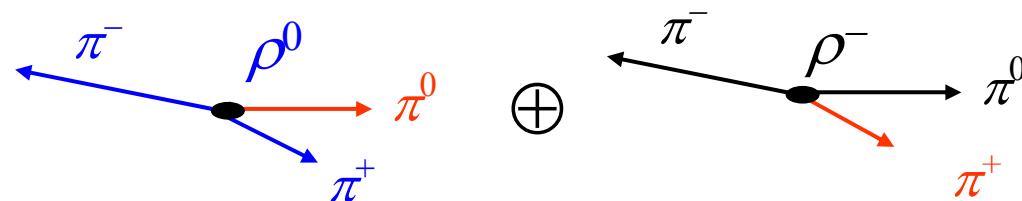
An isospin-pentagon analysis method exists but is not fruitful

⇒ Time-dependent Dalitz-plot analysis assuming isospin symmetry,
measuring 26 coefficients of the bilinear form factors
A. Snyder and H. Quinn, Phys. Rev. D, 48, 2139 (1993)

$$A(B^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ A(\rho^+ \pi^-) + f_- A(\rho^- \pi^+) + f_0 A(\rho^0 \pi^0)$$

$$\tilde{A}(\bar{B}^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ \tilde{A}(\rho^+ \pi^-) + f_- \tilde{A}(\rho^- \pi^+) + f_0 \tilde{A}(\rho^0 \pi^0)$$

Interference in the corners of the Dalitz plot provides information on **strong phases** between resonances



The $\rho(1450)$ and $\rho(1700)$ resonances are also included in this analysis

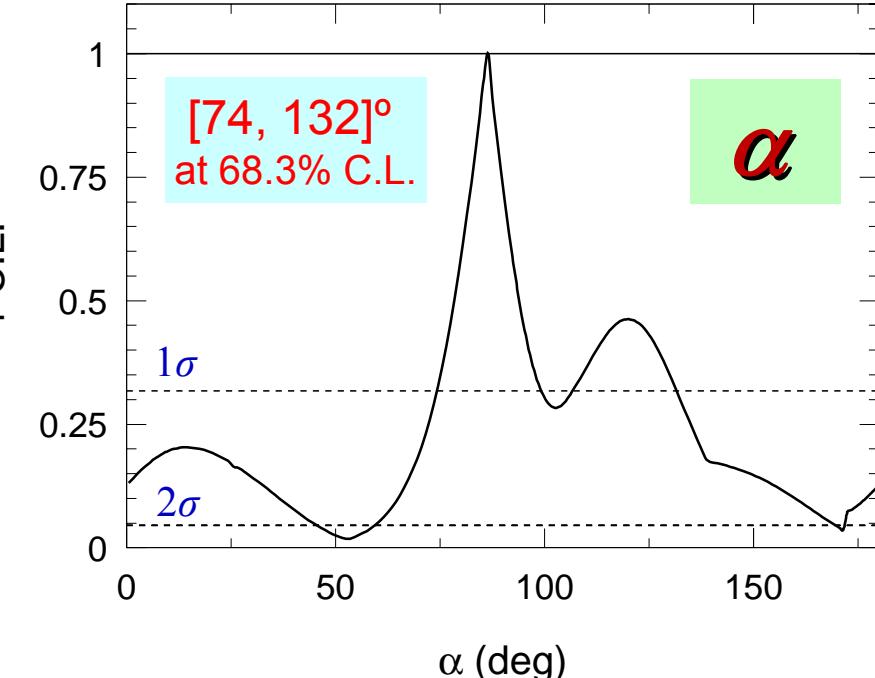
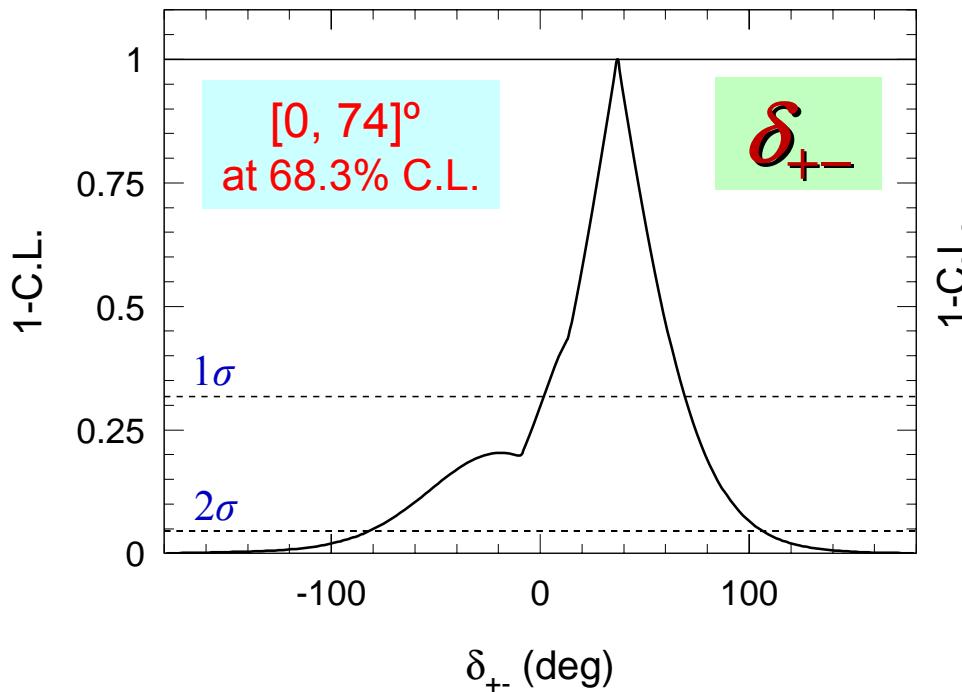
An interpretation of the new $B^0 \rightarrow (\rho\pi)^0$ results

375×10^6 BB pairs
PRD 76, 012004 (2007)



DEI SVB NVMINE VIGET

$\delta_{+-} = \arg(A^{+*}A^-)$: the relative phase between the amplitudes of $B^0 \rightarrow \rho^-\pi^+$ and $B^0 \rightarrow \rho^+\pi^-$



The constraint on α from $B^0 \rightarrow (\rho\pi)^0$ is relatively weak – but free from ambiguities!

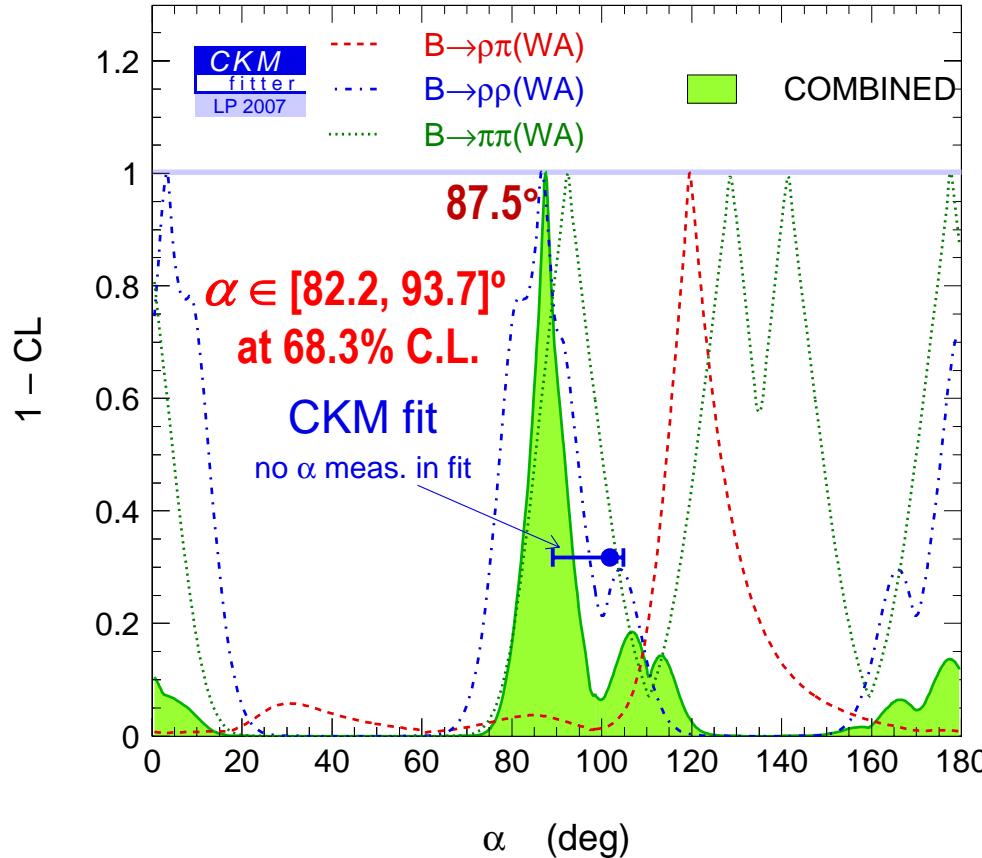
Global fits for the value of α



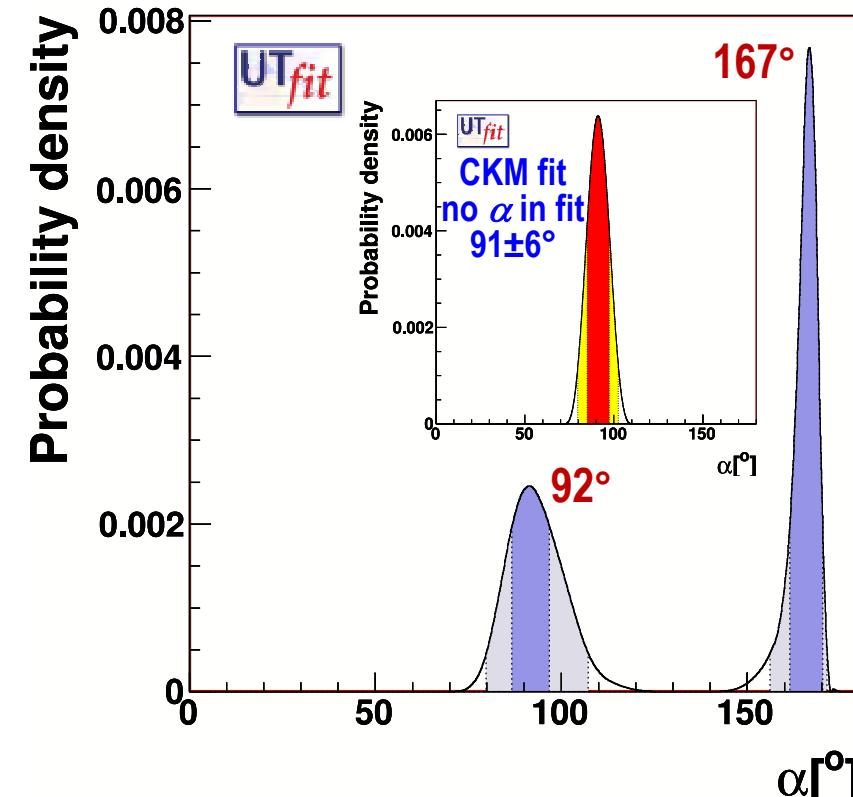
The second-highest-precision test of the KM mechanism of CP violation in meson decays

Two interpretations currently exist that convert the $B \rightarrow \pi\pi, \rho\pi, \rho\rho$ measurements to constraints on α :

A frequentist interpretation



A Bayesian interpretation, with model-dependent choices of priors



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C**41**, 1-131 (2005) [hep-ph/0406184],
updated results and plots available at <http://ckmfitter.in2p3.fr>

M. Ciuchini, G. D'Agostini, E. Franco, V. Lubicz, G. Martinelli, F. Parodi, P. Roudeau, A. Stocchi, JHEP **0107** (2001) 013 [hep-ph/0012308],
updated results and plots available at <http://www.utfit.org>



γ : the hardest to measure directly

Several techniques are combined, but the constraint is still rather weak



Time-dependent: $\sin(2\beta + \gamma)$ from $b \rightarrow c$, $b \rightarrow u$ interference + B^0 mixing

- $B^0 \rightarrow D^\mp \pi^\pm, D^{*\mp} \pi^\pm, D^\mp \rho^\pm$: limited sensitivity due to smallness of $r = |A(b \rightarrow u)/A(b \rightarrow c)|$
- $B^0 \rightarrow D^\mp K^0 \pi^\pm$ Dalitz plot (mostly through $B^0 \rightarrow \bar{D}^{**0} K_S^0$ and $B^0 \rightarrow D^- K^{*+}$)

Not time-dependent: γ from $b \rightarrow c$, $b \rightarrow u$ interference

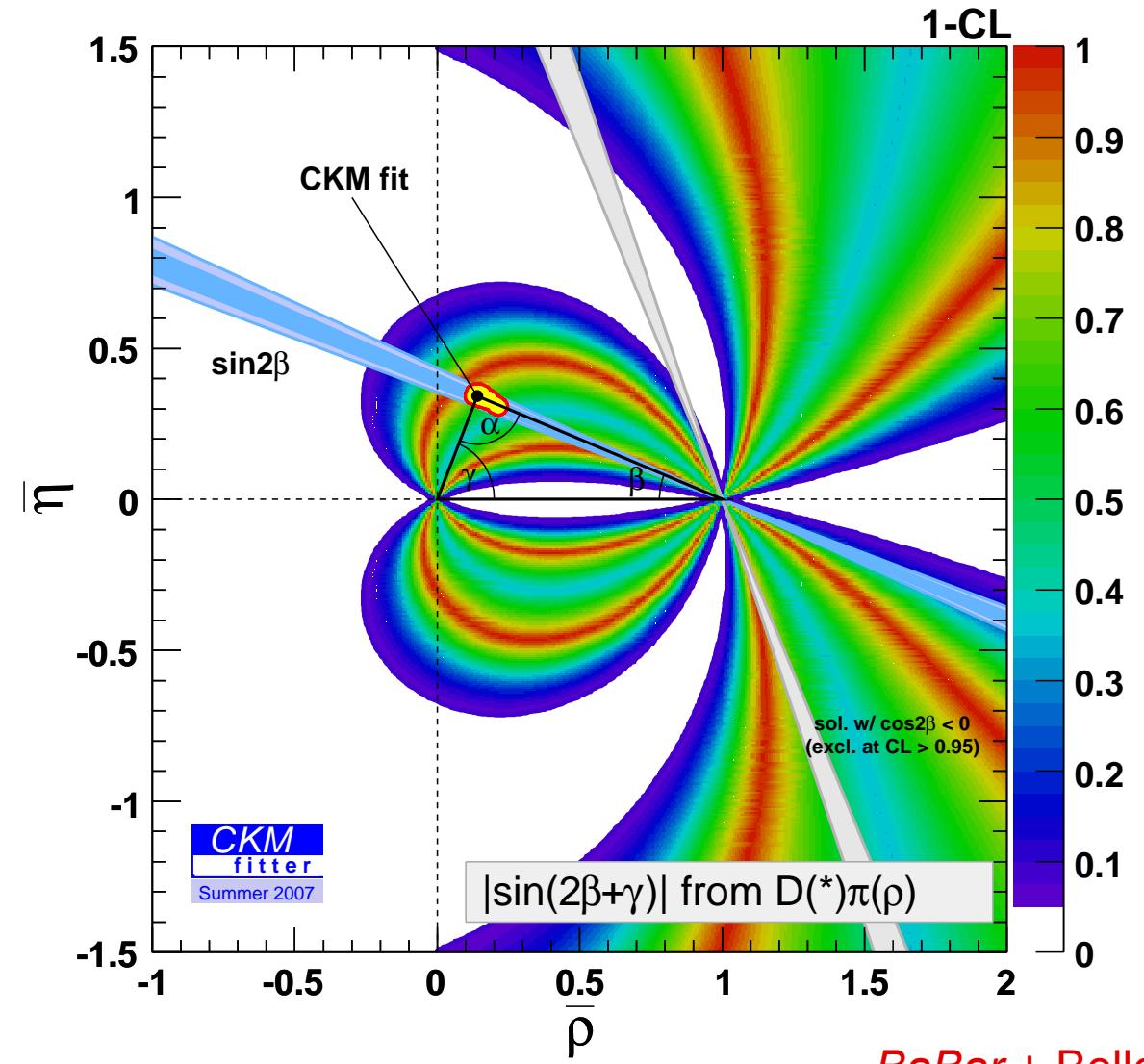
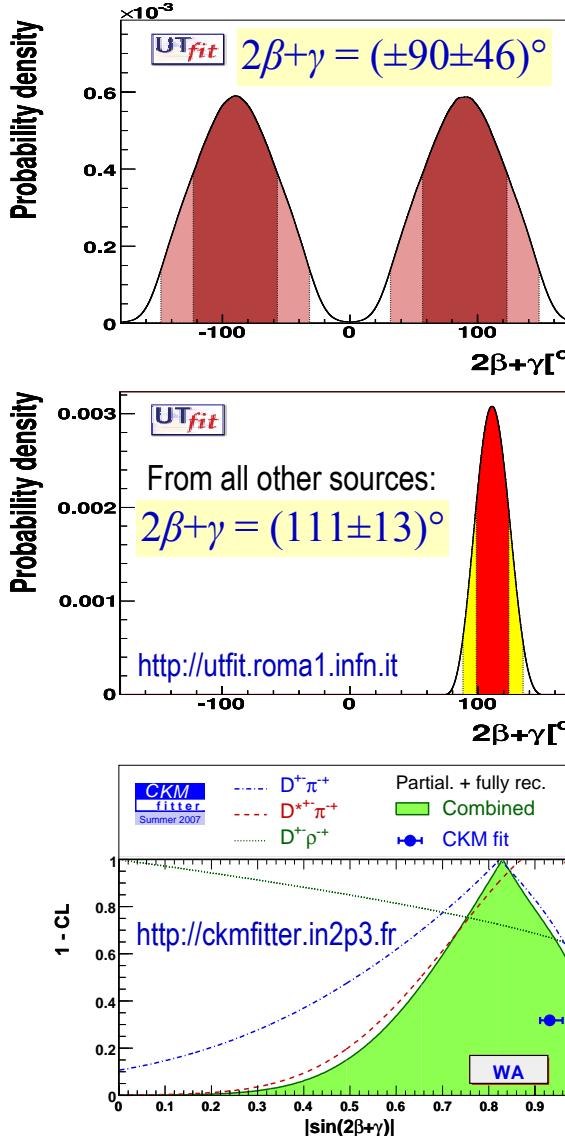
- $B^+ \rightarrow D^0_{CP} K^+$ (GLW = Gronau, London, Wyler): the first idea on the market
- $B^+ \rightarrow \bar{D}^0 K^+, D^0 \rightarrow K^+ \pi^-$ (ADS = Atwood, Dunietz, Soni): limited sensitivity
- $B^0 \rightarrow \bar{D}^0 K^{*0}$ Dalitz plot (also “ADS”) “wrong sign” D^0 decay – doubly Cabibbo-suppressed
- $B^+ \rightarrow \bar{D}^{(*)0} K^+, D^0 \rightarrow K_S^0 \pi^+ \pi^-$ Dalitz plot (GGSZ = Giri, Grossman, Soffer, Zupan)

Indirect: (model-dependent and beyond the scope of this talk)

- $SU(3)$ analysis of amplitudes in $B \rightarrow K\pi, \pi\pi$ (e.g., Gronau and Rosner, arXiv:0704.3459v3 [hep-ph])

$\sin(2\beta+\gamma)$ status as of Summer 2007

Interpretations of $B^0 \rightarrow D^\mp \pi^\pm, D^{*\mp} \pi^\pm, D^\mp \rho^\pm$ by UTfit and CKMfitter



$\sin(2\beta+\gamma)$ in $B^0 \rightarrow D^\mp K^0 \pi^\pm$ Dalitz plot

arXiv:0712.3469, accepted to Phys. Rev. D

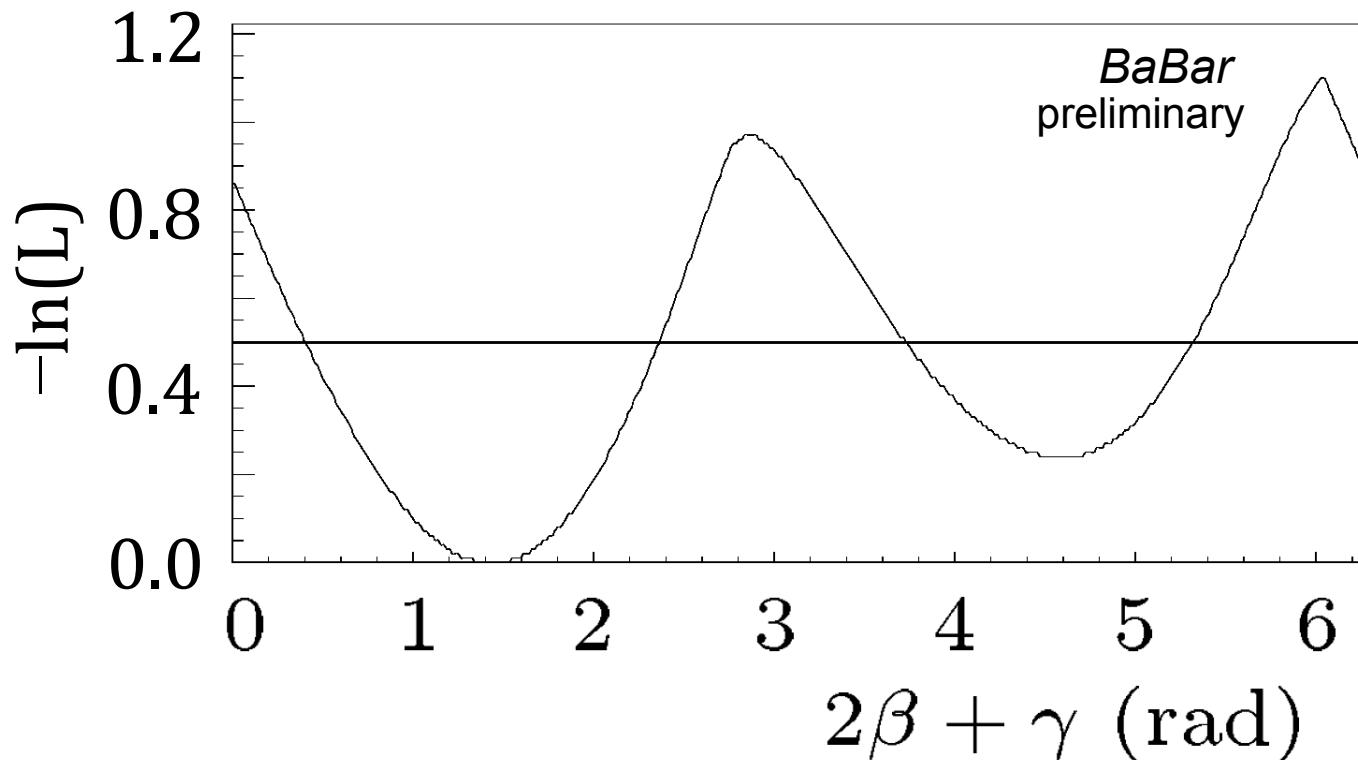


$$N_{BB} = 347M$$

Assumes $r = |A(b \rightarrow u)/A(b \rightarrow c)| = 0.3 \pm 0.1$

$$N_{\text{sig}} = 558 \pm 34$$

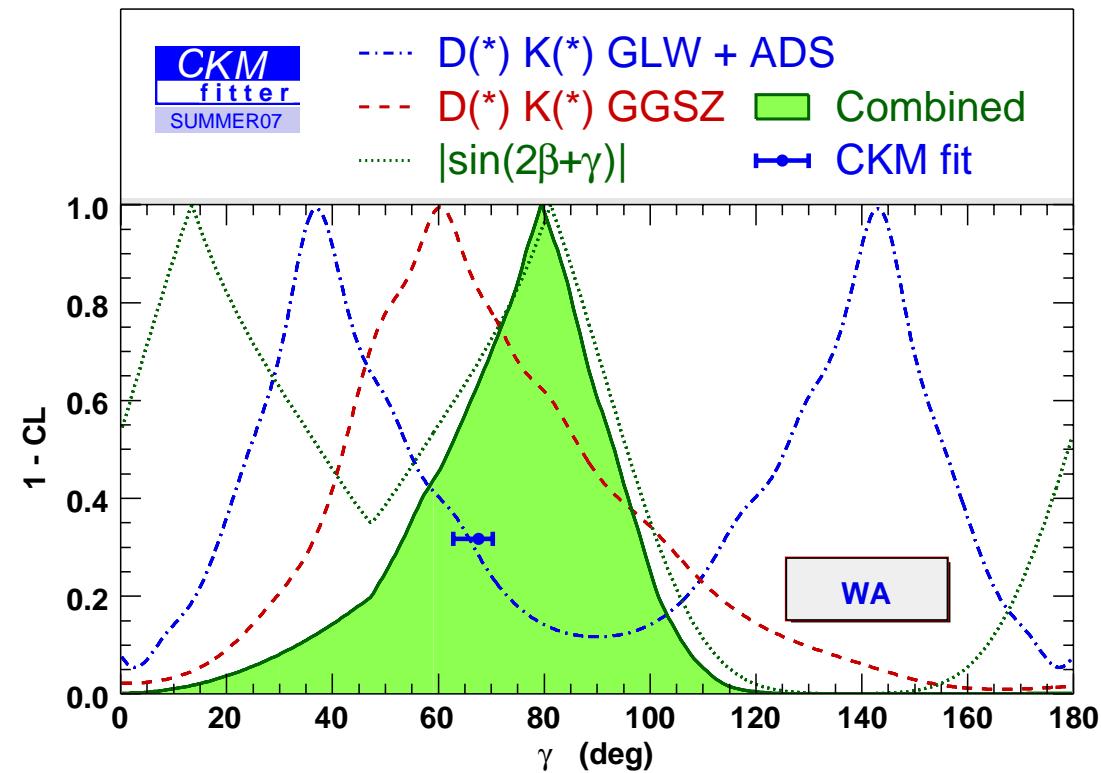
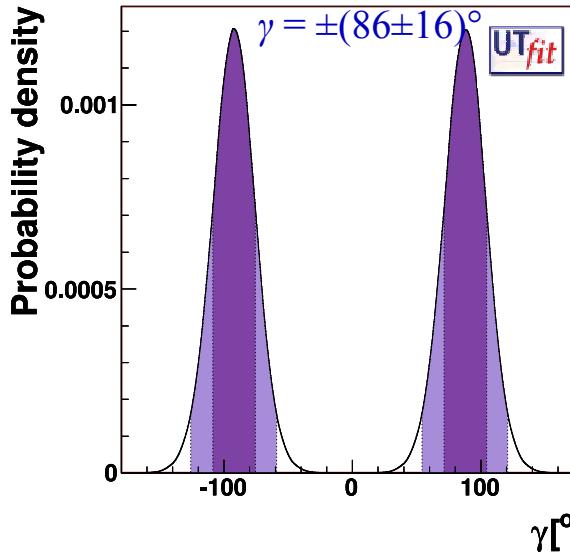
$$2\beta + \gamma = (83 \pm 53 \pm 20)^\circ \text{ or } (263 \pm 53 \pm 20)^\circ$$





γ status as of Summer 2007

Interpretations by UTfit and CKMfitter



CKMfitter: $\gamma = (80^{+18}_{-26})^\circ$

BaBar + Belle

γ in $B^0 \rightarrow \bar{D}^0 K^{*0}$ GGSZ Dalitz plot

BaBar-PUB-07/072, to be submitted to Phys. Rev. D

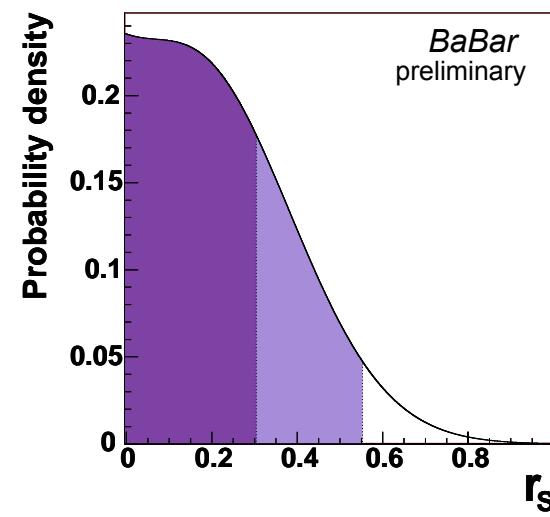
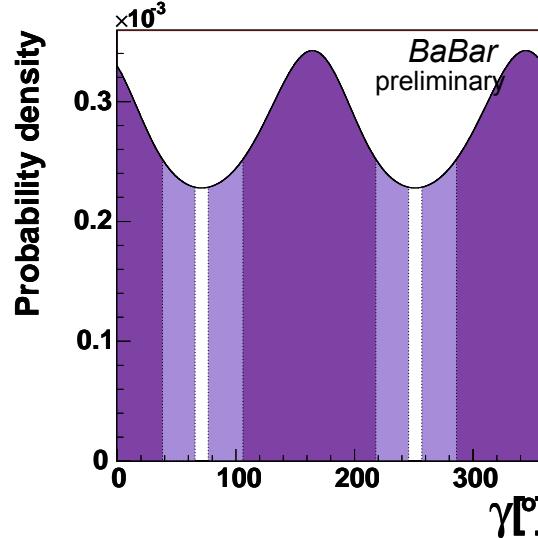
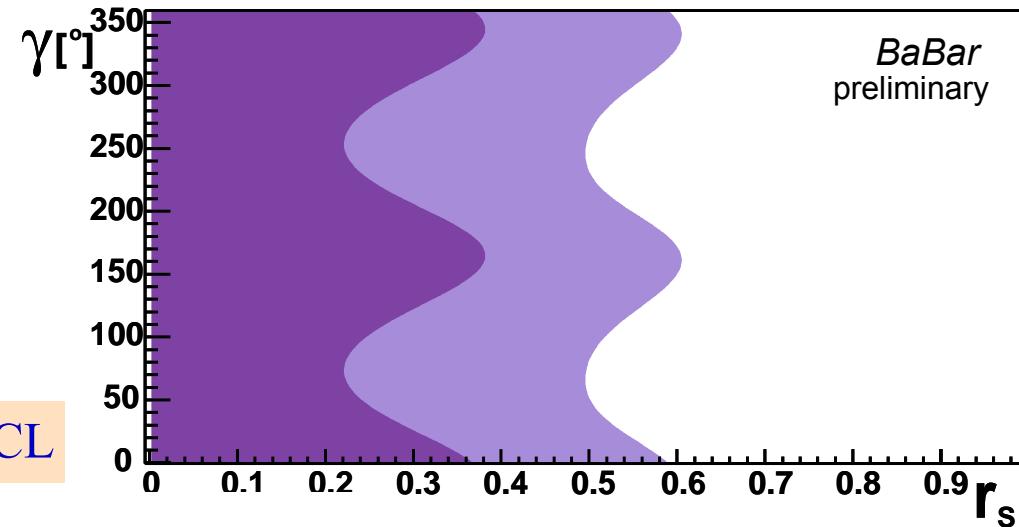


$$N_{BB} = 371M$$

$$N_{\text{sig}} = 39 \pm 9$$

$$\gamma = (162 \pm 56)^\circ \text{ or } (342 \pm 56)^\circ$$

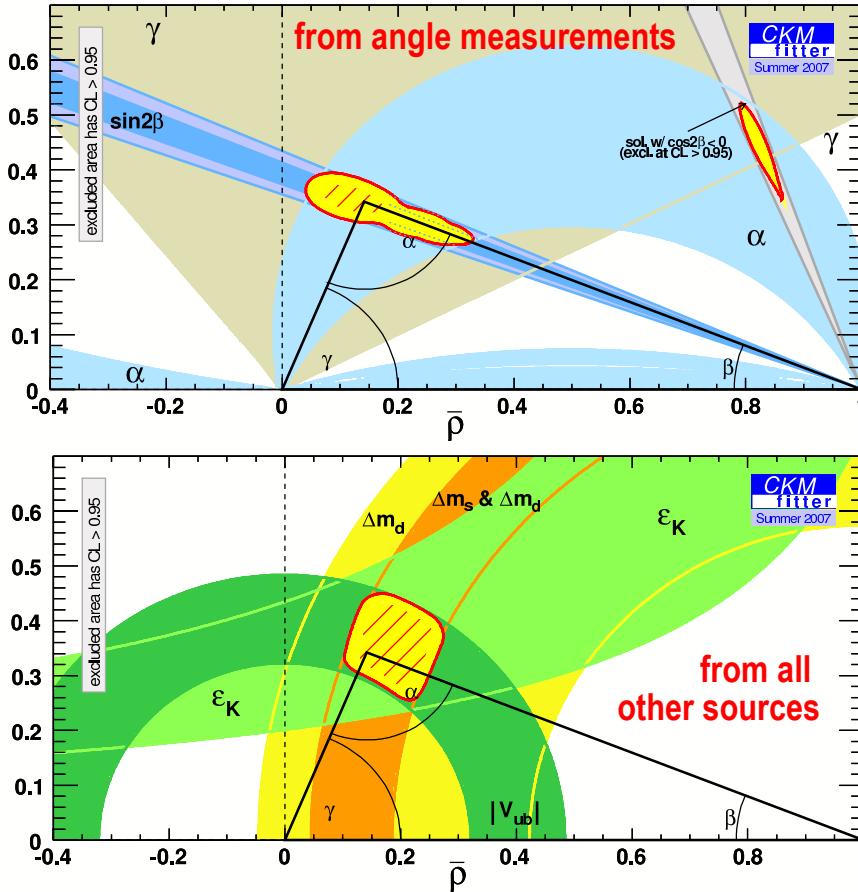
$$r_s = |A(b \rightarrow u)/A(b \rightarrow c)| < 0.55 \text{ @ 95% CL}$$



Current knowledge of the Unitarity Triangle

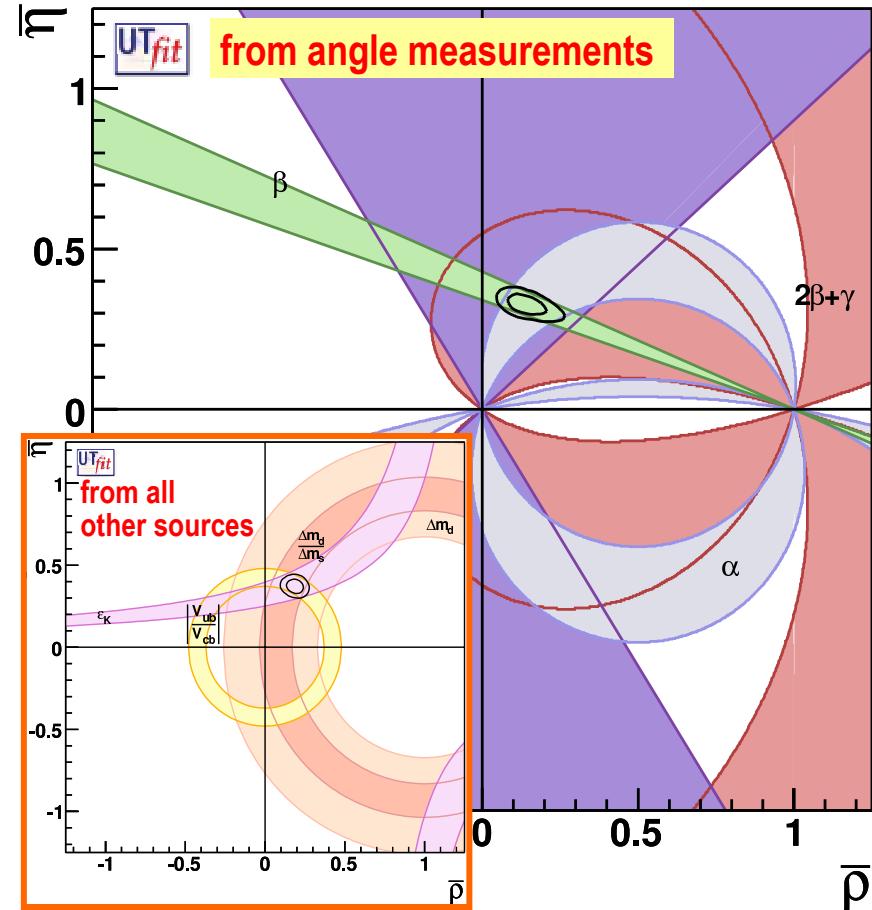
Important: nearly all measurements are still statistics-limited

A frequentist interpretation



CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005), [hep-ph/0406184],
 updated results and plots available at <http://ckmfitter.in2p3.fr>

A Bayesian interpretation, with model-dependent choices of priors



M. Ciuchini, G. D'Agostini, E. Franco, V. Lubicz, G. Martinelli, F. Parodi, P. Roudeau, A. Stocchi, JHEP 0107 (2001) 013 [hep-ph/0012308],
 updated results and plots available at <http://utfit.roma1.infn.it>

Summary and outlook

The Kobayashi-Maskawa phase has been demonstrated to be the dominant source of CP violation in meson decays.

Constraints on the CKM Unitarity Triangle from angle measurements are statistics-limited, comparable with constraints from all other sources – and mutually consistent.

The absence of statistically significant inconsistencies contains a wealth of information about the flavor structure New Physics that can be expected at the TeV scale. In particular, it pushes up the scale of new CP -violating physics in many NP models.